Enhancement of Solar Energy Representation in the GCAM Model

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Abstract

The representation of solar technologies in a research version of the GCAM (formerly MiniCAM) integrated assessment model (GCAM-RE) have been enhanced to add technologies, improve the underlying data, and improve the interaction with the rest of the model. We find the largest potential impact is from the inclusion of thermal Concentrating Solar Power plants, which supply a substantial portion of electric generation in sunny regions of the world. Drawing on NREL research, domestic Solar Hot Water technologies have also been added in the United States region where this technology competes with conventional electric and gas technologies. PV technologies are implemented in the CCTP scenarios, drawing on NREL cost curves for the United States, extrapolated to other world regions using a spatial analysis of population and solar resources.
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1 Introduction

1.1 Research Outline

This work is part of ongoing research to enhance the representation of renewable and end-use energy technologies in the long-term integrated assessment model GCAM (formerly MiniCAM). In previous work building and industrial end-use technologies were enhanced to explicitly represent specific services such as heating, cooling, and hot water along with specific technology options for supplying these services (Rong et al. 2007; Kyle et al. 2009, Wise et al. 2007). Previously an explicit representation of wind technologies and resources was also implemented (Kyle et al. 2007) as well as an enhanced representation of geothermal energy (Hannam et al. 2010).

This report describes work to date to improve the representation of solar energy generation in the model. We have focused on three technologies: thermal Concentrating Solar Power (CSP), domestic Solar Hot Water (SHW), and both rooftop and central station photovoltaic technologies (PV). These are described in the following sections.

The interaction of these technologies with other renewable technologies, the rest of the energy system, and with climate policies will be explored in the next phase of this research. The renewable technology representations described here will be combined with a new representation of the US electricity system that explicitly models different load segments (Wise and Smith 2007). Using this enhanced model, focusing on the United States, the potential role of renewable energy technologies in providing domestic energy supply and lowering greenhouse emissions will be examined.

1.2 ObjECTS GCAM Model

The Object-oriented Energy, Climate, and Technology Systems (ObjECTS) framework uses a flexible, object-oriented modeling structure to implement an enhanced version of the partial-equilibrium GCAM (formerly MiniCAM) model (Kim et al. 2006). The ObjECTS GCAM is an integrated model of the economy, energy supply and demand technologies, agriculture, land-use, carbon-cycle, and climate. This framework is intended to bridge the gap between “bottom-up” technology models and “top-down” macro-economic models. By allowing a greater level of detail where needed, while still enabling interaction between all model components, the ObjECTS framework allows a high degree of technological detail while retaining system-level feedbacks and interactions. By using object-oriented programming techniques (Kim et al. 2006), the model is structured to be data-driven, which means that new model configurations can be created by changing only input data without changing the underlying model code.

The GCAM is a partial-equilibrium model structure that is designed to examine long-term, large-scale changes in global and regional energy systems. The GCAM has a strong
focus on energy supply technologies and has been recently expanded to include a comprehensive suite of end-use technologies. The GCAM (then called MiniCAM) was one of the models used to generate the IPCC SRES scenarios (Nakicenovic and Swart 2000). This model has been used in a number of national and international assessment and modeling activities such as the Energy Modeling Forum (EMF; Edmonds, et al. 2004, Smith and Wigley 2006), the U.S. Climate Change Technology Program (CCTP; Clarke et al. 2006), and the U.S. Climate Change Science Program (CCSP; Clarke et al. 2007) and IPCC assessment reports.

The GCAM model is calibrated to 1990 and 2005 and operates in 15-year time steps to the year 2095. It takes inputs such as labor productivity growth, population, fossil and non-fossil fuel resources, energy technology characteristics, and productivity growth rates and generates outputs of energy supplies and demands by fuel (such as oil and gas) and energy carriers (such as electricity), agricultural supplies and demands, emissions of greenhouse gases (carbon dioxide, CO2; methane, CH4; nitrous oxide, N2O), and emissions of other radiatively important compounds (sulfur dioxide, SO2; nitrogen oxides, NOx; carbon monoxide, CO; volatile organic compounds, VOC; organic carbon aerosols, OC; black carbon aerosols, BC). The model has its roots in Edmonds and Reilly (1985), and has been continuously updated (Edmonds et al. 1996; Kim et al. 2006). GCAM also incorporates MAGICC, a model of the carbon cycle, atmospheric processes, and global climate change (Raper et al. 1996; Wigley and Raper 1992).

