

# Modeling and measuring the transport of foam in porous media in the presence of nanoparticles

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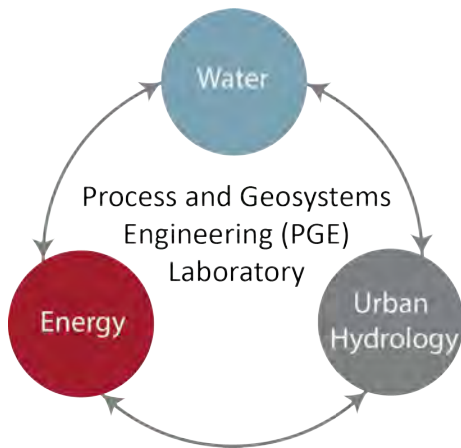
PNNL - Center for the Remediation of Complex Sites (RemPlex) - February 23<sup>rd</sup>, 2021

# Center for Environmental Systems (CES)



- **Mission:** basic and applied research for advanced technology and innovation in environmental engineering.
- **Research:** water, energy, and sustainability with applications to: wastewater and drinking water treatment, renewable energy, and CO<sub>2</sub> utilization and storage.
- **People:** 10 faculty from the Schaefer School of Engineering; 10 PhD students, 5 postdocs; and 2 project managers.
- Research funding on average is: \$ 3M per year.

# Prigiobbe research group



# Urban hydrology

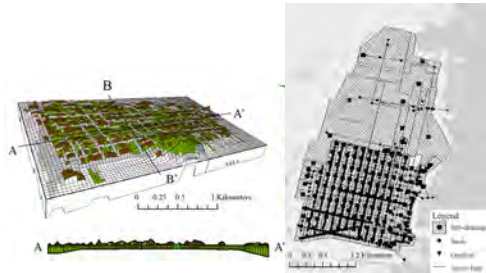
## Nuisance flooding due to groundwater

Groundwater modeling

Sewer modeling

Sewer flooding

Street flooding



Liu, Su, and Prigiobbe (2018) Water 10(12), 1774.

Su, Liu, Beheshti, and Prigiobbe (2020) Environ Sci Pollut Res 27, 14288—14298

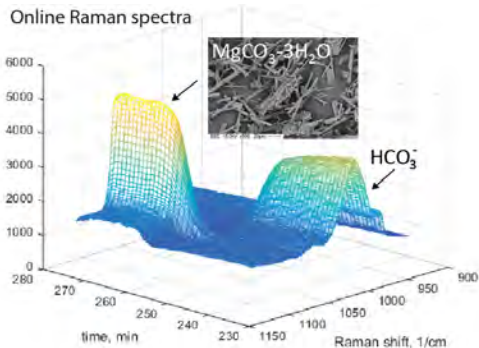
Su, Belvedere, Tosco, and Prigiobbe (202X) Studying nuisance flooding due to groundwater in a coastal urban area. In review.

Liu, Ramirez-Marquez, and Prigiobbe (202X) Combining a statistical model with machine learning to predict groundwater flooding (or infiltration) into sewer networks. In review.

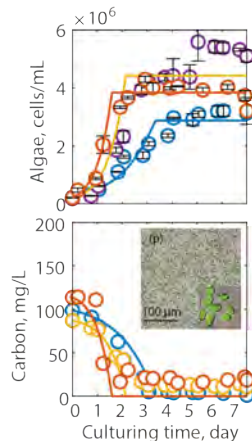
# Energy and water

## CO<sub>2</sub> mineralization for carbon utilization and storage

Precipitation of nesquehonite



Algae growth using nesquehonite



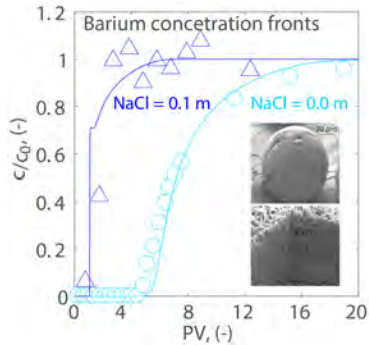
Prigiobbe (2018) *J. Env Chem Eng* 6 930–936.

Ye, Abraham, Christodoulato, and Prigiobbe (2019) *Energy Fuels* 33 8843–8851.

# Energy and water

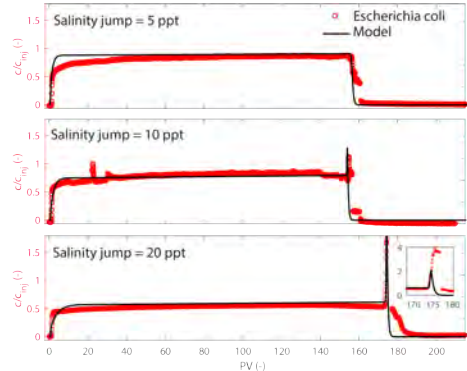
## Reactive transport in porous media

### Produced water



Ye and Prigiobbe (2018) *J Contam Hydrol* 209 24–32.  
Ye and Prigiobbe (2020) *Wat Res* 185 116258.

### Virus and bacteria

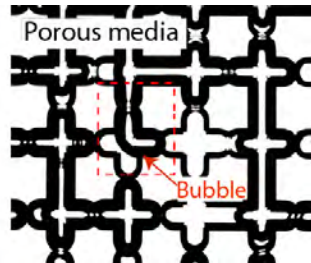


Zhang, Zabaranin, and Prigiobbe, (2019) 127, 252–263.  
Zhang and Prigiobbe (202X). Influence of salinity on *E. coli* transport behaviour. In review.

