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# Predictive Bias and Sensitivity in NRC Fuel Performance Codes

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# **ABSTRACT**

The latest versions of the fuel performance codes, FRAPCON-3 and FRAPTRAN were examined to ensure best estimate behavior of the codes and to ensure (to the extent possible that unintentional bias has been eliminated. Each individual model and type of code prediction was examined and compared to the data that was used to develop the model. In addition, a brief literature search was performed to determine if more recent data have become available since the original model development for model comparison. If new data were discovered, these data were compared to the models and code predictions in FRAPCON-3.3 and FRAPTRAN-1.3 in order to determine if the model is biased. Models or integral effect prediction found to be biased relative to the data were updated and corrected in the upcoming versions of the codes, FRAPCON-3.4 and FRAPTRAN 1.4. Areas where modeling may be lacking were noted for further model development. The details of the updated models are provided in this report.

Subsequently, a sensitivity study was performed on the steady-state code, FRAPCON-3.3 to determine the effects of uncertainty in model predictions, manufacturing parameters and power history on the code outputs of regulatory interest.

# **FOREWORD**

The purpose of this study was to re-examine the NRC fuel performance codes to ensure best estimate behavior of the codes and to ensure (to the extent possible) that unintentional bias has been eliminated. The tendency of these analytical tools to be (or to become) intrinsically conservative is understandable as the regulatory requirements themselves use conservatism to bound uncertainties.

As an example of this regulatory approach, the required and acceptable features of evaluation models used in the calculation of stored energy of the fuel include:

The steady-state temperature distribution and stored energy in the fuel before the hypothetical accident shall be calculated for the burn-up that yields the **highest** calculation cladding temperature (or, optionally, the **highest** calculated stored energy.)

10 CFR 50, Appendix K, Part (I)(A)(1)

Thus, there is a motive for analytical tools used in the regulatory audit vendor safety analyses to incorporate conservatisms in an intrinsic or automated fashion. However, this may not be consistent with the need to compare code predictions with experimentally-derived information, such as fuel centerline thermocouple data. This current study seeks to identify and remove such conservatisms from the code (as opposed to removing them from the regulation).

Further, in recognition of recent vendor efforts to combine uncertainties in fuel code input parameters, a sensitivity study was performed on the steady-state code, FRAPCON-3.3 to determine the effects of uncertainty in model predictions, manufacturing parameters, and power history on the code outputs of regulatory interest. This effort makes direct use of the first part of this study – the comparison of individual model or type of code prediction with the data that was used to develop that model. The results of these two complementary efforts both seek to improve the tools used by NRC in regulatory analysis.

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## **EXECUTIVE SUMMARY**

FRAPCON-3 (Lanning et al., 1997a, Lanning et al, 1997b, Berna et al., 1997, Lanning et al., 2005a) is the steady state fuel performance code maintained by Pacific Northwest National Laboratory (PNNL) for the United States Nuclear Regulatory Commission (USNRC). FRAPCON-3 predicts fuel rod performance in pressurized water reactors (PWRs) and boiling water reactors (BWRs) by modeling the material responses of both the fuel and the cladding under normal operating conditions and anticipated operational occurrences (AOOs) with a duration of several minutes or greater. FRAPTRAN (Cunningham et al., 2001a, Cunningham et al., 2001b) is the corresponding transient fuel performance code maintained by PNNL for the USNRC. FRAPTRAN predicts fuel rod performance in PWRs and BWRs by modeling the material responses of both the fuel and the cladding under fast transient and accident conditions.

Material properties modeled by FRAPCON-3 and FRAPTRAN include fuel thermal conductivity, fuel thermal expansion, cladding oxide thermal conductivity, cladding thermal conductivity, gas conductance, fission gas release, cladding corrosion, fuel swelling, creep of irradiated cladding, cladding yield strength, Young's modulus of cladding, cladding axial irradiation growth, and cladding thermal expansion. By modeling material properties, important fuel rod performance parameters, such as rod internal gas pressure, peak fuel centerline temperature, and cladding permanent (i.e. plastic) hoop strain, can be predicted up to high burnup levels (65 GWd/MTU).

It has been noted that the original fuel performance codes used by the USNRC, the predecessors of FRAPCON-3 and FRAPTRAN were intrinsically conservative. In fact, the current version of FRAPCON-3 continues to provide conservative options (although these options are no longer used or recommended by PNNL). Despite efforts to update the codes and the models over the past 15 years, the codes are still considered by some to be not just optionally but intrinsically conservative. In order to quantitatively determine if these codes are biased, the latest versions of FRAPCON-3 and FRAPTRAN were examined to determine if the individual material property models or code outputs are biased relative to the available data

Each material property model was examined and compared to the data that was used to develop the model. In addition, a brief literature search was performed to determine if more recent data has become available, since the original model development, to further validate each model. If new data were discovered, these data were compared to the models in FRAPCON-3.3 and FRAPTRAN 1.3 in order to determine if the model is biased relative to the data. In addition to examining each model individually, code predictions that are a combination of multiple model predictions such as fuel centerline temperature, and fission gas release were compared to data from rods where these parameters were measured to determine if these integral effect predictions are biased. Although several individual models were found to be biased, the overall integral predictions of FRAPCON-3.3 and FRAPTRAN 1.3 compare well with integral effects data.

For models or integral effect predictions that was found to be biased relative to the data, a new correlation was developed that provides a best-estimate fit to the available data. New correlations have been developed for cladding corrosion and hydrogen pickup, radial power profile for heavy water reactor conditions, radial power profile for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> fuel, fuel thermal expansion at high temperature, gas thermal conductivity at high temperature, and

cladding creep. These new correlations are discussed in this report and will be included in the upcoming versions of the codes, FRAPCON-3.4 and FRAPTRAN 1.4. Areas where modeling may be lacking were noted for further model development.

Fuel performance codes similar to FRAPCON-3 and FRAPTRAN are developed by the fuel vendors and are used to demonstrate safe performance of the fuel rods for each core reload analysis. The fuel vendors must demonstrate that uncertainty in model predictions, fabrication parameters and power history are accounted for in this analysis. In order to do this, fuel vendors have used methodologies where the uncertainty in key critical parameters are included and others that have little effect on the outputs of regulatory interest are not included.

In order to determine the effect of each key parameter on the outputs of regulatory interest, a sensitivity study was performed using FRAPCON-3 where each fabrication parameter, model, and power history parameter was individually biased to a high and low value to determine the sensitivity of the uncertainty in these parameters to the outputs of regulatory interest. The results of this study are summarized in this document. This report shows the sensitivity of selected model uncertainties, manufacturing uncertainties, and power uncertainties on the code prediction of rod internal gas pressure, fuel centerline temperature, and cladding strain for sample BWR and PWR cases. It should be noted that the sensitivity to these parameters could change based on differences in power history or fuel rod design. The results from this study can be used to select parameters to vary in an analysis to determine upper bound output values from a statistical combination of uncertainties.

# ABBREVIATIONS

ASME American Society of Mechanical Engineers

AOO Anticipated Operational Occurrence

BOL Beginning of Life
BWR Boiling Water Reactor
CE Combustion Engineering

CHF Critical Heat Flux

CRUD Chalk River Unknown Deposit (generic term for various residues

deposited on fuel rod surfaces, originally coined by Atomic Energy of Canada, Ltd. (AECL) to describe deposits observed on fuel from

the test reactor at Chalk River.)

DNB Departure from Nucleate Boiling
EBWR Experimental Boiling Water Reactor
EPMA Electron Probe Micro-Analysis

FDI Fuel Duty Index
FGR Fission Gas Release
HTC Heat Transfer Correlation
HWR Heavy Water Reactor

ID Inner Diameter

INEL Idaho National Engineering Laboratory

LGHR Linear Heat Generation Rate LOCA Loss of Coolant Accident

MOX Mixed Oxide

NSRR Nuclear Safety Research Reactor

OECD Organization for Economic Co-operation and Development

OD Outer Diameter
PBF Power Burst Facility

PCMI Pellet/Cladding Mechanical Interaction

PIE Post Irradiation Examination

PNNL Pacific Northwest National Laboratory

PWR Pressurized Water Reactor
RIA Reactivity Initiated Accident
RXA Recrystallized Annealed
SNF Spent Nuclear Fuel

SPP Second Phase Precipitates
SRA Stress Relief Annealed
TD Theoretical Density

USNRC United States Nuclear Regulatory Commission

W Westinghouse

# 1.0 INTRODUCTION

FRAPCON-3 (Lanning et al., 1997a, Lanning et al, 1997b, Berna et al., 1997, Lanning et al., 2005a) is the steady state fuel performance code maintained by Pacific Northwest National Laboratory (PNNL) for the United States Nuclear Regulatory Commission (USNRC). FRAPCON-3 predicts fuel rod performance in pressurized water reactors (PWRs) and boiling water reactors (BWRs) by modeling the material responses of both the fuel and the cladding under normal operating conditions and anticipated operational occurrences (AOOs) with a duration of several minutes or greater. FRAPTRAN (Cunningham et al., 2001a, Cunningham et al., 2001b) is the corresponding transient fuel performance code maintained by PNNL for the USNRC. FRAPTRAN predicts fuel rod performance in PWRs and BWRs by modeling the material responses of both the fuel and the cladding under fast transient and accident conditions.