The detailed representations described here have been implemented and tested in a version of the GCAM that will be identified in this report as GCAM-RE (GCAM-Renewables).

2 CSP Electricity Generation

Thermal Concentrating Solar Power (CSP) plants concentrate direct solar radiation to produce heat and generate electricity using a turbine or thermal engine. One advantage of CSP technologies is that generation at times when solar radiation is not available can be provided by use of an auxiliary heating system, which is a low capital cost addition to the plant. All current plants are built as hybrid plants enabling them to provide firm power. CSP technology used in this way, therefore, sidesteps the intermittency issue.

CSP technology in the GCAM-RE model is implemented as described in the PNNL report by Zhang and Smith (2008) and in a submitted journal paper (Zhang et al 2009). Details of the implementation can be found in these documents. Separate technologies are implemented for intermediate and peak generation without thermal storage, intermediate and peak generation with several hours of thermal storage, and baseload generation with large amounts of thermal storage.

As described in the above references, a parameterization was developed (Figure 1) that determines the use of auxiliary generation as a function of penetration. Similarly, the
amount of solar energy lost due to exceeding demand as a function of penetration is also parameterized.

![Figure 1 – Auxiliary generation as a function of penetration for intermediate and peak generation with thermal storage.](image)

We find that a critical parameter characterizing the performance of CSP technologies is the number of days of low direct normal irradiance when this technology cannot operate. This data is not generally available, although it can be approximated using the National Solar Radiation Data Base (NSRDB). We developed a correlation between the NSRDB and globally gridded parameters from NASA to estimate the number of low direct normal irradiance (DNI) days globally (Figure 2). Average irradiance on sunny days is much more similar in different world regions than total direct normal irradiance, which averages over low DNI days, making the estimate of low DNI days an important priority for future research.

In prime areas with relatively few low DNI days, CSP technologies need to consume little backup fuel (assumed to be either natural gas or biomass). In areas with a larger number of low DNI days, CSP technologies can still have a role, acting in essence as fuel extenders by combining solar energy with either natural gas or biomass.

A key feature of the solar resource is that high quality solar resource is generally spatially concentrated within most regions. Therefore, assumptions are necessary for the extent to which electricity generated in sunny regions can be transmitted to other regions. In a reference case set of assumptions CSP power can provide the largest share of intermediate and peak generation and a significant fraction of baseload generation in those regions with good quality CSP resources. A more substantial expansion of CSP will require large-scale transmission capacity to transmit power to regions more distant from the highest quality solar resources.
Figure 2 – Estimate of low DNI days (< 3,000 W/m² per day) where thermal CSP plants were assumed to not be operational.

Figure 3 shows the fraction of US electric load under a reference case scenario (Zhang et al. 2009). We find that CSP is highly competitive as technology serving intermediate and peak loads. Systems without thermal storage are competitive but systems with thermal storage are more competitive if these are developed and deployed as assumed here. In the US south-west and west where the highest quality solar resources are located we find CSP technologies are capable of providing a large fraction of intermediate and peak load.

Fraction of US Electric Load

Figure 3 – Fraction of total U.S. electric load supplied by thermal CSP technologies under a reference case scenario.
Baseload CSP plants with around 12 hours of thermal storage become more competitive later in the century and supply an increasing share of US electricity as costs are assumed to decline over time.

3 Domestic Solar Hot Water

3.1 Overview

Solar domestic hot water (SDHW) systems in the United States region are implemented in GCAM-RE as additional technologies that can supply hot water service. These technologies are implemented in a similar manner to the other building end-use technologies, that is, with an efficiency and an amortized capital and maintenance cost. Solar hot water technologies will also be subject to a capacity limit which represents buildings that cannot be serviced by this technology due to shading or building type, such as high-rise buildings. For consistency with other solar work for GCAM these calculations are conducted globally using GIS tools and global data sets so that these results can potentially be applied to all regions in the model and to US sub-regions if desired.