# Outline

- 1 Motivation and introduction
- 2 Mechanistic model of foam transport in porous media in the presence of nanoparticles
- 3 Experiments of foam generation in the presence of nanoparticles using a microfluidic system
- 4 Experiments of foam transport using a column-flood system for model verification
- 5 Summary and conclusions

# What is a foam?





# When is foam flooding employed?

## Enhanced-oil recovery

Continuous gas flooding



- Viscous fingering
- Gravity segregation
- Early gas breakthrough

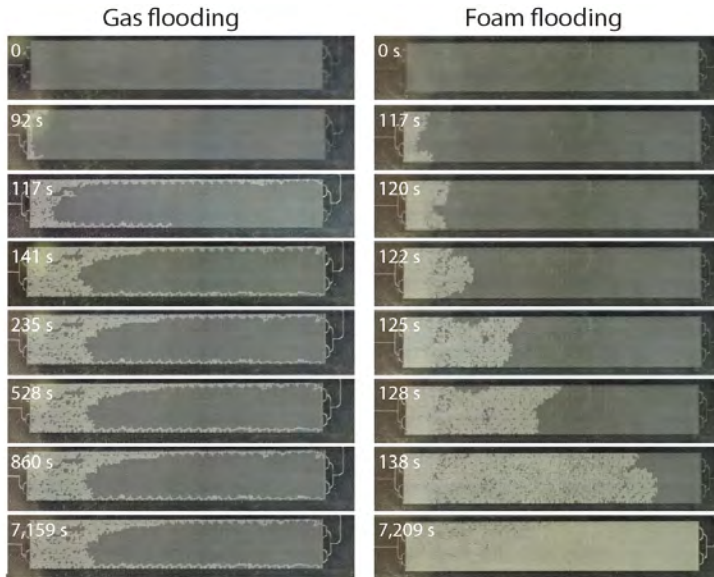
Foam flooding



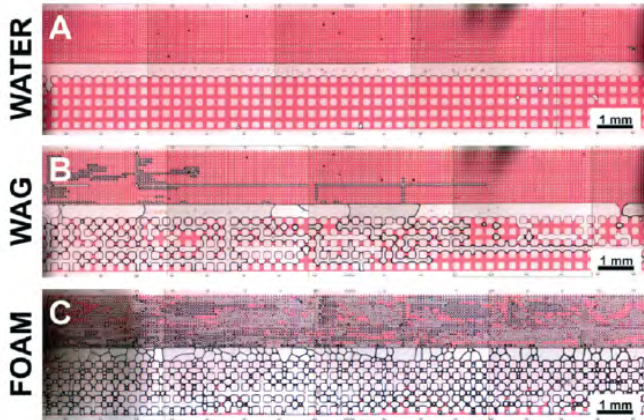
- Better sweep efficiency
- Reduction of gravity segregation
- Smoothing of heterogeneities

Rossen. Foams in enhanced oil recovery, Marcel Dekker, New York (1996).

# Better sweep efficiency and reduced fingering



# Smoothing of heterogeneities

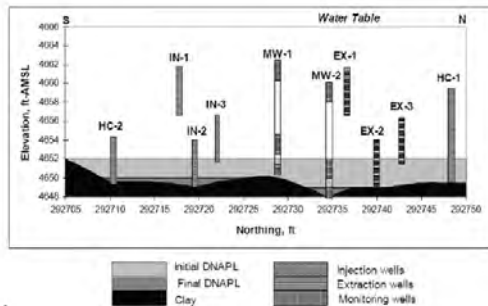


Conn, Ma, Hirasaki, and Biswal (2014) *Lab on a Chip* 14 3968.

# When is foam flooding employed?

## Foam flooding for DNAPL removal

- Formation of foam in high-permeability zones to divert surfactant solution to zones of lower permeability.
- Reduction of DNAPL saturation from 22 % to 0.03 %.
- The low water content ( $\sim 5\%$ ) reduces contaminant mobilization.

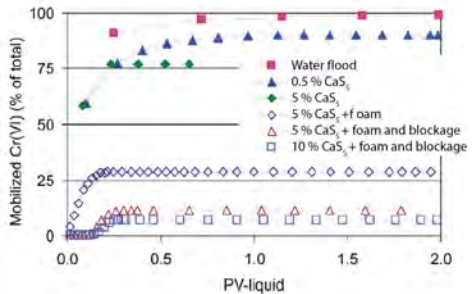


Hirasaki *et al.* (1997) Field Demonstration of the Surfactant/Foam Process for Aquifer Remediation, *SPE* 39292.

# When is foam flooding employed?

## Foam flooding for the delivery of calcium polysulfide ( $\text{CaS}_5$ )

- Delivery of amendment with water for the immobilization of metals and radionuclides in the vadose zone is inefficient and can mobilized the contaminants.
- The delivery of  $\text{CaS}_5$  with foam to immobilize  $\text{Cr(VI)}$  was reduced from 70-98% when conventional method were used to 27% when foam combined with foam-blocking was applied.



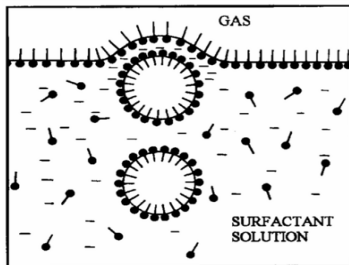
- Reaction:  $2\text{CrO}_4^{2-} + 3\text{CaS}_5 + 10\text{H}^+ \rightarrow 2\text{Cr(OH)}_3 + 15\text{S}_{(s)} + 3\text{Ca}^{2+} + 2\text{H}_2\text{O}$

Zhong, Qafoku, Szecsody, Dresel, and Zhang (2009) *Vadose Zone J.* 8 976–985.

Zhong, Qafoku, Szecsody, Dresel, and Zhang (2009) WM2009 Conference, March 1-5, 2009, Phoenix, AZ

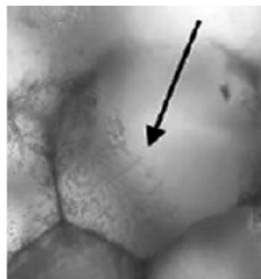
# How a foam is stabilized

## Surfactant



- Reduction of surface tension/energy.
- Elasticity of the gas-liquid interface.

## Particles



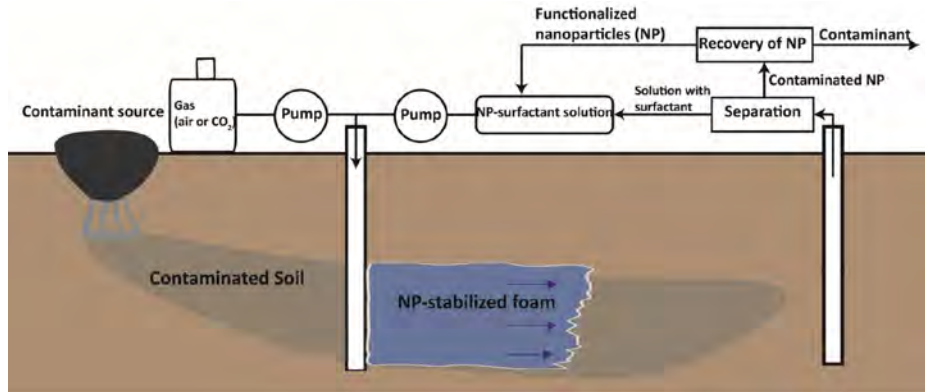
- Reduction of gas diffusion.
- Reduction of drainage.
- Increase of the critical capillary pressure ( $P_c^*$ ).