Material properties modeled by FRAPCON-3 and FRAPTRAN include fuel thermal conductivity, fuel thermal expansion, cladding oxide thermal conductivity, cladding thermal conductivity, gas conductance, fission gas release, cladding corrosion, fuel swelling, creep of irradiated cladding, cladding yield strength, Young's modulus of cladding, cladding axial irradiation growth, and cladding thermal expansion. By modeling material properties, important fuel rod performance parameters, such as rod internal gas pressure, peak fuel centerline temperature, and cladding permanent (i.e. plastic) hoop strain, can be predicted up to high burnup levels (65 GWd/MTU).

It has been noted that the original fuel performance codes used by the USNRC, the predecessors of FRAPCON-3 and FRAPTRAN were intrinsically conservative. In fact, the current version of FRAPCON-3 continues to provide conservative options (although these options are no longer used or recommended by PNNL). Despite efforts to update the codes and the models over the past 15 years, the codes are still considered by some to be not just optionally but intrinsically conservative. In order to quantitatively determine if these codes are biased, the latest versions of FRAPCON-3 and FRAPTRAN were examined to determine if the individual material property models or code outputs are biased relative to the available data.

This document describes the work that was done to evaluate the USNRC fuel performance codes FRAPCON-3.3 (Lanning et al., 1997a, Lanning et al., 1997b, Berna et al., 1997, Lanning et al., 2005a) and FRAPTRAN 1.3 (Cunningham et al., 2001a, Cunningham et al., 2001b) for any predictive bias and to determine the sensitivity of model, manufacturing, and power history uncertainties on predictions of fuel centerline temperature, cladding strain, and rod internal pressure. The intent of this report is <u>not</u> to ensure the conservatism in predicted fuel behavior. The intent is to ensure best-estimate behavior of the codes and to ensure (to the extent possible) that unintentional bias has been eliminated.

Section 2.0 provides the results of the bias study. In this section, each individual material property model is compared to the data that was used to develop the model as well as new data that has become available since the original model development. In addition, code predictions that rely on the integral effects of multiple material property models, such as fission gas release and fuel centerline temperature, are compared to data that have been taken from fuel rods where these properties were measured.

For individual material properties or code predictions that were found to be biased or otherwise in error, a new correlation was developed to provide a best estimate fit to the data that had been used in the original model development and the new data that was available. Section 3.0 describes the

new models that have been developed as a result of this study. For each new model, a detailed description is provided as well as a plot showing its comparison to data. Each of these models will be included in the upcoming versions of the codes, FRAPCON-3.4 and FRAPTRAN 1.4. Areas where modeling may be lacking were noted for further model development.

Section 4.0 provides the result of the sensitivity study that was performed using FRAPCON-3.3. This study documents the effect of uncertainty in various models, manufacturing parameters, and power histories on the code predictions of rod internal pressure, centerline temperature, and cladding hoop strain.

Overall conclusions from these studies are given in Section 5.0. References are given in Section 6.0.

# 2.0 BIAS ASSESSMENT

The latest code versions, FRAPCON-3.3 and FRAPTRAN 1.3, were examined to determine if the codes are intrinsically conservative. Each model was examined and compared to the data that were used to develop the model. In addition, a brief literature search was performed to determine if more recent data has become available, after release of the three code versions, to compare to each model. If new data were discovered, these data were compared to the models in FRAPCON-3.3 and FRAPTRAN-1.3 in order to determine if the model is biased relative to the data. This section will not validate the current models, as this work has already been performed (Lanning et al, 1997a, Lanning et al, 1997b, Lanning et al, 2005a, Cunningham et al, 2001b). Rather this section will just examine the models and integral effect predictions to determine if they are biased relative to the data.

Most of the material properties used in these come from the library of nuclear material properties found in MATPRO (Hagrman et al., 1981). Some of these properties have been updated in FRAPCON-3.3 and FRATPRAN 1.3 as a result of new data at higher burnup becoming available.

The result of this study is a list given in section 2.8 of models in FRAPCON-3.3 and FRAPTRAN 1.3 that are considered to be best-estimate relative to the most up-to-date data and a list of models that are biased relative to the data. In addition, the integral effects calculations such as temperature and cladding strain are compared to data to determine if these predictions are biased. Models or integral effect predictions found to be biased relative to the data will be updated and corrected in the upcoming versions of the codes, FRAPCON-3.4 and FRAPTRAN 1.4. Areas where modeling may be lacking were noted for further model development.

# 2.1 Thermal Modeling and Assessment

This section describes the thermal modeling in FRAPCON-3.3 and FRAPTRAN-1.3. Section 2.1.1 describes the code solution method. Sections 2.1.2-2.1.6 describe the property models that are used in determining the temperature distribution radially from the cladding outer surface to the fuel center. Section 2.1.7 describes the assessment of the code predictions to measured temperature data from instrumented fuel rods.

# 2.1.1 Code Solution Method, Fuel Rod Heat Transfer Solution Methods and Pellet Heat Generation Radial Profile

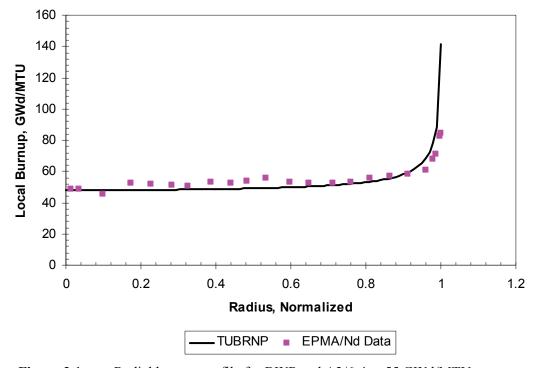
The FRAPCON-3.3 and FRAPTRAN-1.3 codes iteratively calculate the interrelated effects of fuel and cladding temperature, rod internal gas pressure, fuel and cladding deformation, release of fission product gases, fuel swelling and densification, cladding thermal expansion and the irradiation-induced growth, cladding corrosion, and CRUD (Chalk River Unknown Deposit) deposition as functions of time and fuel rod specific power. The solution methods are described in detail in Berna et al. (1997) and Cunningham et al. (2001a).

For both codes, the models assume a cylindrical fuel pellet located symmetrically within a cylindrical fuel rod cladding surrounded by coolant. The local linear heat generation rate is used to calculate the coolant bulk temperature. Using this temperature as a boundary condition, FRAPCON-3.3 uses a one-dimensional (1-D) steady-state solution method to determine the temperature distribution in the cladding, gap, and fuel from the outside in, while FRAPTRAN-1.3 uses a 1-D transient solution method to determine the temperature distribution in the cladding, gap, and fuel from the outside in.

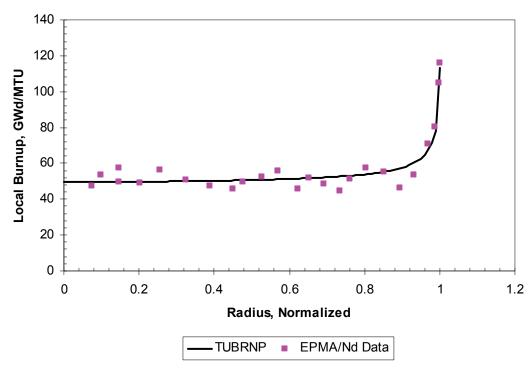
FRAPCON-3.3 uses the TUBRNP subcode (Lassman et al., 1994) to calculate the radial power profile as a function of U-235 enrichment and burnup. FRAPCON is also capable of calculating radial power profiles for mixed oxide (MOX) fuel as a function of plutonium isotope concentration and burnup. FRAPCON-3.3 has the capability of calculating a radial power profile for fuel in a heavy water reactor (HWR), but it does not appear to give adequate predictions of these radial power profiles. FRAPCON-3.3 does not have the capability to model the radial power profile for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> fuel. The capability to model fuel in HWR conditions and to model UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> will be added to the upcoming version of FRAPCON-3 and is described in Section 3.

Because the radial power profile is burnup dependent, FRAPTRAN-1.3 does not have a radial power profile model, but rather has an option for user input of radial power profile or for initialization from FRAPCON-3.3. Since FRAPTRAN-1.3 models events that take place over a very short period of time (<10 min), there will be minimal burnup accumulation so it is acceptable to use the same radial power profile throughout the duration of the event. For an event that occurs after some period of irradiation, the base irradiation is modeled in FRAPCON-3, and the burnup dependent information including the radial burnup profile is passed to FRAPTRAN for the calculation of the fast transient event. It is acknowledged that for a fast transient such as a reactivity initiated accident (RIA) the radial power profile in the fuel rod closest to the control rod will be somewhat asymmetric. However, in a two-dimensional code (axial and radial) such as FRAPTRAN, it is acceptable to use the same radial power profile calculated for steady-state. The overall shape will not significantly change during the transient.

The burnup profiles calculated by TUBRNP are compared to radial burnup measurements made by electron probe microanalysis (EPMA) of the non-mobile fission product, Nd, at various burnup levels for BWR and PWR rods. These comparisons are reported in Lanning et al. (1997a) and can be seen in Figures 2.1 through 2.5. There have been no comparisons made to HWR rods such as those from the Halden reactor.