3.2 SHW Parameters

To implement SHW in the GCAM-RE model we will take advantage of the finding of Christensen and Barker (1999) that solar system efficiency, defined as energy savings divided by incident solar energy, is roughly constant across a wide range of climatic zones. As a formula, this becomes:

$$\frac{E_{conv}^{sav} - E_{SHW}^{aux sav}}{E_{solar}} = C_{SHW}, \text{ where}$$

1) 

$E_{conv}^{sav} = $ Amount of energy consumed by a conventional hot water system not including losses. (see below)

$E_{SHW}^{aux sav} = $ Amount of auxiliary energy consumed by the solar hot water system not including tank losses. (see below)

$E_{solar} = $ Amount of solar energy incident on the solar hot water collector

$C_{SHW} = $ A constant that characterizes a particular solar hot water system (referred to by Christensen and Barker (1999) as the system efficiency)

The formulation in Equation (1) is, formally, slightly different than the definition used by Christensen and Barker (1999) in that our formulation would formally include other changes in the overall system efficiency due to the operation of a solar hot water system as compared to a conventional hot water system. For properly sized systems, these
differences should generally be negligible.\textsuperscript{1} Given the aggregate nature of our application, this simplification does not introduce significant error compared to other uncertainties.

The constant $C_{SHW}$ has a small dependence on ambient temperature; however for purposes of this project these will be neglected. There is a significant dependence on water draw amount, whereby $C_{SHW}$ decreases significantly as the draw amount decreases (from 0.43 to 0.33 as the draw was halved from 300 liters/day to 150 liters/day). Given the national level of this implementation it is difficult to determine the appropriate average value for water draw. However, given that our top-down calibration (see below) indicates an average daily water draw on the low end of the consumption range, we use the intermediate assumption of 225 liters/day draw and a base value for $C_{SHW} = 0.39$. A newer algorithm for mains temperature and adjustment for pipe losses reduces this value to $C_{SHW} = 0.36$. (J. Burch, pers com), which is the value used in this work.

Two of the terms in Equation (1) can be estimated for any given point on the globe given data developed as part of this project: $E_{conv}^{sav}$ and $E_{solar}^{sav}$. The incident solar energy is simply the average annual solar irradiance times the solar collector area. Solar irradiance is taken from the NASA SEE estimate, where we used annual average values for the radiation on equator-pointed 48 Degree tilted surfaces.

The energy needed for conventional water heating ($E_{conv}^{sav}$), not including losses, is approximately equal to:

\begin{equation}
E_{conv}^{sav} = c_p \cdot V \cdot (T_{hw} - T_{mains}) / \epsilon_{recov}, \text{ or }
\end{equation}

the annual hot water draw ($V$) times the specific heat of water and the annual average temperature difference between mains and the hot water set point over the conventional water heater energy recovery efficiency. A set point of 55°C (Christensen and Barker 1999) is assumed. The estimate of mains temperature used here is described in the appendix. The energy recovery efficiency is the instantaneous efficiency of the auxiliary heating system not including conductive and diffusive losses, and is approximately 1 for electric systems and 0.82 for gas-fired systems. The energy recovery efficiency is used in the calculation of energy savings (Equation 1) instead of the net system efficiency (also called the energy factor) because other system losses are, to first order, common to both solar and conventional systems.\textsuperscript{1}

Solving for auxiliary energy demand,

\begin{equation}
E_{SHW}^{aux} = E_{conv}^{sav} - C_{SHW} \cdot E_{solar}^{sav}.
\end{equation}

A population-weighted average estimate for the amount auxiliary heat demand can be calculated for each region given the two quantities estimated above. For consistency with the source calculation for the system efficiency constant we assume a collector area of

\textsuperscript{1} Thanks to Jay Burch (pers communication) for pointing out this distinction.
3.72 m\textsuperscript{2} (Christensen and Barker 1999) for this calculation. Following Christensen and Barker (1999) we place a limit of $E_{SHW,aux}^{sav} \leq 0.2E_{conv}^{sav}$ for each grid cell.

In its simplest form, GCAM operates with two inputs for each technology, an amortized capital plus non-fuel O&M cost and an I-O coefficient that represents the amount of energy input needed for a unit of service output (this is an inverse efficiency). Because the “efficiency” for SHW can be > 1 for sunny regions, for clarity, we will work with I-O coefficients. Because energy demand is inversely proportional to efficiency, the I-O coefficient for the SHW technology will be related to the efficiency of a conventional technology as:

\begin{equation}
C_{I-O}^{SHW} = \left( \frac{E_{SHW,aux}^{sav}}{E_{SHW}^{sav}} \right) / E_{conv}^{sav},
\end{equation}

or in terms of efficiency,

\begin{equation}
\epsilon_{SHW} = \epsilon_{conv} \cdot \left( \frac{E_{conv}^{sav}}{E_{SHW,aux}^{sav}} \right),
\end{equation}

where the energy quantities are regional average values as calculated above and $\epsilon_{conv}$ is the system efficiency (energy factor) for the conventional system. As above, we have assumed that losses from the storage tank are similar for both systems.\textsuperscript{2} SHW heaters could potentially use either electric or gas backup systems, and both are included as options.