Image from: Martinez *et al.* (2008) *Soft Matter* 4.

# Nano-remediation with foam

Nano-remediation is based on the use of engineered nanoparticles for in situ degradation, transformation, or immobilization of pollutants.

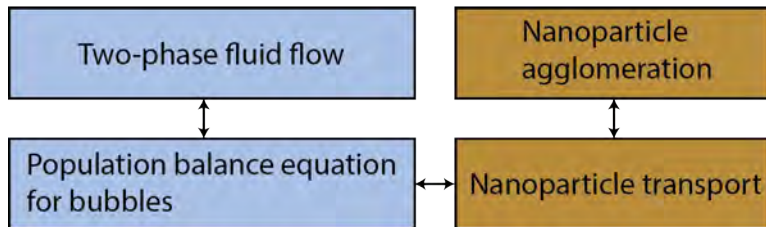
Using foam, nanoparticle mobility control is improved and water is reduced.



# Mechanistic model of foam transport in porous media in the presence of nanoparticles



# Scheme of the model



Li and Prigiobbe (2019) *Transp Porous Media* **131** 269—288.

# Modeling foam transport in porous media

## Governing equations\*

Fractional flow equation

$$\phi \frac{\partial S_w}{\partial t} + u_t \frac{\partial f_w}{\partial x} = 0,$$

Population balance equation (PBE) for bubbles

$$\phi \frac{\partial (S_g n_f)}{\partial t} + u_t \frac{\partial (f_g n_f)}{\partial x} = \phi S_g (r_g - r_c),$$

- $S_w$  and  $S_g$  are the water and the gas saturations, (-);
- $\phi$  is the porosity, (-);
- $u_t$  is the total flux, where  $u_t = u_w + u_g$ , m/s;
- $n_f$  is the bubble concentration, #/m<sup>3</sup>;
- $r_g$  and  $r_c$  are the rates of generation and coalescence, #/(m<sup>3</sup>s);
- $f_w$  is the water fraction, (-).

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\*Kovscek et al., Chem. Eng. Sci. 50(23), 1995; Kam and Rossen, SPEJ 8, 2003.

# Modeling foam transport in porous media

## Constitutive equations<sup>†</sup>

Rate of generation

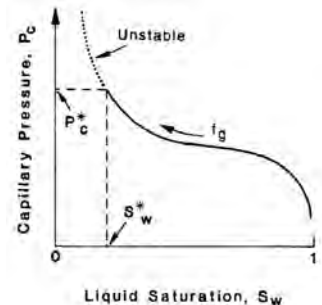
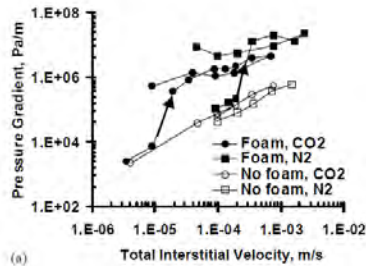
$$r_g = C_g(\nabla p)^m,$$

$C_g$  and  $m$  are model parameters.

Rate of coalescence

$$r_c = C_c n_f \left( \frac{S_w}{S_w - S_w^*} \right)^n,$$

$C_c$  and  $n$  are model parameters and  $S_w^*$  is the minimum water saturation.



<sup>†</sup>Gaughlitz *et al.*, Chem. Eng. Sci. 57, 2002. Khatib *et al.*, SPE Reservoir Eng., 1988.

# Modeling nanoparticle transport in porous media

## Governing equations of nanoparticles transport

$$\frac{\partial(\phi S_w c_w + \rho_b R)}{\partial t} + u_w \frac{\partial c_w}{\partial x} - D\phi \frac{\partial^2(S_w c_w)}{\partial x^2} = k_b S_w c_w,$$
$$\frac{\partial(\phi S_g c_g)}{\partial t} + u_g \frac{\partial c_g}{\partial x} = -k_b S_w c_w,$$

- $c$  is the nanoparticle concentration, g/m<sup>3</sup>;  $R$  is the nanoparticle retention, g/kg;  $\rho_b$  porous medium density, kg/m<sup>3</sup>;  $D$  hydrodynamic dispersion, m<sup>2</sup>/s;  $k_b$  adsorption/desorption rate, g/m<sup>3</sup>s.

## Governing equations of nanoparticles aggregation ‡

$$\frac{\partial n_p(t, x)}{\partial t} = \frac{1}{2} \int_0^\infty \beta(t, x - y, y) n_p(t, x - y) n_p(t, y) dy - n_p(t, x) \int_0^\infty \beta(t, x, y) n_p(t, y) dy,$$

- $n_p$  is the number of nanoparticle, #/m<sup>3</sup>;  $\beta$  is the aggregation kernel;  $x$  and  $y$  are characteristic length of the particles, m.

‡Kumar and Ramkrishna, Chem. Eng. Sci.(1996) 51 1333–1342.

# Modeling nanoparticle transport in porous media

## Constitutive equations

Attachment/detachment

$$\rho_b \frac{\partial R}{\partial t} = k_{att} \phi c - \rho_b k_{det} R_{max},$$

- $k_{att}$  and  $k_{det}$  attachment and detachment coefficients, (-);
- $R_{max}$ , maximum attachment capacity, g/kg.

Aggregation kernel<sup>§</sup>

$$\beta_{j,k} = \frac{2k_B T}{3\mu W_{j,k}} (r_j + r_k) \left( \frac{1}{r_j} + \frac{1}{r_k} \right),$$

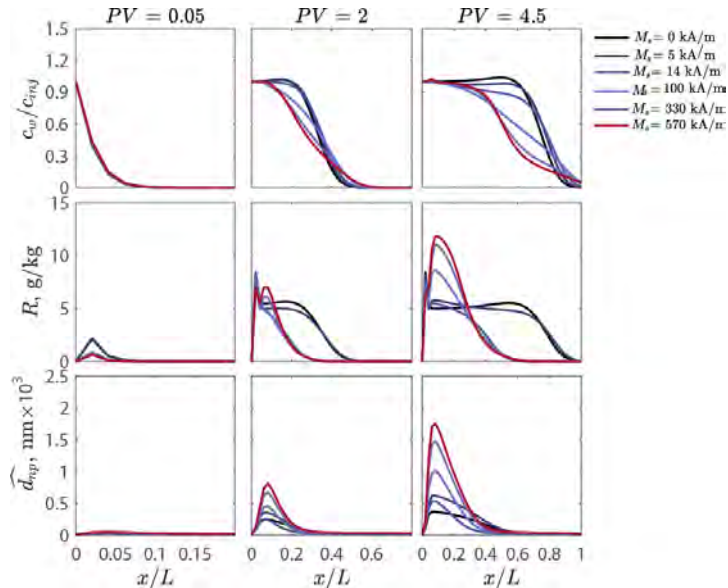
$$W_{i,k} = (r_j + r_k) \int_r^\infty \frac{e^{(V_T/K_B T)}}{r^2} dr,$$

- $V_T$ , total interaction energy, i.e., electrostatic, van der Waals, and magnetic energy.