**Figure 2.1** Radial burnup profile for BWR rod A3/6-4 at 55 GWd/MTU



**Figure 2.2** Radial burnup profile for BWR rod H8/36-4 at 55 GWd/MTU

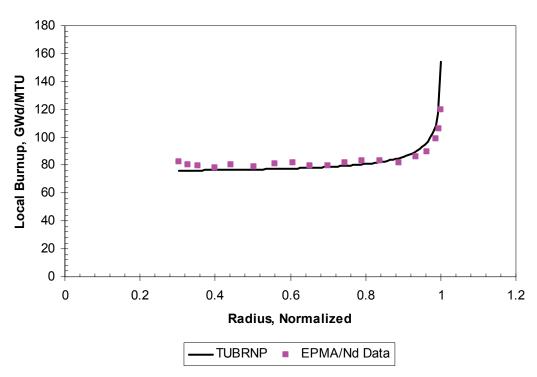


Figure 2.3 Radial burnup profile for PWR rod BK365 at 83 GWd/MTU

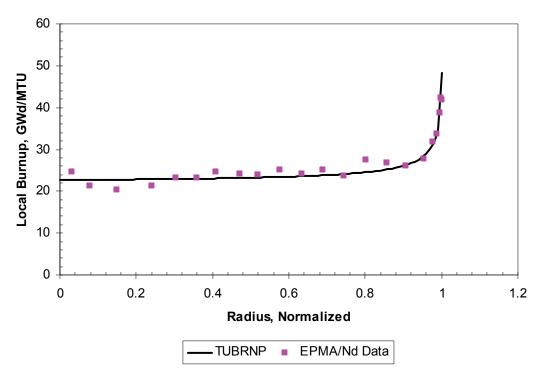
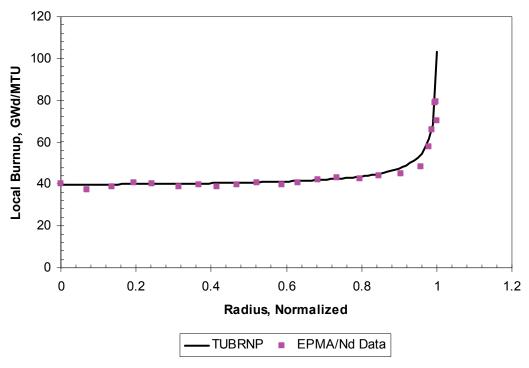


Figure 2.4 Radial burnup profile for PWR rod D200 at 25 GWd/MTU



**Figure 2.5** Radial burnup profile for PWR rod D226 at 45 GWd/MTU

These comparisons demonstrate that the TUBRNP model in FRAPCON-3.3 predicts the EPMA data well. It appears that the TUBRNP model may overpredict the edge burnup. The reason for this is because the actual power profile is very edge peaked, but the EPMA data does not always

capture this on the very edge of the pellet. This is demonstrated by examining the data in Figures 2.1 and 2.2 where for BWR rods with the same burnup, significantly different edge peaking can be seen. It can be concluded that the radial power profile model predicts radial power and burnup well within the accuracy of the data.

## 2.1.2 Fuel Thermal Conductivity

The FRAPCON-3.3 and FRAPTRAN-1.3 codes have two fuel thermal conductivity models. One model is for urania ( $UO_2$ ) and the other model is for mixed-oxide fuel (MOX). In addition, each model has the same correction for gadolinia ( $Gd_2O_3$ ) additions. Section 2.1.2.1 describes the assessment of the  $UO_2$  model. Section 2.1.2.2 describes the assessment of the MOX model. Section 2.1.2.3 describes the assessment of the correction for  $Gd_2O_3$  additions.

### $2.1.2.1 \quad UO_2$

The UO<sub>2</sub> thermal conductivity model is the same in both FRAPCON-3.3 and FRAPTRAN-1.3. This model is described in Lanning et al. (2005a). This model is a function of burnup and temperature. Unirradiated (Ronchi, 1999, Lucuta, 1996, Christensen et al., 1964, Godfrey et al., 1094, Bates, 1970, Gibby, 1971, Weilbacker, 1972, Goldsmith and Douglas, 1973, and Hobson et al., 1974) and irradiated (Carrol, 1994, Ronchi, 2004) data was collected to compare to model predictions. Figures 2.6 and 2.7 show the predicted minus measured values for thermal conductivity for unirradiated and irradiated disks, respectively. It can be seen from these figures that the model provides a best-estimate calculation of UO<sub>2</sub> thermal conductivity. There is a slight code underprediction for thermal conductivity values greater than 5 W/m-K. These values are measured at and around room temperature and will not impact fuel temperature calculations at normal reactor conditions. The UO<sub>2</sub> model is acceptable based on good comparison to thermal conductivity data and measured centerline temperatures.

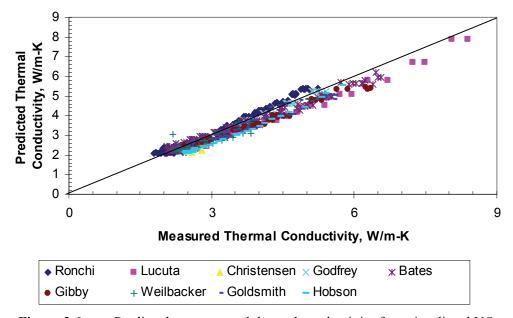


Figure 2.6 Predicted vs. measured thermal conductivity for unirradiated UO<sub>2</sub>.

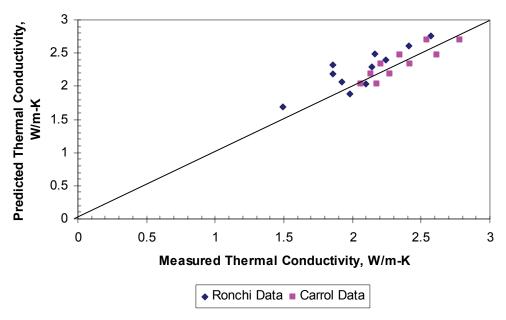


Figure 2.7 Predicted vs. measured thermal conductivity for irradiated UO<sub>2</sub>.

## 2.1.2.2 MOX

The MOX thermal conductivity model in FRAPCON-3.3 is described in Lanning et al (2005a). This model is a function of burnup, oxygen to metal ratio and temperature. Lanning et al. (2005a) provides no model to data comparisons. A literature search was performed and several sources of unirradiated MOX thermal conductivity were found (Duriez, 2000, Philipponneau, 1992). Figure 2.8 shows the predicted vs. measured values for thermal conductivity for unirradiated disks. It can be seen from this figure that the current MOX model provides a best-estimate prediction of MOX thermal conductivity. No data was found on irradiated MOX, but the burnup dependence in this model is the same as the burnup dependence in the  $\rm UO_2$  model and is judged to be acceptable based on comparisons to fuel temperatures measured in-reactor as a function of burnup.

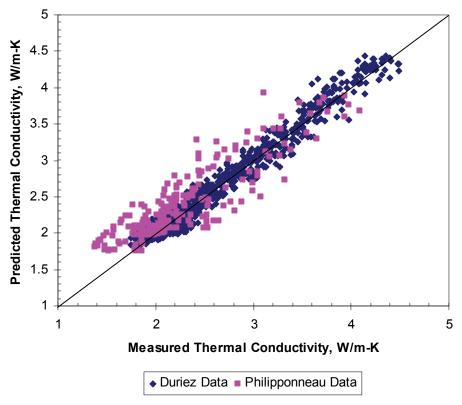


Figure 2.8 Predicted vs. measured thermal conductivity for MOX fuel

### 2.1.2.3 $UO_2$ - $Gd_2O_3$

The Massih adjustment (Massih, 1992) for thermal conductivity of UO<sub>2</sub> – Gd<sub>2</sub>O<sub>3</sub> fuel is used in FRAPCON-3.3 as described in Lanning et al. (2005a). No adjustment for thermal conductivity of UO<sub>2</sub> – Gd<sub>2</sub>O<sub>3</sub> fuel is used in FRAPTRAN-1.3, but this will be added in FRAPTRAN-1.4 to be consistent with FRAPCON-3.4. There was no assessment of this model adjustment in Lanning (2005a), however, recently, a database of gadolinia thermal conductivity measurements has been collected on irradiated (Minato, 2001, Amaya, 1997, Newman, 1982, and Hirai, 1991) and unirradiated disks (Minato, 2001, Amaya, 2002). Based on good comparisons to these data and centerline temperature data from Halden tests on gadolinia rods, it was determined that the Massih adjustment is acceptable. Figures 2.9 and 2.10 show the predicted vs. measured values for thermal conductivity for unirradiated and irradiated disks, respectively. It should be noted that thermal conductivity measurements on irradiated disks are only valid at the irradiation temperature (Beyer, 1998) and this is why there is significantly less data for irradiated disks than unirradiated disks. The largest overprediction shown in Figure 2.9 is for samples measured at room temperature. This overprediction will not affect the in-reactor temperature predictions (For temperature greater than 400°C, thermal conductivity is less than 3.5 W/m-K). Comparisons to temperature measurements will be shown in Section 2.1.7.