The total cost of both conventional and SHW technologies will have a central value and a distribution that depends largely on geographic location, but also on fuel cost variations. This is the situation described by Clark and Edmonds (1993) where the logit choice formulation used in the GCAM model is applicable. While the logit choice mechanism is strictly applicable if the shapes of the distributions are identical, given the many uncertainties, any error introduced by this inconsistency is acceptable. In this case, the cost distribution for SHW systems is best fit by a logit exponent of -3, which is a much wider cost distribution than that for conventional systems.

For the USA, where we can embed the SHW technology into the detailed buildings model, the fraction of regional demand that can be supplied by SHW (see below) can be implemented into the model as a capacity limit.

\textsuperscript{2} Equation 4 formally would use the actual conventional and auxiliary energy consumption, however, both of these are proportional to the $\_sav$ quantities with a conversion factor of $\epsilon_{recov} / \epsilon_{conv}$, which cancels.
For other regions (and the aggregate USA buildings implementation) the solar hot water supply sector would have to compete as another technology option in the aggregate buildings representation. This could be done similarly to the USA detailed version except the capacity limit would also need to incorporate the fraction of the total building demand for hot water services. This may be investigated in the future. An additional issue is the amount of hot water demand per person in other world regions. In many world regions per-capita hot water demand is much lower than in the United States. Values for Japan and/or Europe could be used for other world regions.

3.3 Cost of SHW Service

The cost of SHW service can be broken into two parts: the capital and (non-fuel) O&M costs of the SHW system, and the cost of purchasing backup energy. The total cost of conventional and solar hot water heating, respectively, would therefore be:

6) cost of SHW: \( c_{\text{SHW}} + c_{\text{fuel}}^{\text{SHW}} \), and

cost of Conv HW: \( c_{\text{conv}} + c_{\text{fuel}}^{\text{conv}} \),

where \( c_{\text{conv}} \) and \( c_{\text{shw}} \) are the amortized capital and maintenance costs for conventional and solar hot water systems respectively, and the second terms are annual fuel costs.

The amortized capital and O&M costs for the SHW systems will be determined using the same financing assumptions as used for conventional hot water systems. One significant difference, however, is lifetime. Many conventional hot water systems have relatively short lifetimes, and low capital cost. SHW systems generally have longer lifetimes of around 20 years.

3.4 Preliminary Results

Figure 4 shows a preliminary calculation of the penetration of SHW systems in the United States under a reference case with no climate policy. Capital costs for SHW were assumed to be $6,000 in 2005 as found in a recent review of costs in California (KEMA 2009), declining by 2% per year. The cost used here is similar to the average active system cost of $4,960, found in a market review conducted by the authors, assuming installation costs are 23% of total cost (KEMA, Inc.). A review conducted in New York state, however, found much higher costs of $9,000-$11,000 for flat panel systems (Perlman & McNamara 2008), in part due to much larger installation costs averaging 50% of total cost. While these costs are from different studies that may not have similar methodologies, it appears that costs for a colder climate such as New York may be substantially higher than costs in sunnier regions. In the implementation proposed here, the installed cost should be an average cost in areas where solar systems could be used. If this cost differential proves to be accurate, then further consideration of the appropriate value for the assumed average installed cost would be warranted.
In this preliminary implementation (Figure 4), SHW systems begin to provide a significant fraction of hot water service by mid-century once system costs were assumed to have decrease. The capital cost of SHW systems was assumed to decrease by 2% per year between 2005 and 2035 and 1% per year thereafter, resulting in capital costs approximately twice that of conventional systems by the end of the century.

Electric heat pump technologies increase market share at the expense of conventional technologies due to their higher efficiencies and increases in the cost of natural gas. Solar technologies can be even more efficient than heat pumps in terms of energy savings, but are more expensive so are competitive only in particularly sunny areas where auxiliary fuel use is low. We also find that the manner in which the technology competition within the model is structured makes a significant difference in model results. These details will be examined further in the next phases of this research.