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<sup>§</sup>Hunter and White, Foundations of Colloid Science, Clarendon Press, 1987

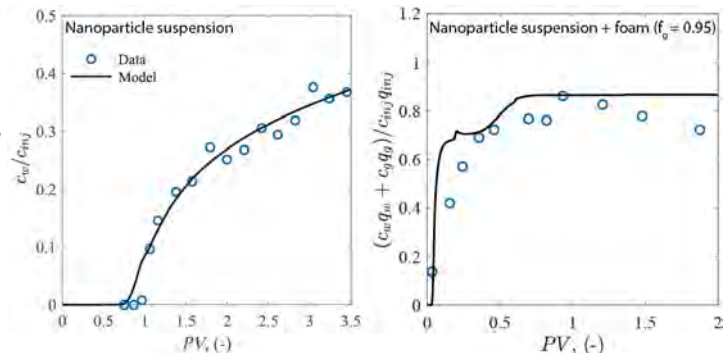
# Effect of magnetic properties of the nanoparticles



Li and Prigiobbe (2019) *Transp Porous Media* 131 269—288.

# Comparison of the model with literature data

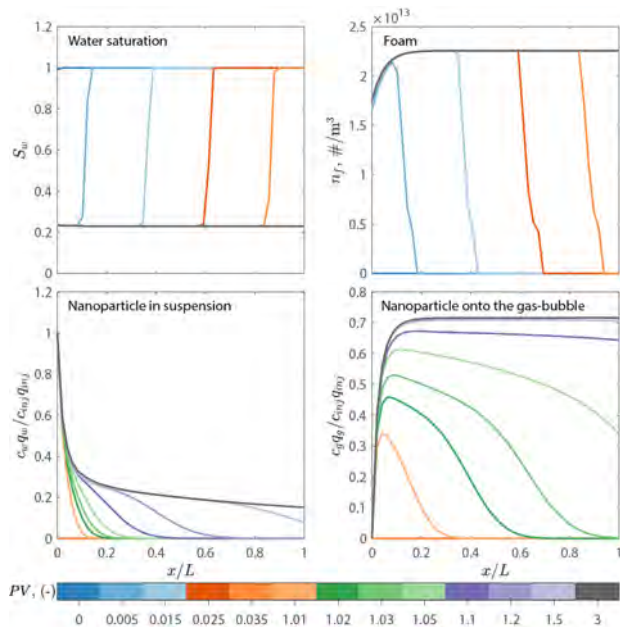
- $Q = 1.3 \text{ mL/min}$ ,
- $r_{NP} = 54.5 \text{ nm}$ ,
- $k = 1.2 \times 10^{-12} \text{ m}^2$ ,
- $c_0 = 3 \text{ g/L}$ ,



Phenrat et al. (2007) *Environ. Sci. Technol.* **41** 284.;

Ding et al. (2013) *J. Env. Eng.* **139**(9) 1206.

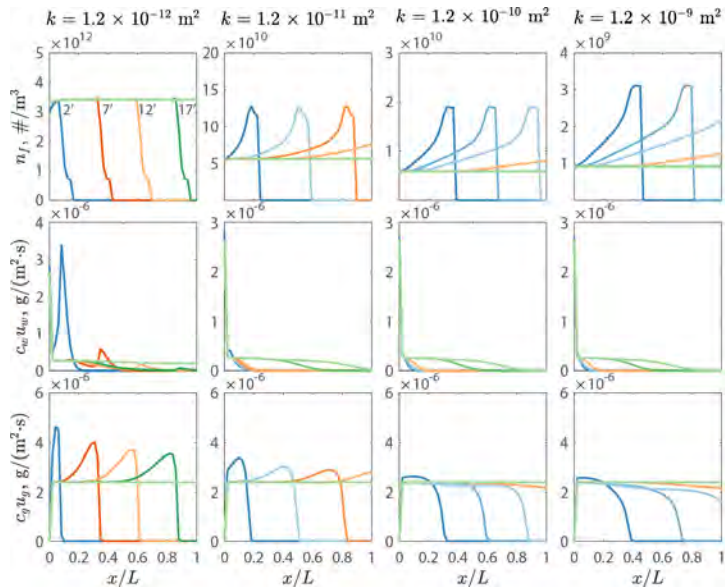
# Simulations of nanoparticle carried with foam





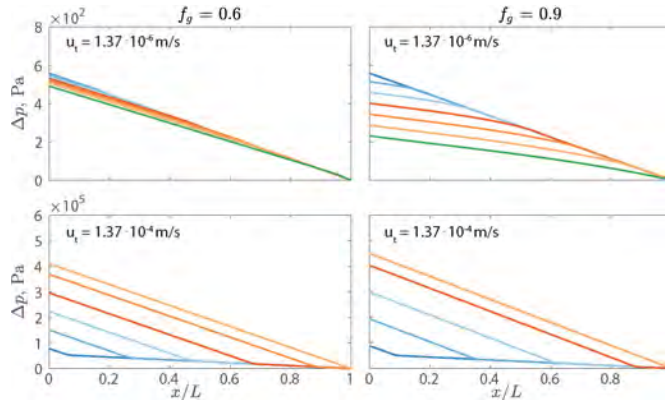
# Simulations of nanoparticle carried with foam

## Effect of permeability



# Simulations of nanoparticle carried with foam

## Pressure profiles

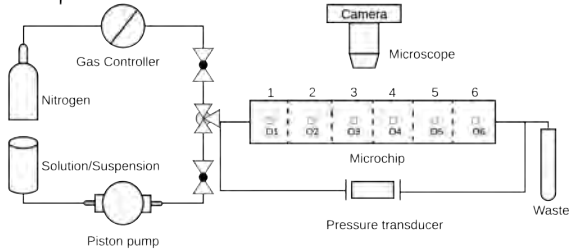


- The pressure within the domain increases with the total flux up to 500 kN/m<sup>2</sup> acceptable for applications of foam flooding in the shallow subsurface.
- For optimal design, aquifer properties should be considered to maximize delivery, minimize the duration of the operation, and contain the pressure.