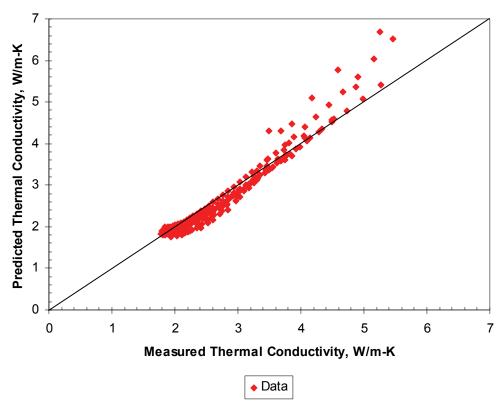


Figure 2.9 Predicted vs. measured thermal conductivity for unirradiated UO<sub>2</sub> Gd<sub>2</sub>O<sub>3</sub>.

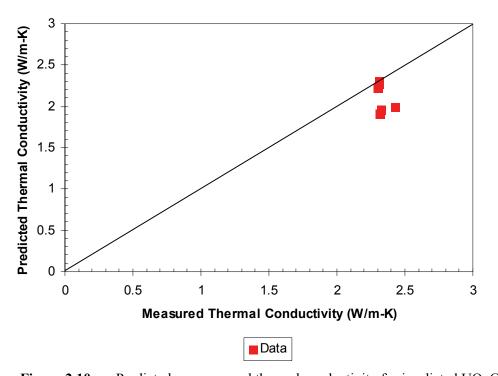


Figure 2.10 Predicted vs. measured thermal conductivity for irradiated UO<sub>2</sub> Gd<sub>2</sub>O<sub>3</sub>.

## 2.1.3 Gap Conductance

The gap conductance model in FRAPCON-3.3 and FRAPTRAN-1.3 is based upon the assumption of a symmetric radial gap between the fuel pellet and the cladding, which has finite size even when strong pellet-cladding mechanical interaction ("hard contact") occurs due to surface roughness effects. Effects of pellet eccentricity upon effective gap conductance are deemed to be overshadowed by the effects of pellet cracking and fragment outward relocation, which for any normal irradiation will occur upon the first rise to full power (see Section 2.1.5).

Hence, three parallel paths of heat conduction are envisioned across the pellet-cladding gap:

- a. Conduction (bulk diffusion) through the gas (modified by thermal accommodation at the bounding surfaces, in the Knudsen regime).
- b. Conduction through points of contact (when pellet-cladding contact has occurred).
- c. Radiation heat transfer (for pellet outer surface temperatures during normal operation, this is a minor contribution).

These three paths will be discussed in the sections below.

#### 2.1.3.1 Conductance through the Gas

The conductivity of the pure gases and gas mixtures encountered in fuel rods is described in Section 2.1.6.5. This includes the mixing rules for calculating mixed-gas conductivity and conductivity of fill gas (normally helium) that has become significantly diluted by released fission gases. The conductance contribution from this pathway is described by Berna et al. (1997).

The physical gap separation is calculated from the as-fabricated input gap size, modified by fuel and cladding displacements due to thermal expansion, fuel relocation, fuel densification and swelling, and cladding creep. Fuel creep in the FRAPCON-3.3 and FRAPTRAN-1.3 codes is not calculated, as it is not a large source of pellet outer surface displacement during normal operation. This assumption of a "rigid pellet" is discussed in greater detail in Section 2.5.

The "temperature jump distance" is an increment added to the physical gap separation to account for imperfect thermal accommodation (i.e., energy transfer) of the gas molecules impinging on the bounding surfaces of the gap. That is, the gas molecule kinetic energy is incompletely transferred to thermal energy in the cladding, and the thermal energy of the atoms on the fuel pellet surface is incompletely transferred to the gas molecules in the gap. Both of these incomplete energy transfers result in higher fuel temperatures, and they are represented by "accommodation coefficients" (with values of <1.0) for both surfaces. The relationship between temperature jump distance and accommodation coefficient is described by Berna et al. (1997).

The development of this model, and its selection from among other possibilities, is explained in (Lanning, 1975). Both ex-reactor gap conductance experiments at PNNL (Garnier and Begej, 1979a, Garnier and Begej, 1979b) and in-reactor experiments at Halden Reactor Project in Norway (Miller, 1980) have confirmed the magnitude of the jump distance that is calculated by FRAPCON-3.3.

It should be noted that, for modern PWR and even BWR fuel rods, the pressurization of the helium fill gas leads to in-reactor rod internal pressures that make absolute values of temperature jump distance very insignificant relative to the total gap size. This is even true when the gap has

closed because the temperature jump distances are still small relative to the combined fuel pellet and cladding surface roughnesses.

It should further be noted that, when pellet-cladding contact first occurs, the gap size reduces to the sum of the roughness values. However, as hard contact occurs, this gap size is further reduced slightly as a function of the interface pressure. This is explained in (Lanning et al., 1997a).

#### 2.1.3.2 Conductance through points of cladding-pellet contact

When the net fuel pellet and cladding deformations result in pellet-cladding contact and mechanical interaction, direct solid-to-solid heat transfer will occur across the roughness asperity points where, on a microscopic level, contact is actually occurring. Initially, the contact pressure is very small, because the cracked and relocated pellet fragments will be partially pushed back into place by the ongoing differential displacements of fuel and cladding (so-called "soft contact"). In FRAPCON-3.3, this period of soft contact is assigned zero interfacial pressure, and hence no credit is taken for solid-solid contact conductance. When 50% of the fuel pellet outward relocation is consumed by differential deformations, the mechanical model is permitted to calculate interfacial pressure from the increasing differential displacements, and the solid-solid contact conductance is calculated as a function of interface pressure and cladding and fuel conditions. This model is described by Berna et al. (1997).

In FRAPTRAN-1.3 as opposed to FRAPCON-3.3, the relocation is not allowed to recover due to the rapid nature of transients and the pellet-cladding contact conduction described above is used immediately upon gap closure.

#### 2.1.3.3 Radiation heat transfer

Due to the high axial aspect ratio for the fuel-to-cladding gap, the radiation heat transfer from the fuel pellet surface to the cladding is calculated assuming the fuel and cladding are infinite concentric cylinders, gray body derived by Kreith (1964). This model is described by Berna et al. (1997).

This model appears to provide an adequate approximation of the radiation heat transfer between the two bodies. Typically, this pathway constitutes a very small fraction of the total conductance.

## 2.1.4 Fuel Thermal Expansion

The fuel thermal expansion model in both FRAPCON-3.3 and FRAPTRAN-1.3 is the FTHEXP model documented in MATPRO 11, Rev. 2 (Hagrman et al. 1981). The actual coding in terms of comments and formatting varies somewhat, however the effective coding is the same.

The model is based on both measurements of the lattice constant by x-ray diffraction, which were applied for model development at temperatures below 800K only, and data from bulk thermal expansion measurements. The same model form is used for both UO<sub>2</sub> and PuO<sub>2</sub> fuels, with the constants changed depending on the fuel type. Fuel thermal expansion for mixed oxide is determined based on weight fraction.

The model in FRAPCON-3.3 and FRAPTRAN-1.3 was compared to data provided in the original MATPRO reference (Grønvold, 1955, Baldock et al., 1966, Christensen, 1963, Kempter and Elliott, 1959, Burdick and Parker, 1956, and Tokar and Nutt, 1972). In, addition, a literature search was performed to find any further thermal expansion data since the publication of the MATPRO model. This search yielded a review of thermal expansion data by Martin (1988) and

Momin et al (1991) and a model that fits the data well. In addition, two other sources (Fink, 2000b and Carbajo, 2001) recommend the Martin model. The data used in the development of the MATPRO model and the Martin model are shown in Figure 2.11. It can be seen from this figure that the MATPRO model and the Martin model are highly similar up to 2200K. Beyond this, the MATRPO model provides lower thermal expansion than the Martin model.

Based on the latest thermal expansion data, the thermal expansion model in FRAPCON-3.3 and FRAPTRAN-1.3 may underpredict fuel thermal expansion above 2200K. The magnitude of under prediction could be as high as 10% by 3000K.

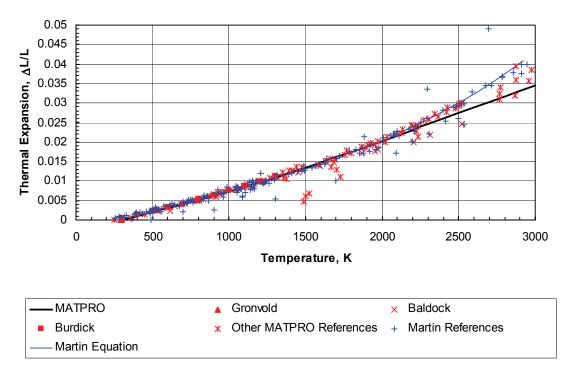


Figure 2.11 Thermal expansion data and model predictions for UO<sub>2</sub>

The impact of underpredicting the fuel thermal expansion for temperatures greater than 2200K is as follows.

- less radial/axial thermal expansion for temperatures greater than 2200K
- less gap closure at higher temperature
- less cladding strain at higher temperature
- less increase in gas pressure at higher temperature

Based on these data comparisons it is concluded that the fuel thermal expansion model in FRAPCON-3.3 and FRAPTRAN-1.3 provides a best estimate prediction for fuel thermal expansion up to 2200K. Beyond this temperature, the model may underpredict fuel thermal expansion. This model will be updated in both FRAPCON-3.4 and FRAPTRAN 1.4 as described in Section 3.4.