![Hot Water Output](image)

*Figure 4 – Residential hot water technology share in a reference case scenario.*

### 3.5 Fraction of Regional Demand Potentially Met by SHW

The final necessary data element needed is an estimate of the fraction of the total hot water demand that can potentially be met by SHW. This sets an upper limit on the amount of SHW penetration. All domestic hot water demand in a region that is not considered excluded by the above considerations can potentially be supplied by SHW systems. No detailed studies on rooftop availability for SHW systems have been conducted, and what analysis has been done is focused on PV systems. Further, the little information that does exist is on the basis of fraction of roof area available for PV, as opposed to fraction of households that have sufficient suitable roof area available for a SHW system, which occupy much less space than most rooftop PV systems and have
looser constraints in regard to shading. We consider the assumptions made here reasonable, but quite uncertain.

The ability to install a SHW system will depend on housing type, shading, and roof orientation. For housing type, we use population density as a surrogate variable as this is globally available at relatively high resolution. In order to map from housing type to population density we drew on the compilation of Campoli and MacLean (2007) to determine how housing density relates to rooftop availability for SHW systems. From this compilation we estimate that limits on rooftop availability begin at about 3 housing units per acre and that, by 50 housing units per acre, few opportunities exist for rooftop installations. At these higher densities multi-story units become more common and the amount of available rooftop space is relatively small compared to the number of units in a building. To convert from housing density to population density we assume the number of persons per household to decline from 2.8 to 2.0 as the housing unit density goes from 3 to 50 units per acre (Bennefield and Bonnette 2003). To convert from a neighborhood scale to landscape scale we assume 20% of the land is not occupied by residential buildings.

Rounding the result, we, therefore, assume that no residential rooftop area is available for SHW systems when population density is higher than 13,500 persons per km², that 100% of the residential rooftops are potentially available for population densities below 1,500 persons per km², with a linear interpolation in between these limits. The fraction of US population excluded due to high densities is 7%. The only regions with a substantial fraction of their population excluded are Japan and Korea, with 23% and 40% excluded, respectively.

The shading factor is calculated from global gridded data of potential forest cover (Ramankutty and Foley 1998) and roof shading assumptions. Drawing from Chaudhari et al. (2004), we assume that 65% of the residential buildings in areas that have natural forest cover have sufficient un-shaded rooftop space for SHW systems while we assume the shading by trees in other areas (with no native tree cover) is not extensive enough to prevent SHW system installation. Shading by other causes or other issues (roof shape, nearby buildings, etc.) is assumed to reduce potential installations by 10%.

Residential roof orientation is assumed accessible to solar water heating in 83% of homes (Chaudhari et al, 2004). Pitched roofs make up 92% of residential roofs while flat roofs make up 8%. Flat roofs are oriented in the correct direction 100% of the time. Pitched roofs are 75% gable ended with two pitched sides, and 25% hip roofs with four sides. Of the gable roofs, 75% are assumed to have one half of the roof facing the correct solar orientation, while hip roofs have four sides with one facing the optimum solar orientation. The combined roof type, population density, and shading factors result in an assumption that SHW systems can potentially be used by 40-70% of the US population, depending on region. The average value for the US is 60%. This is slightly higher than the assumptions in Denholm (2007), who derived a United States average value of 50%.
3.6 Calibration/Comparison with top-down calculation

For consistency, and to ensure an accurate comparison within the model framework, the results of the bottom-up calculations should be compared with the top-down calculations used to calibrate the model. Residential hot water consumption in the GCAM USA buildings model was calibrated using energy consumption data from RECS and stock average water heater efficiency (system efficiency, a.k.a. energy factor) derived from stock data used in the NEMS modeling system. The average installed stock system efficiency used for calibration was 54% for gas and 86% for electric hot water heaters. The top-down calculation resulted in a value for hot water service 40% smaller than the value calculated using an average household water draw of 243 L/day (SRCC/GAMA = 64 gallons/day), a hot water set temperature of 57.1 °C, a US population-weighted mains temperature of 13.4 °C, and 103,246,000 households.

Any number of biases and data uncertainties can contribute to this difference. It is possible that the RECS data underestimates hot water consumption. For calibration purposes, we propose to split the difference and assume that the actual hot water draw is lower than the SRCC value, but larger than that implied by the RECS data. This is consistent with some recent studies that indicate hot water usage in the 50 gal/day range (J. Burch pers com), comparable to the adjusted value we assume here.