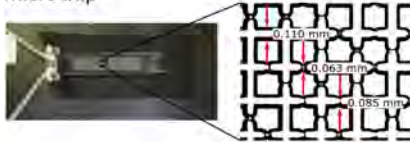
# Experiments of foam generation in the presence of nanoparticles using a microfluidic system

# Experiments

## Set-up



## Microchip



## Operating conditions:

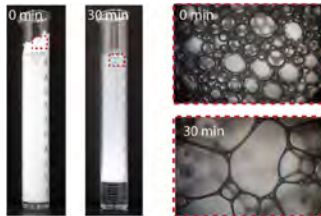
- Saturation with a brine of either surfactant (SDS, sodium dodecyl sulfate), nanoparticles (fumed silica, Nycol), or a combination.
- Nanoparticle of  $\sim 50$  nm average diameter.
- Injection of  $N_2$  at the flow-rate of 0.1-0.5 mL/min.
- Experiments were recorded with a high-speed camera in six locations (O1 through O6) and a pressure transducer.

Li and Prigiobbe (2020) *Chem Eng Sci* 215, 115427.

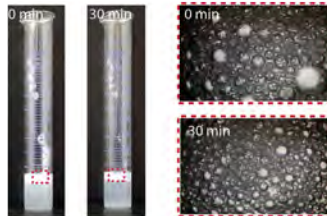
# Experiments

## Foamability and stability tests

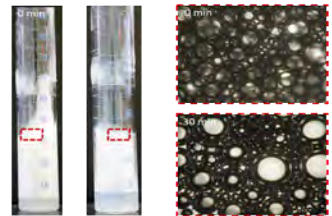
Surfactant 1 wt.% of SDS



Nanoparticles 1 wt.% of fumed silica

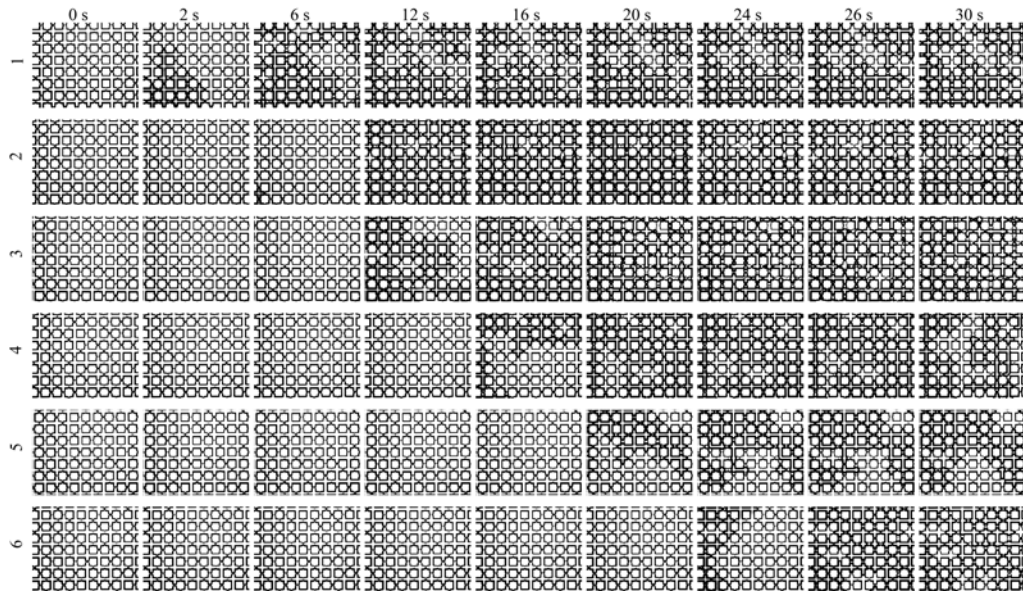


1 wt. % SDS and fumed silica



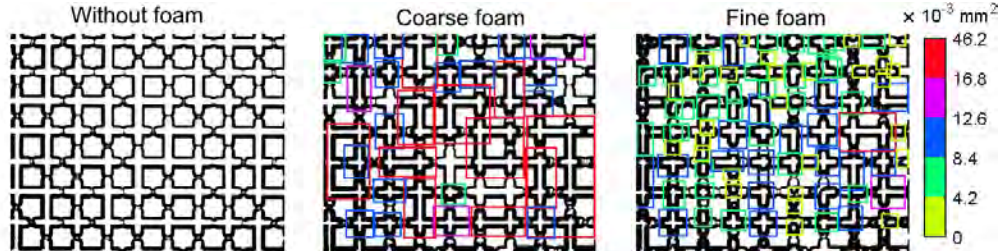
# Experiments

## Images of bubble transport across the microchip



# Image processing

- An algorithm based on convolutional neural network (CNN) was implemented for bubble recognition within the recorded images.
- Approximately 6,000 bubbles were labeled as a training data set corresponding to 60 images.
- Hundreds of bubbles in an image could be recognized within one second by using GPU acceleration (Quadro K620 GPU).



# Modeling

## Generation rate

$$r_g = \frac{dN(t)}{dt} \frac{1}{V},$$

## Bubble number evolution

$$N(t) = \sum_{i=1}^6 \frac{n_i(t)}{a_i} A_i,$$

where:

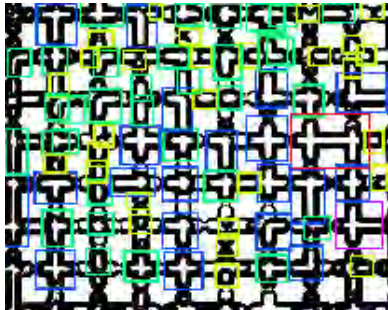
$t$  is time, s.

$N(t)$  is the total number of bubbles, #/s.

$n_i(t)$  is the bubble number in the  $i^{th}$ -view area, #/s.

$a_i$  is the  $i^{th}$  view area and  $A_i$  is the  $i^{th}$ -section area,  $m^2$ .