#### 2.1.5 Fuel Relocation

When fresh fuel rods first rise to operating power level, the pellets begin to crack radially, due to the thermal hoop stresses generated by the temperature gradient from center to surface and the differential thermal expansion of central region material compared to peripheral region material. A full diametral crack has been observed to develop at linear heat generation rates (LHGRs) as low as 3 kW/ft (Lanning and Cunningham, 1981). Higher LHGR levels typically experienced at beginning of cycle result in multiple radial cracks. The resulting roughly pie-shaped pellet fragments quickly relocate outwards toward the cladding, due to thermal ratcheting (increasing and decreasing temperature rearranging pellet fragments). This results in significant gap closure and reduction in the effective thermal gap, and hence increase in the gap conductance.

A best-estimate pellet relocation model was developed for GAPCON-THERMAL-2 Rev. 2 (GT2R2) (Beyer and Cunningham, 1984) and was recommended for use in FRAPCON-3 in conjunction with the FRACAS-1 mechanical model. This GT2R2 model is a function of LHGR and burnup. The gap closure due to relocation as a fraction of the as-fabricated pellet-cladding gap is given for FRAPCON-3.3 by Lanning et al. (1997a).

This relocation model is not applied in FRAPTRAN-1.3 because relocation has a small burnup dependence and there is no significant burnup accumulation over the time periods of the events that are modeled in FRAPTRAN-1.3. However, FRAPTRAN-1.3 does assume some initial relocation prior to the start of a transient based on the FRAPCON-3.3 model (Cunningham et al., 2001a). For fresh fuel, the relocation is assumed to be 30% of the gap size. For irradiated fuel, the relocation is assumed to be 45% of the gap size. If FRAPCON-3.3 is used to initialize a FRAPTRAN-1.3 evaluation, then the relocation calculated by FRAPCON-3.3 is used.

The assumption is made in FRAPCON-3.3 that 50% of the relocation displacement must be consumed by differential pellet-cladding displacements, before "hard" contact (pellet-cladding mechanical interaction) occurs. This is derived from beginning-of-life (BOL) measurements of the onset of cladding axial elongation, and from Halden squeeze tests that show approximately half the assigned relocation must be taken up before fuel pellet compliance changes back towards that of a solid pellet. In FRAPTRAN-1.3, no recovery of the relocation is allowed due to the rapid nature of transients and "hard" contact is assumed to occur as soon as the fuel and cladding come into contact.

Fuel pellet center temperatures measured at BOL in instrumented test rods have repeatedly been found to be lower than values predicted assuming that the as-fabricated fuel-cladding gap size is reduced solely by differential fuel and cladding thermal expansion (Lanning, 1981; Kjaerheim and Rolstad, 1967). It has long been concluded, on the basis of microscopic examination of fuel cross sections (Galbraith, 1973, and Dutt, et al., 1974), that fuel pellet cracking promotes an outward relocation of the pellet fragments that causes additional gap closure, and hence increases the gap conductance and lowers the fuel temperatures. This process begins at beginning-of-life (BOL) and quickly reaches equilibrium. Oguma (1983) characterized this approach to equilibrium based on his analysis of BOL test fuel rod elongation data from Halden instrumented test assemblies.

In a series of tests in the PBF reactor at Idaho National Engineering Laboratory (INEL) (Garner, 1978), titled the Gap Conductance (GC) series, GC-1,2, and 3, test rods of varying gap size and fill gas compositions were instrumented with both centerline thermocouples and multiple coplanar off-center thermocouples, in an attempt to quantify this transfer of thermal resistance from gap to fuel. The results indicated a major effect; according to INEL's analysis, the BOL gap size is reduced to much less than 50% of its unrelocated value on average. However, this does not agree with the extensive Halden data at BOL that suggests that the relocated gap size is approximately 50% of the un-relocated value.

"Soft" pellet cladding mechanical interaction (PCMI) occurs when the cracked (and highly deformable) pellet interacts mechanically with the cladding, producing fuel-cladding contact and limited enhanced axial rod elongation, but not the steep elongation vs. LHGR and bamboo ridging associated with "hard" PCMI. A rod displaying soft PCMI in operation also displays pellet deformability in rod radial compression tests. The occurrence of "soft" PCMI is consistent with the results of several experiments in the Halden Reactor, including NRC-sponsored tests, in which fuel temperature and rod elongation were simultaneously measured as a function of burnup and LHGR (Williford, 1980).

Verification of the resulting gap closure functions have been done primarily with instrumented fuel tests in which fill gasses have been alternated at constant LHGR between helium and argon, and the change in pellet center temperature noted. These are indirect verifications of gap size, but they do have the advantage of yielding an "effective thermal gap" under varying conditions of LHGR level and burnup, which is the essential parameter that a fuel performance code needs to perform fuel temperature calculations.

Figure 2.12 shows the temperature changes that occurred in a  $UO_2$  rod from IFA-633 near BOL when the helium fill gas was exchanged for argon fill gas at LHGRs steps up to 17 kW/m (Wright, 2004). The close agreement between predicted temperature change by FRAPCON-3.3 and that measured is qualitative verification that, for this open-gap situation, the thermal gap is closely predicted by the current relocation model.

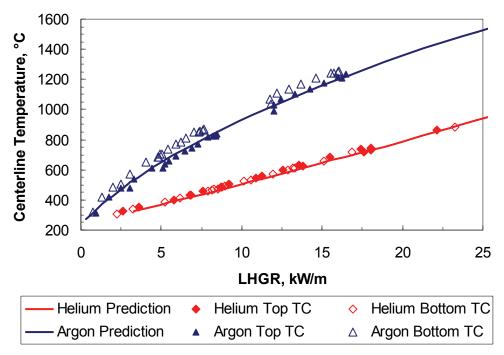


Figure 2.12 Predicted and measured fuel centerline temperatures with argon and helium fill gases for a IFA-633 UO<sub>2</sub> rod (as-fabricated radial gap is 105μm)

# 2.1.6 Other Models and Properties

This section will describe the following models and properties and provide data comparisons for each one.

Clad-coolant heat transfer

- Oxide thermal conductivity
- CRUD thermal conductivity
- Cladding thermal conductivity
- Gas conductance
- Cladding thermal expansion

The following subsections provide an assessment of each of these models

#### 2.1.6.1 Cladding-Coolant Heat Transfer

The coolant bulk temperature in FRAPCON-3.3 is calculated for each axial node assuming a single, closed coolant channel as described in Berna (1997). The calculation of the fuel rod surface temperature is performed assuming forced convection and/or nucleate boiling depending on the conditions. The model selection and a description of each model are described in Berna (1997).

In FRAPTRAN-1.3 there are several ways for the user to specify the coolant conditions. The first is for the user to specify the coolant temperature, pressure, and surface heat transfer coefficient. In this case, the code uses these values to calculate the cladding surface temperature using the coolant temperature. The second is for the user to specify the coolant as water and specify the enthalpy, pressure, mass flux, and select a heat transfer correlation (HTC) and critical heat flux (CHF) correlation. The HTC and CHF correlations have been updated in FRAPTRAN 1.4. User guidelines will be provided for selecting the appropriate correlations. Work has been performed to assess the correlations and demonstrate that these correlations provide best-estimate predictions of cladding surface temperature over a wide range of coolant conditions (Cuta, 2007).

It is concluded that the clad-coolant heat transfer models in FRAPCON-3.3 are acceptable and provide best-estimate values of cladding surface temperature based on good comparisons to fuel centerline temperature and general acceptance of the correlations used. The correlations used in FRAPTRAN-1.3 were satisfactory 25 years ago, but based on new data and information, they needed to be updated. The new correlations have been added to FRAPTRAN-1.4 and provide a best-estimate prediction of cladding surface temperature over a wide range of coolant conditions but are not documented in this report.

#### 2.1.6.2 Oxide Thermal Conductivity

The zirconium oxide (ZrO<sub>2</sub>) thermal conductivity model used in both FRAPCON-3.3 (Lanning et al., 2005a) and FRAPTRAN-1.3 (Cunningham et al., 2001a) is the ZOTCON model documented in MATPRO 11, Rev. 2 (Hagrman et al. 1981).

The model is based on the data of Kingery et al. (1954). Data from Maki (1973) and Lapshov and Bashkatov (1973) were reviewed during the development of the ZOTCON model, but not used in the model because it was concluded that those data were not applicable. The model is stated to be applicable for the temperature range 100-1400°C.

The MATPRO description provides data source references and a plot of the Kingery et al. data compared to the ZOTCON model. This data-model comparison is provided in Figure 2.13. The Kingery et al. reference used two sample types for data generation: a bulk ZrO<sub>2</sub> that was 100% dense and used for the model, and a sample that had approximately 13% porosity, but was not used for model development.

A search was performed for ZrO<sub>2</sub> thermal conductivity data published since the development of the ZOTCON model. The only openly-published source of oxide thermal conductivity versus temperature data that was found was Gilchrist (1979). Gilchrist measured the thermal conductivity of oxide grown on Zry-2 tubes rather than bulk ZrO<sub>2</sub>. The oxides were generated under different oxidation conditions and to different thicknesses.