If the stock average efficiency is underestimated this would contribute to this difference. However, 30% or more of US households report water heaters at least 10 years old (RECS 2005), so there is a limit to how high the average stock efficiency might be.

4 Rooftop Photovoltaic

Photovoltaic technologies are implemented in GCAM as described in Clarke et al. (2008). PV supply curves developed by NREL (Denholm and Margolis 2008) used data on solar irradiance and the distribution of buildings, and assumed a mix of orientations to produce a supply curve for distributed PV generation. This curve is used to represent rooftop PV in the United States and is assumed to shift over time as PV technology costs decline.

Effectively, a net metering assumption was assumed. Distributed PV was assumed to compete with grid-produced electricity at the meter, so that the price of distributed PV is compared to the delivered cost from the electric grid.

4.1 Extension to other world regions

For CCTP and other global analysis, a representation of distributed PV technologies is needed for other world regions. To produce a global estimate for distributed PV supply we used a simple procedure whereby the US supply curve was scaled to account for population distribution, solar resource, and family size. Ideally, regional estimates for rooftop area should be used, but these are not available.
To account for regional differences in solar irradiance, the population-weighted solar irradiance for each model region was estimated using NASA Surface meteorology and Solar Energy data. The entire US resource curve was scaled by the estimated value of total irradiance relative for each region relative to the US value calculated in the same manner. This takes into account regional differences in solar radiation levels.

The total solar resource was then adjusted to account for the total population in each region. We assume that the total distributed solar “resource” to be proportional to the population in each region with corrections for population density and household size. The solar resource curve calculated by Denholm and Margolis (2008) assumed 1) no PV installations in multi-story buildings due to a combination of limited rooftop area and other uses for rooftop space and 2) a smaller solar installation on attached homes (e.g. townhomes, etc.). In our extrapolation to other regions we used population density as a surrogate for explicit information on building types, assuming lower overall PV installations as population density increases. To correct for population density we determined the “effective population” of each region for purposes of scaling by summing population within each region with a population density cap of 1000 persons/km$^2$, and excluding areas with population densities greater than 2000 persons/km$^2$. Thus, we assume that PV installations will be proportional to population density until a population density of 1000 persons/km$^2$, at which point no further increase is assumed to occur. Areas with population densities greater than 2000 persons/km$^2$ are assumed to be primarily high-rise buildings with limited rooftop area available for PV installations. The calculation was conducted at a 5 minute resolution using the Gridded Population of the World version 3 (CIESIN 2005).

The final adjustment was for household size. Regional with a higher number of persons per household were assumed to have more persons per dwelling and, therefore, would have a lower per-capita availability of rooftop space for PV installations. The PV resource curve was, therefore, multiplied by the ratio of household size relative to the US for each region. Formally, there is nothing in this analysis that limits distributed PV installations to rooftops. It is conceivable that much of the distributed PV installed could be located nearby, but not on top, of dwellings or other structures. In residential areas, however, there may be significant limits to the amount of space that residents may wish to devote to PV installations. Average regional household sizes were determined.

The resulting maximum distributed solar PV resource for each region is given below. The adjustments shown are cumulative from left to right, with the right-hand column being the final, adjusted total resource. Adjusting for average irradiance increases the available resource in sunny regions (e.g., Australia/NZ, Middle East, Africa) and decreases the resource in cloudy regions (FSU, Eastern Europe). Adjusting for the combination of population and population density dramatically changes the resource. Very large resources result in sunny regions with large populations such as China, Africa, and India. Scaling by household size reduces the total distributed PV resource for these regions.
To roughly account for increases in housing area over time, the PV resource is assumed to grow slightly as a function of GDP. While there is projected to be significant population growth in many of these regions, much of this growth, particularly in developing countries, will likely occur in dense urban areas, which would not necessarily result in large increases in distributed PV relative to the current estimated potential. A more rigorous accounting of rooftop PV availability would require a more detailed description of population changes over time, including rural, suburban, and urban population levels along with changes in household size and, ideally, floor space and building characteristics (multi-story, attached, high-rise, etc.).