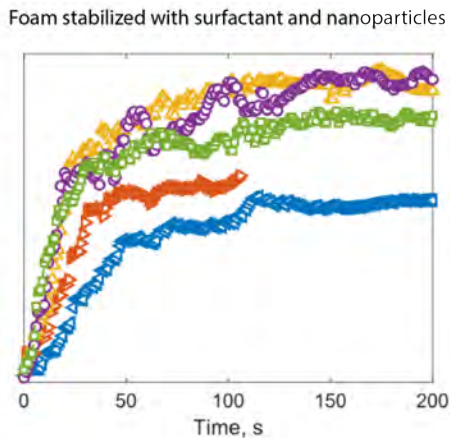
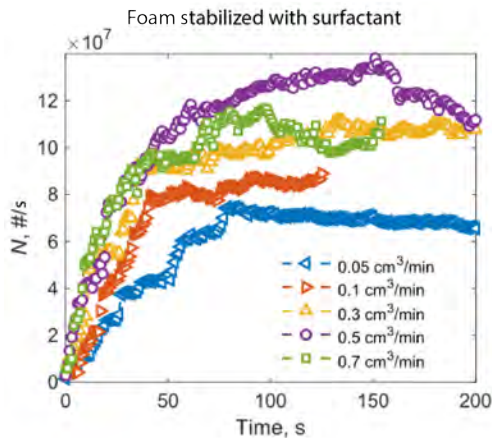
$V$  is the porous medium volume,  $m^3$ .





# Results

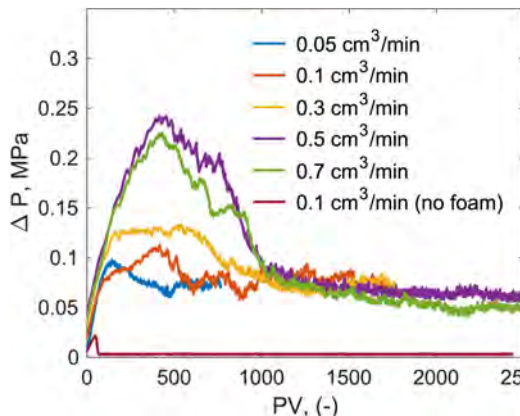
Total number of bubbles ( $N$ , #/s)



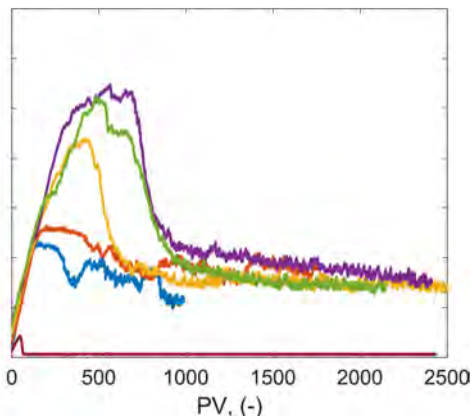
# Results

## Transport tests

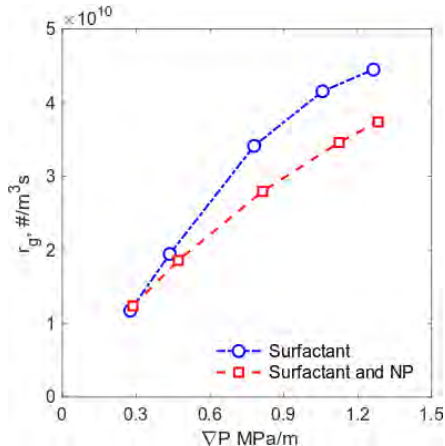
Foam stabilized with surfactant



Foam stabilized with surfactant and nanoparticles



# Foam generation rate



Generation rate,  $r_g$  ( $\#/\text{m}^3\text{s}$ )

$$r_g \propto (\nabla P)^\alpha,$$

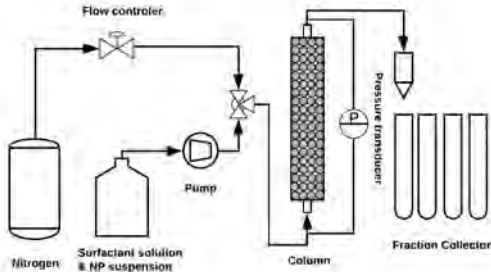
where:

$\nabla P$  is the pressure gradient, MPa.

$\alpha$  is a model parameter.

# Experiments of foam transport using a column-flood system for model verification

# Experiments



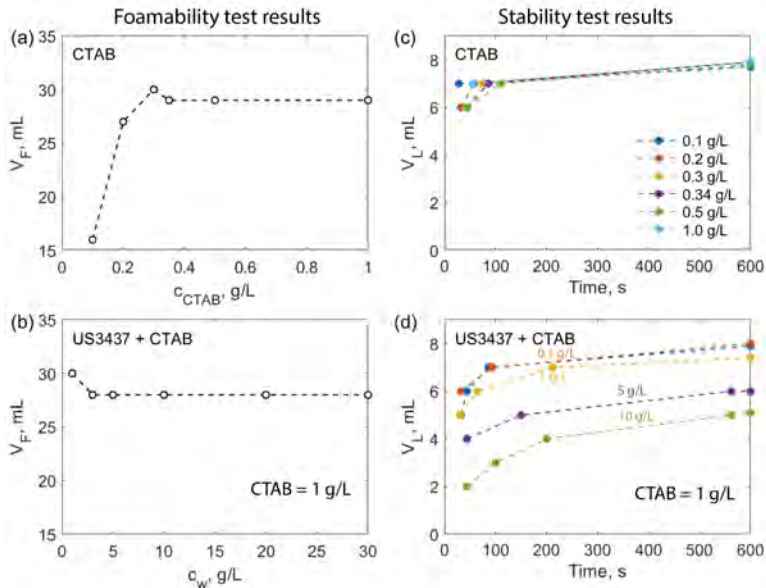
Li and Prigiobbe (202X) Modeling and measuring foam transport in the presence of nanoparticles. *In preparation*.

## Operating conditions:

- Saturation with a brine containing either surfactant (CTAB, Cetyl Trimethyl Ammonium Bromide), silica nanoparticles (US3437, US Research Nanomaterials), or a combination.
- Nanoparticle of  $\sim 50$  nm average diameter.
- Injection of  $N_2$  at the flow-rate of 0.1–1.0 mL/min.
- Experiments were monitored with a pressure transducer and sampled collected for nanoparticle concentration determination.