Two room-temperature values of  $ZrO_2$  thermal conductivity were found. Accuractus.com (Accuractus, 2007) listed the thermal conductivity as 2 W/m-K for bulk  $Y_2O_3$  stabilized  $ZrO_2$ . Matweb.com (Matweb, 2007) listed the thermal conductivity as 1.675 W/m-K for material that was 100% dense.

A comparison of the MATPRO ZrO<sub>2</sub> thermal conductivity model to the Kingery et al. (1954) data is presented in Figure 2.13. There is an excellent model-data comparison for the 100% dense material. However, the model is approximately 20% high compared to the data from the porous ZrO<sub>2</sub>. This is important because the porous material, with the lower thermal conductivity is believed to be more representative of the actual oxide on cladding.

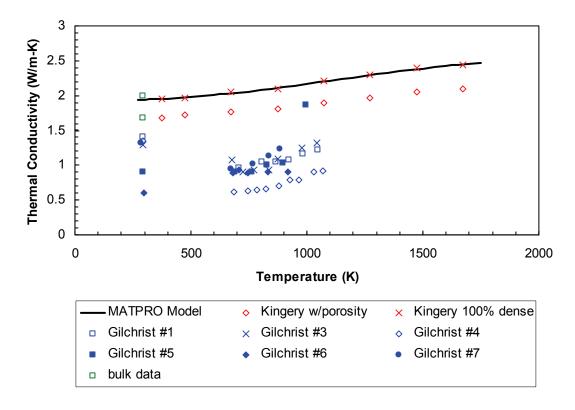
The ZrO<sub>2</sub> data by Gilchrist (1979) are also shown in Figure 2.13. The Gilchrist samples are oxide actually grown on Zry-2 tubes and are, therefore, more representative of the oxide observed inreactor. These data are considerably lower than the MATPRO model and the Kingery et al. porous data. This figure demonstrates that the model in FRAPCON and FRAPTRAN predicts 100% dense oxide well, but overpredicts less dense oxide that is seen in-reactor by approximately 100%.

The two room-temperature data points are also included in Figure 2.13 ("bulk data" points). These two data points are in general agreement with the MATPRO model and the data presented by Kingery et al. As with the Kingery et al. data, the oxide source is apparently high-density bulk oxide rather than porous oxide. High-density bulk oxide apparently has a higher thermal conductivity than porous oxide and does not appear to be an appropriate material for generating thermal conductivity data for the purpose of modeling fuel rod thermal performance.

The impact of overpredicting oxide thermal conductivity (i.e., overpredicting heat flow through the oxide) would be:

- underprediction of the temperature at the oxide-metal interface;
- underprediction of oxide growth because of underpredicting the oxide-metal interface temperature; and
- underprediction of the bulk cladding temperature, gap gas temperature, and fuel temperature.

It is recommended that the MATPRO ZrO<sub>2</sub> thermal conductivity model be further evaluated with an expectation of reducing the predicted thermal conductivity. An Organization for Economic Cooperation and Development (OECD) document (OECD 1995) from 1995 also concluded that "thermal conductivity of oxide needs further clarification." Based on the Gilchrist data, a simple "fix" might be to reduce the predicted oxide thermal conductivity by 50%. Debate on this issue is ongoing. The difference in centerline temperature that the cladding thermal conductivity model being biased high would have is only about 10°C.



**Figure 2.13** Comparison of MATPRO ZrO<sub>2</sub> model to data used to develop the model and newer data

### 2.1.6.3 CRUD Thermal Conductivity

CRUD is commonly defined as the deposition of oxidation products, formed in the primary coolant circuit, on the surface of the fuel rods. There are two types of CRUD that accumulate, a light fluffy CRUD and a more tenacious CRUD. The light fluffy CRUD is mainly an iron oxide (hematite) and is usually not a significant barrier to heat flow. The tenacious CRUD can differ depending on if it is in a BWR or a PWR with the former being a zinc-iron oxide with nickel and the later consisting of a nickel ferrite oxide, but can also consist of other oxides or compounds. The tenacious CRUD deposition is important in fuel rod modeling from the standpoint of affecting the zirconium oxide/metal interface temperature, and thus the rate of formation of additional zirconium oxide (Cheng et al., 2000).

The CRUD thermal conductivity model used in FRAPCON-3.3 (Lanning et al., 2005a) is a constant value of 0.87 W/m-K (0.5 BTU/hr-ft-F).

The FRAPCON-3.3 documentation does not state where the CRUD thermal conductivity value originates. There is no CRUD thermal conductivity model used in FRAPTRAN-1.3 (Cunningham et al., 2001a) nor is there a CRUD thermal conductivity model defined in MATPRO 11, Rev. 2 (Hagrman et al. 1981).

A search was performed for published CRUD thermal conductivity data. There was very little information found. Leyse (2003) stated a value of 0.8 W/m-K for hydrated alumina in the Experimental Boiling Water Reactor (EBWR). This is close to the value used in FRAPCON-3.3.

The effects of an uncertain value for CRUD conductivity are mitigated by the fact that the growth of CRUD is reactor specific, and FRAPCON-3.3 does not have a CRUD growth model. Rather the user must either input a constant CRUD thickness or a rate of CRUD growth. Currently, no data in the open literature exists to verify a value used for the GRUD growth rate.

## 2.1.6.4 Cladding Thermal Conductivity

The cladding thermal conductivity model in both FRAPCON-3.3 (Lanning et al. 2005a) and FRAPTRAN-1.3 (Cunningham et al. 2001a) is the CTHCON model documented in MATPRO (Hagrman et al. 1981). FRAPTRAN-1.3 includes an optional cladding thermal conductivity model appropriate for Zr-1Nb type alloys such as ZIRLO that are not included in FRAPCON-3.3. This model was included at the request of the Russian Research Center, Kurchatov Institute (the Russian E110 cladding alloy is Zr-1Nb) and has not been validated by PNNL. Therefore it will not be included in this assessment.

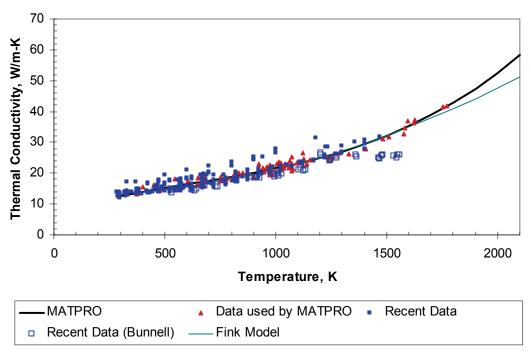
The CTHCON model is based on thermal conductivity data for both Zircaloy-2 and Zircaloy-4. This model draws no distinction between these two alloys. CTHCON is a function of temperature only. No thermal diffusivity data were used to develop the CTHCON model.

Hagrman et al. (1981) provides data source references, plots of data compared to the model, and tables of the thermal conductivity data used to develop the model, including data for Zircaloy-2 (Anderson et al., 1962, Lucks and Deem, 1958, and Powers, 1961) and Zircaloy-4 (Chirigos et al., 1961, Feith, 1966, and Scott, 1965).

A search was performed for Zircaloy thermal conductivity and diffusivity data published since the last modification of the CTHCON model in June 1978. Multiple data sources were found containing data from both Zircaloy-2 and Zircaloy-4 (Murabayashi et al., 1975, Gilchrist, 1976, Peggs et al., 1976, Bunnell et al., 1983, Maglic et al., 1994, Krett and Cleveland, 1997).

In addition, Fink (2000a) provides a summary of the data used to develop the CTHCON model in MATPRO, thermal diffusivity data not used in development of the CTHCON model, thermal conductivity data reported in the literature since the CTHCON model was produced, and a new second-order polynomial correlation that takes into account some of the newer thermal conductivity data.

Figure 2.14 provides a comparison of the CTHCON model as incorporated in MATPRO, FRAPCON-3.3, and FRAPTRAN-1.3 with the data on which it is based, extrapolated to the melting point of Zircaloy (2098K). In addition, this figure shows the more recent data and the Fink model. The scatter in the data due to differences in alloy, form, or measurement direction is comparable to the variation between individual data sets. The scatter in the data is distributed relatively uniformly around the curve representing the CTHCON model, except for the Bunnell et al. (1983) data above 1300K. However, these data are anomalously lower than all other data reported in the literature. It can be seen that below 1600K, the MATPRO model and the Fink model are relatively consistent with each other. The largest difference comes above 1600K, where the MATPRO model predicts higher conductivity than the Fink model. However, there is little data at these temperatures and the MATPRO model predicts the few high temperature data points better than the Fink model.



**Figure 2.14** MATPRO model (CTHCON), the data on which it is based, newer data, and the Fink Model.

Based on this comparison, it can be concluded that the model used in FRAPCON-3.3 and FRAPTRAN-1.3 for cladding thermal conductivity provides a best-estimate prediction for Zircaloy-2 and Zircaloy-4.