**Total Distributed PV resource**

<table>
<thead>
<tr>
<th>Region</th>
<th>Scaled by average irradiance</th>
<th>Scaled using population density</th>
<th>Scaled by household size</th>
</tr>
</thead>
<tbody>
<tr>
<td>USA</td>
<td>2.7</td>
<td>2.7</td>
<td>2.7</td>
</tr>
<tr>
<td>Canada</td>
<td>2.2</td>
<td>0.2</td>
<td>0.2</td>
</tr>
<tr>
<td>Western Europe</td>
<td>2.3</td>
<td>3.6</td>
<td>3.0</td>
</tr>
<tr>
<td>Japan</td>
<td>2.5</td>
<td>0.7</td>
<td>0.6</td>
</tr>
<tr>
<td>Australia_NZ</td>
<td>3.2</td>
<td>0.3</td>
<td>0.2</td>
</tr>
<tr>
<td>Former Soviet Union</td>
<td>2.2</td>
<td>2.1</td>
<td>1.7</td>
</tr>
<tr>
<td>China</td>
<td>2.7</td>
<td>14.3</td>
<td>9.2</td>
</tr>
<tr>
<td>Middle East</td>
<td>3.6</td>
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<td>1.1</td>
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<td>Africa</td>
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<td>5.2</td>
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<tr>
<td>Latin America</td>
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<td>5.8</td>
<td>3.4</td>
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<td>Southeast Asia</td>
<td>3.3</td>
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</tr>
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<td>Eastern Europe</td>
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<td>Korea</td>
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</tr>
<tr>
<td>India</td>
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</tr>
</tbody>
</table>

*Table 1 – Total distributed (rooftop) PV resource assumed for 14 GCAM model regions in EJ of electricity generation.*

**Acknowledgements**

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5 Appendix — Mains Temperature

In order to estimate the energy needed for hot water heating, an estimate of the average temperature of water mains, or more precisely – the difference between ambient and mains temperature, is needed. In regions with abundant data, algorithms can be used to fit data to appropriate functional forms for detailed analysis of specific locations (Burch and Christensen 2007). Here we use a global assimilation data set to estimate mains temperature in all world regions as broad averages over one degree grid cells.

Ground temperature 2 meters deep is used as water mains temperature ($T_m$) (RETScreen, 2009). In this approximation the mains temperature depends on surface temperature with a sinusoidal lag term that depends on depth and soil thermal diffusivity. A minimum mains temperature of is $1^\circ$ C is assumed.

Mains temperature at every grid point is estimated drawing from Hillel (1982) as:

$$T_m = T_s + A_0 e^{-z/d} \sin \left[ \frac{2\pi(t-t_0)}{s} - \frac{z}{d} \right]$$

Where,

- $T_m = $ mains temperature
- $t = $ day of year
- $d = $ dampening depth
- $t_0 = 15; $ time lag from arbitrary starting date of January 1 to day of minimum temperature
- $z = $ depth (m);
- $A_0 = $ annual temperature amplitude
- $T_s = $ average annual earth skin temperature.

$T_s$ is the average annual earth skin temperature from NASA Surface meteorology and Solar Energy Global Data, $t$ is the day of year, $t_0$ is the time lag from an arbitrary start date which is January first until the day with the minimum temperature of the year. The annual temperature amplitude is also from NASA Surface meteorology and Solar Energy Global Data.

We evaluate the above function for the median day of each season using the following assumptions:

- $(t_0 = 15)$ January 15 is used as the coldest day of the year (Burch, 2007).
- $t$ is calculated using the median day of each season.
  - Spring= day 90 (April 15)
  - Summer= day 181 (July 15)
  - Fall= day 273 (October 15)
The damping depth $d$ (m) is calculated as (Hillel, 1982)

$$d = \left( \frac{2D_h}{\omega} \right)^{1/2},$$

where $\omega = \frac{2\pi}{365}$, and $D_h$ is the thermal diffusivity taken as the average of four soil types listed below. Permafrost and rock soils are not included. The average soil thermal diffusivity found is 0.04235.

<table>
<thead>
<tr>
<th>Soil Type</th>
<th>Thermal Diffusivity ($D_h$) in $m^2/s$ (RetScreen, 2009)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heavy soil- damp (clay, compacted sand, loam)</td>
<td>6.45x10^{-7}</td>
</tr>
<tr>
<td>Heavy soil- dry (clay, compacted sand, loam)</td>
<td>5.16x10^{-7}</td>
</tr>
<tr>
<td>Light soil- damp (loose sand, silt)</td>
<td>5.16x10^{-7}</td>
</tr>
<tr>
<td>Light soil- dry (loose sand, silt)</td>
<td>2.84x10^{-7}</td>
</tr>
</tbody>
</table>
References