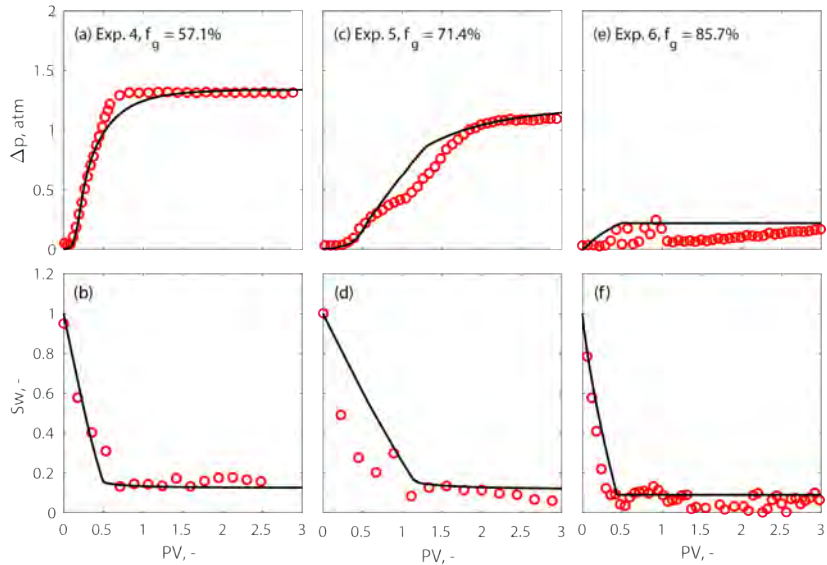
# Results

## Foamability and stability tests



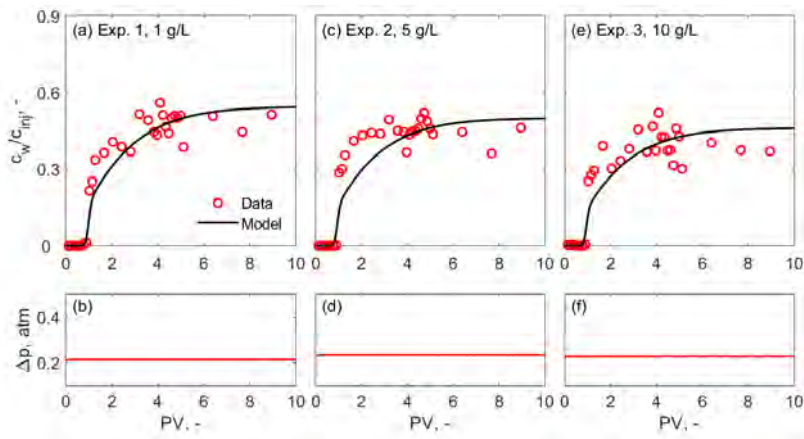
# Results

## Transport of foam stabilized with only surfactant



# Results

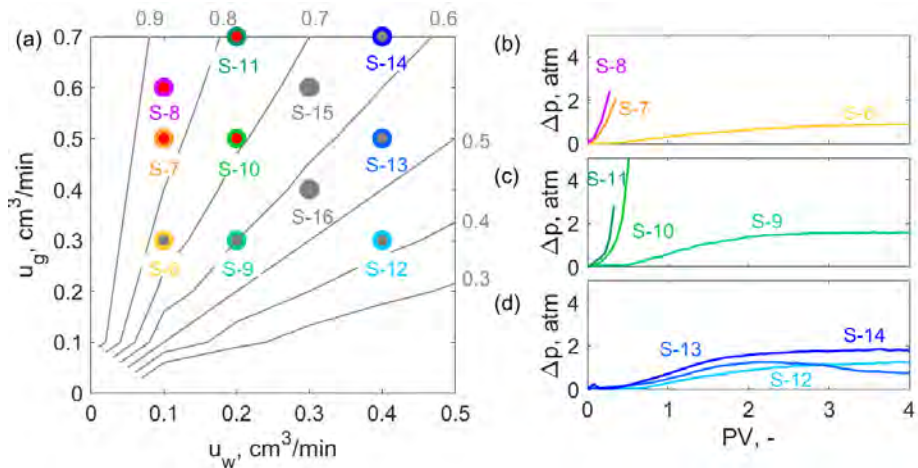
## Transport of nanoparticles





# Results

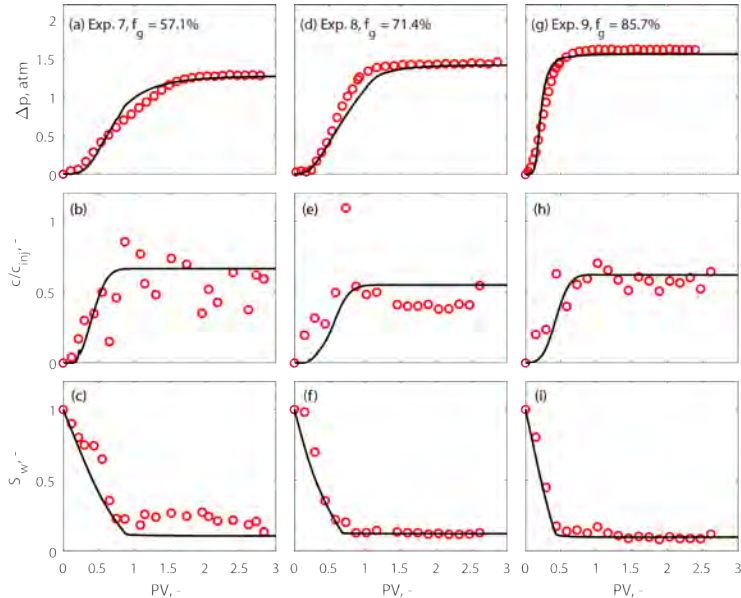
Transport of foam stabilized with surfactant and nanoparticles,  $c_w = 5$  g/L



$u_g$  and  $u_w$  are the rates of the gas and the water.