# 2.1.6.5 Gas Thermal Conductivity

The gas thermal conductivity models included in the GTHCON subroutines and those for FRAPCON-3.3 (Lanning et al. 2005a) and FRAPTRAN-1.3 (Cunningham et al. 2001a) exhibit some differences. The thermal conductivity models for the gases helium (He), argon (Ar), krypton (Kr), xenon (Xe), hydrogen (H<sub>2</sub>), and nitrogen (N<sub>2</sub>) are the same in both codes (with the exception of one difference in the fourth significant digit of the "bb" parameter for Xe). The individual gas thermal conductivity models and fit coefficients in both codes agree with those listed in MATPRO (Hagrman et al. 1981). The methodology for calculating the thermal conductivity of gas mixtures is identical in both codes (with the exception of one difference in the fourth and fifth significant digits of the "a" parameter for steam (H<sub>2</sub>O)) and agrees with that described in Hagrman et al. The gas thermal conductivity model for steam is different in FRAPCON-3.3 and FRAPTRAN-1.3, and neither code agrees with the steam conductivity model in Hagrman et al. This discrepancy, and what will be done regarding this will be discussed below.

The mixing model included in FRAPCON-3.3 is identical to that employeed in FRAPTRAN-1.3. This mixing model is identical to the mixing model described by Hagrman et al. (1981).

The data source references for the gas thermal conductivity models are provided by Hagrman et al. (1981) as follows. The He model is based on data from Johnston and Grilly (1946), Kannuluik and Carman (1952), von Ubisch (1959), Zaitseva (1959), Cheung et al. (1962), Timrot and Totskii (1965), Timrot and Umanskii (1965), Gambhir et al. (1967), and Saxena and Saxena (1968a). The Ar model is based on data from Kannuluik and Carman (1952), von Ubisch (1959),

Zaitseva (1959), Cheung et al. (1962), Gambhir et al. (1967), and Brokaw (1969). The Kr model is based on data from Kannuluik and Carman (1952), von Ubisch (1959), Zaitseva (1959), and Gambhir et al. (1967). The Xe model is based on data from Kannuluik and Carman (1952), Zaitseva (1959), and Gambhir et al. (1967). The H<sub>2</sub> model is based on data from Johnston and Grilly (1946) and Timrot and Umanskii (1966). The N<sub>2</sub> model is based on data from Keyes (1952), Cheung et al. (1962), and Brokaw (1969). The low temperature steam thermal conductivity model is taken from the American Society of Mechanical Engineers (ASME) (ASME, 1968), and the high temperature steam conductivity model is taken from Tsederberg (1965). The methodology for calculating the thermal conductivity of gas mixtures was taken from Brokaw (1969).

A literature search was performed to obtain more gas thermal conductivity data. The following sources of data were found for each type of gas

- Three new references were selected for comparison with the Hagrman et al. He thermal conductivity model over the temperature range 400-2500K. These were Faubert and Springer (1973), Jain and Saxena (1975), and Jody et al. (1977).
- Five new references were selected for comparison with the Hagrman et al. Ar thermal conductivity model over the temperature range 350-2500K. These were Timrot and Umanskii (1966), Saxena and Saxena (1968b), Faubert and Springer (1972), Springer and Wingeier (1973), and Stefanov et al. (1976).
- Three new references were selected for comparison with the Hagrman et al. Kr thermal conductivity model over the temperature range 318-2300K. These were Saxena and Saxena (1969), Vargaftik and Yakush (1971), and Stefanov et al. (1976).
- Three new references were selected for comparison with the Hagrman et al. Xe thermal conductivity model over the temperature range 298-2200K. These were Saxena and Saxena (1969), Springer and Wingeier (1973), and Stefanov et al. (1976).
- One new reference was selected for comparison with the Hagrman et al. H<sub>2</sub> thermal conductivity model over the temperature range 373-1273K. This was Saxena and Saxena (1970).
- Three new references were selected for comparison with the Hagrman et al. N<sub>2</sub> thermal conductivity model over the temperature range 304-2473K. These were Vargaftik and Zimina (1964), Faubert and Springer (1972), and Chen and Saxena (1973).

Figures 2.15 to 2.20 show the predicted and measured thermal conductivity for He, Ar, Kr, Xe,  $H_2$ , and  $N_2$ , respectively. Each of these figures show the MATPRO model, the data used in developing the MATPRO model, and recent data that has been collected as part of this assessment. It can be seen from these figures that the He model fits the data well up to 2500K. The Ar, Kr, Xe, and  $H_2$  models predict the data well up to 1200K, and overpredict the data at higher temperature. The  $N_2$  models predict the data well up to 1200K and underpredict the data at higher temperature. The poor performance of these rods at high temperature is due to a lack of available data when these correlations were developed. This will not affect any of the current predictions, because the steady-state gas temperature never gets above the temperature where the models deviate from the measurements. This may impact high temperature transient and accident analyses. These correlations will be updated to fit recent data in FRAPCON-3.4 and FRAPTRAN 1.4. The updates are discussed in Section 3.5.

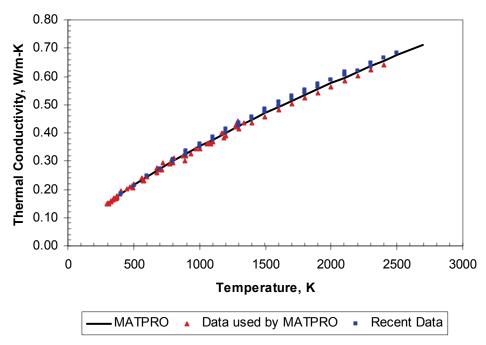


Figure 2.15 Thermal conductivity data and model predictions for He

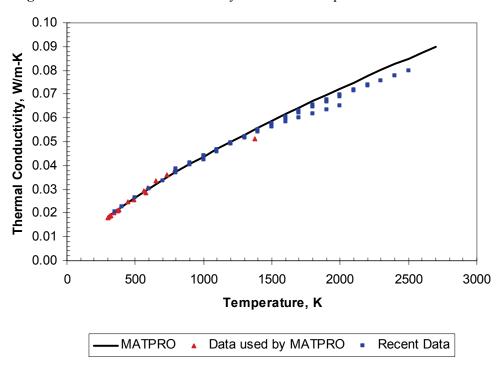


Figure 2.16 Thermal conductivity data and model predictions for Ar

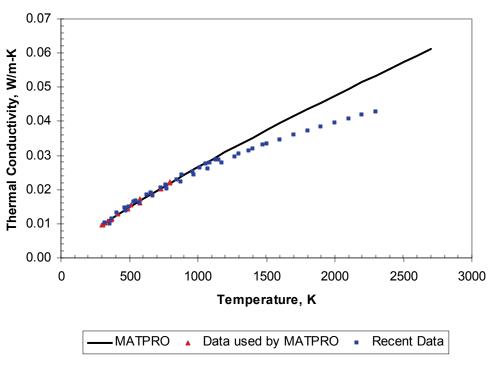


Figure 2.17 Thermal conductivity data and model predictions for Kr

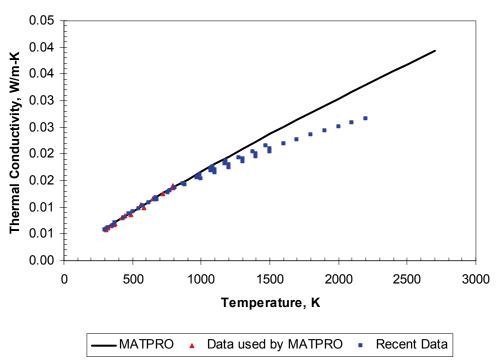


Figure 2.18 Thermal conductivity data and model predictions for Xe

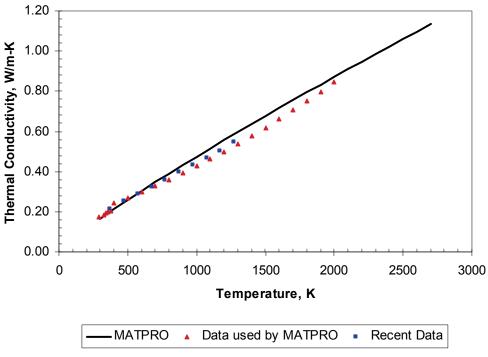


Figure 2.19 Thermal conductivity data and model predictions for H<sub>2</sub>

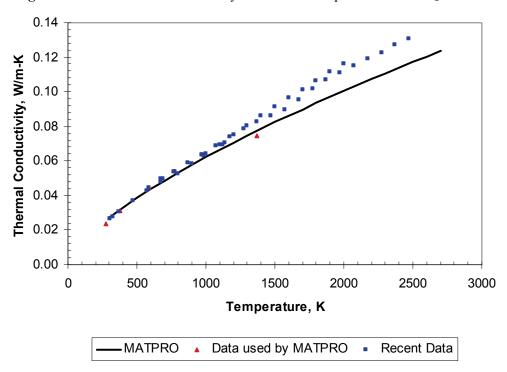
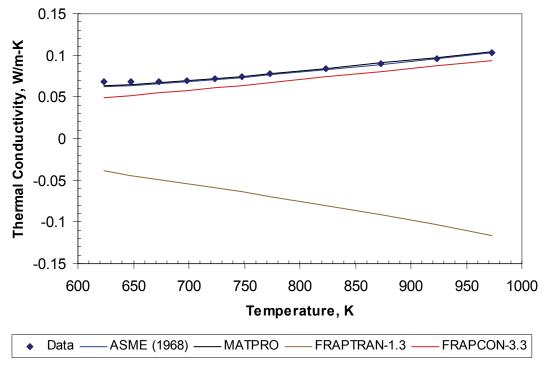


Figure 2.20 Thermal conductivity data and model predictions for N<sub>2</sub>

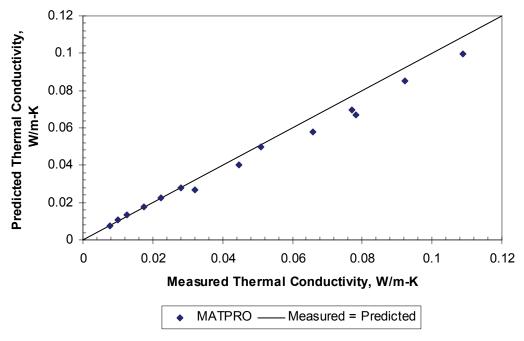
As discussed earlier, there is a difference in the models for steam conductivity between what is in MATPRO, FRAPCON-3.3, and FRAPTRAN-1.3. These three models are plotted in Figure 2.21 for a pressure of 100 MPa. Also shown in this figure is the ASME model that is essentially the same as the MATPRO model, and some data.