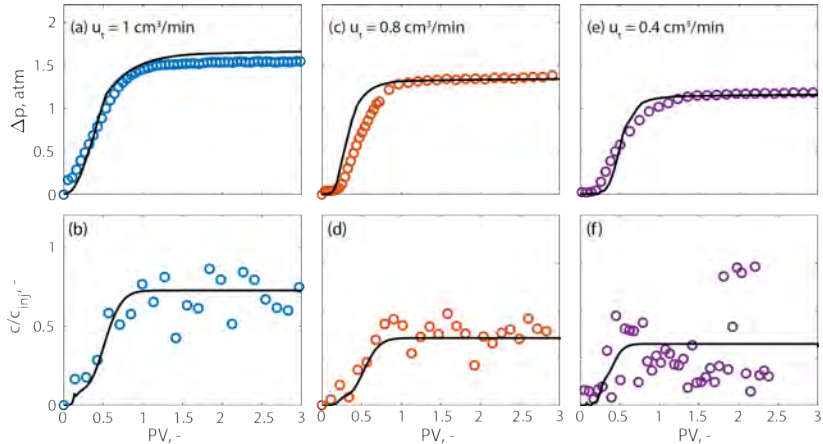
# Results

Transport of foam stabilized with surfactant and nanoparticles,  $c_w = 1$  g/L



# Results

Effect of total flow rate ( $u_t$ ,  $\text{cm}^3/\text{min}$ ) at  $f_g = 85.7\%$



Total flow rate:  $u_t = u_g + u_w$ .

# Summary and conclusions

- The use of **foam** has the potential to improve the efficiency of conventional remediation methods for contaminated sites including amendment delivery and nano-remediation where reactive nanoparticles (NPs) are used.
- Challenges are the design and the description of the process. A **mechanistic model** coupling foam and nanoparticle transport was developed and verified with experiments.
- **Simulations** show a very stable high-quality foam can be formed using NPs even in a low permeability medium within the shallow subsurface.
- **Experiments** agree very well with the model and show NPs can be delivered with high-quality foam and much faster when carried by bubbles than by water alone.
- **Future work** will focus on the extension of the model to account for chemical reactions and heterogeneity.

# Acknowledgments



Ph.D. student:  
Qingjian Li



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PRF 57739-DNI9.

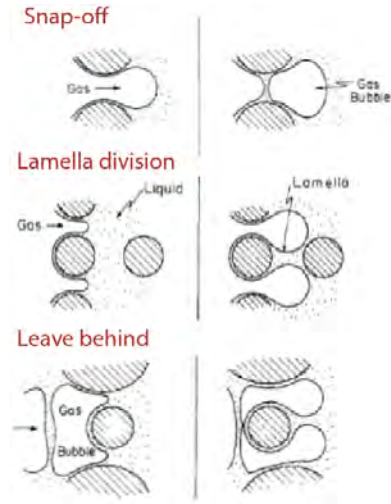


Innovation & Entrepreneurship Office  
for Academics at Stevens Institute of  
Technology.

Contact information: Valentina Prigiobbe  
Email: [valentina.prigiobbe@stevens.edu](mailto:valentina.prigiobbe@stevens.edu)

# How foam is generated

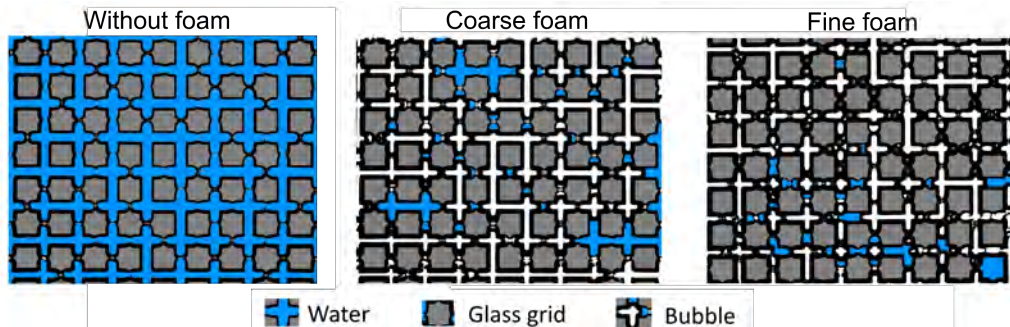
- **Snap-off.** As the bubble expands,  $P_c$  decreases favoring the water flow into the throat. Under a critical  $P_c$  value a new gas bubble forms.
- **Lamella division.** As a bubble flows through separate channels one lamella divides into two lamellae.
- **Leave behind.** The liquid is constrained into a lamella which might rupture or stay stable. It occurs below critical flow velocities and forms coarse foam.



Ransohoff and Radke (1988) *J Reservoir Eng of SPE* 3, 573–585.

# Results

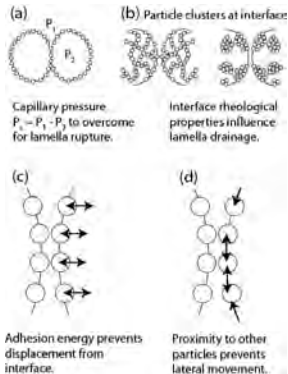
## Transport tests



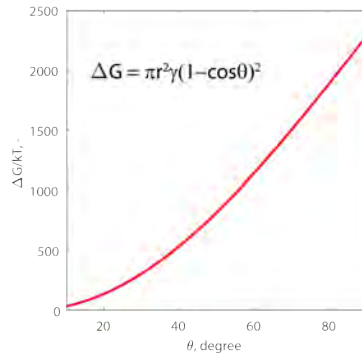
# Nanoparticle at the bubble interface

- Particle size, shape, hydrophobicity/wettability, concentration, capillary attraction, and solution composition are the main factors for foam stabilization.
- Flocculation between the armored bubbles and the unadsorbed particles and particle packing reduces drainage and increases foam strength.

## Configurations



## Gibbs free energy of particle desorption

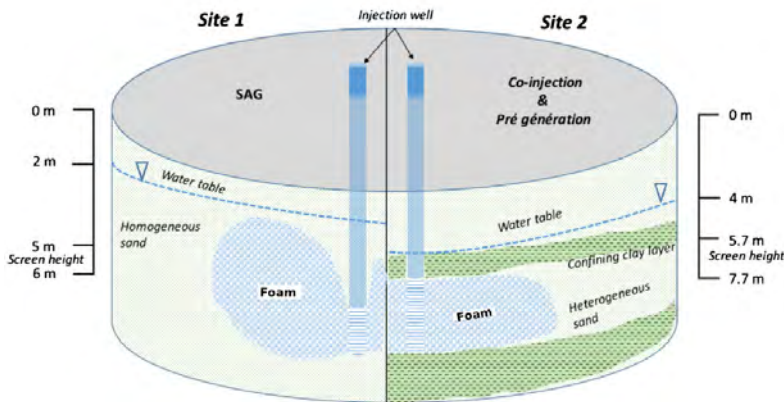


Pugh (2016) *Bubble and Foam Chemistry*. Cambridge.



# Application of foam for environmental remediation at the field scale

## Foam as a blocking agent



Portois et al. (2018) *Transp Porous Med* 124 787–801.