It can be seen from this figure that the MATPRO and ASME models predict the data well. The FRAPCON-3.3 model underpredicts the data by 10-30%, because it is only valid up to 0.1 MPa. The FRAPTRAN-1.3 model predicts negative values for the thermal conductivity which indicates a coding error in this model. The ASME model will be included in both FRAPCON-3.4 and FRAPTRAN-1.4 since it predicts the data best and is valid over the largest pressure range. This discrepancy has not affected any of the assessment cases to date since none of them used steam as a fill gas. In FRAPTRAN 1.3, the code uses steam in the fuel/cladding gap after the rods bursts, but at this point, temperature predictions are not of great concern.



**Figure 2.21** Thermal conductivity data and model predictions for steam at 100 MPa

The mixing model in FRAPCON-3.3 and FRAPTRAN-1.3 was used to compare against thermal conductivity data taken on various gas mixtures (Ibbs and Hirst, 1929, Mason and von Ubisch, 1960, and Gray and Wright, 1961). It can be seen from Figure 2.22 that the gas mixing model in FRAPCON-3.3 and FRAPTRAN-1.3 predicts these data well. Some biases in the predictions at higher temperatures may be due to over- or under-prediction in the individual conductivities of the gases at high temperature.



**Figure 2.22** Predicted vs. measured thermal conductivity for various gas mixtures.

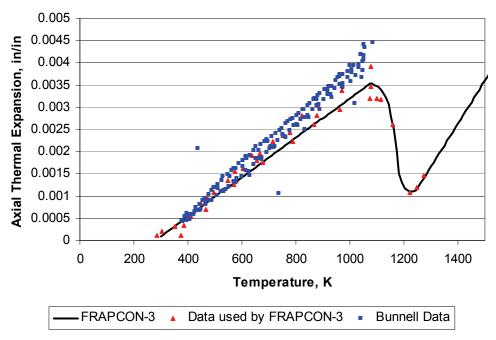
Based on this assessment, it is concluded that the He model for thermal conductivity and the mixing model are acceptable. The models for Ar, Kr, Xe, H<sub>2</sub>, and N<sub>2</sub> thermal conductivity will be fit to the new high temperature data that had not been available during the original model development. However, these changes are not expected to significantly change code predictions because the gap temperature is significantly less than 1200K. The models for steam conductivity in FRAPCON-3.3 and FRAPTRAN-1.3 will be replaced by the ASME model.

### 2.1.6.6 Cladding Thermal Expansion

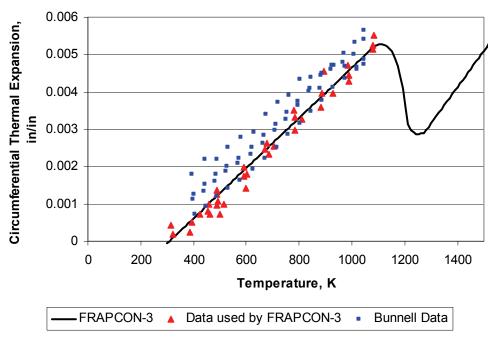
The cladding thermal expansion model in both FRAPCON-3.3 (Lanning et al. 2005a) and FRAPTRAN 1.3 (Cunningham et al. 2001a) is not the same as that in the CTHEXP model documented in MATPRO 11 Rev. 2 (Hagrman et al. 1981). Rather, the fuel codes use a look up table that contains thermal expansion in the axial and circumferential directions based on several data sources (Kearns 1965, Scott 1965, and Mehan and Wiesinger 1961).

The model in FRAPCON-3.3 and FRAPTRAN 1.3 was compared to these data and a litereature search was performed to determine if any other data are available. The search yielded one new data source (Bunnell et al. 1977). The data used in the development of the model in FRAPCON-3.3 and FRAPTRAN 1.3 as well as the new data are shown in Figures 2.23 and 2.24 for the axial and circumferential directions, respectively. It can be seen that the original data agree well with these models in both directions. The new data is slightly greater than the model in the circumferential direction, and significantly greater than the model in the axial direction. The original data were taken on as received cladding specimens with a room temperature reference. The data from Bunnell et al has been adjusted so the strain is zero at 300K, but the actual reference temperature for the experiment was not stated. Because of this uncertainty in the new data, the original data is assumed to better represent the thermal expansion of Zircaloy.

Based on the original thermal expansion data, the cladding thermal expansion model in FRAPCON-3.3 and FRAPTRAN 1.3 provides a best-estimate fit to data up to 1100K. Very little data exists above this temperature such that the model cannot be validated above 1100K.



**Figure 2.23** Axial thermal expansion model from FRAPCON-3.3 and FRAPTRAN 1.3 compared to data



**Figure 2.24** Circumferential thermal expansion model from FRAPCON-3.3 and FRAPTRAN 1.3 compared to data

# 2.1.7 Integral Assessment

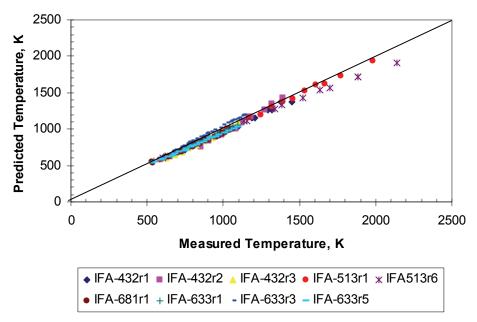
Instrument fuel rods irradiated in Halden have been used to assess the predicted temperatures from FRAPCON-3.3, by comparing the predictions to measurements taken in-reactor using centerline thermocouples, and expansion thermometers. The following sections show the results of temperature comparisons for UO<sub>2</sub> rods, UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> rods and MOX rods.

In a search of the literature, PNNL has been unable to find any reported tests that have collected centerline temperature during fast transients. Therefore, FRAPTRAN-1.3 was not assessed relative to its prediction of centerline temperature. However, since it uses the same models as FRAPCON-3.3, it is expected to provide centerline temperature predictions that are as accurate as those of FRAPCON-3.3.

### 2.1.7.1 UO<sub>2</sub> Temperature Comparisons

FRAPCON-3 was initially assessed against BOL temperature measurements taken during the first ramp to power and against temperature measurements made throughout the life of the rod. Five rods are used to assess the performance of FRAPCON-3 at beginning of life. These rods are IFA-432 rod 1, IFA-432 rod 2, IFA-432 rod 3, IFA-513 rod 1, and IFA-513 rod 6. Four additional rods, IFA-681r1, IFA-633r1, IFA-633r3, and IFA-633r5 were recently added to the beginning of life temperature assessment. The rods, IFA-432 rod 1, IFA-432 rod 2, IFA-432 rod 3, IFA-513 rod 1, IFA-513 rod 6, and IFA-562 rod 18 were also initially used to assess the performance of FRAPCON-3 as a function of burnup with a seventh rod being recently added. The seventh rod is IFA-597 rod 8. IFA-432 rod 2 has been removed as an assessment of FRAPCON-3 as a function of burnup, as the test is not prototypic of current fuel designs due to its large gap, and a small overprediction in fission gas release can result in a large temperature overprediction.

Figure 2.25 shows the predicted vs. measured temperature for the BOL ramp up to power for the five assessment cases. It can be seen from this figure that FRAPCON-3.3 predicts these temperatures within  $\pm 50$ K for all these rods except IFA-513r6. This rod is slightly underpredicted at high temperatures. However, this prediction is still within the uncertainty of the data. A  $\pm 50$ K uncertainty on temperature predictions is reasonable given the uncertainty in the thermocouple data and the calculated rod power.



**Figure 2.25** Predicted and measured temperature for BOL ramp to power.

The following figures show measured and predicted fuel centerline temperatures from rods with centerline temperature measurements. Individual rod predictions may demonstrate a systematic error (bias) that may be due to thermocouple decalibration or a systematic error in the power history provided due to decalibration in the neutron detectors. However, when all the comparisons are examined, it is found that there is no overall systematic error (bias) in the prediction of  $UO_2$  fuel temperature throughout life similar to what was seen in Figure 2.25 for  $UO_2$  at BOL.

Figure 2.26 shows the measured and predicted centerline temperature for IFA-432r1. This figure contains data from the lower thermocouple. This rod also contained an upper thermocouple, but it failed after 150 days. The comparisons to the upper thermocouple data are similar to the lower thermocouple. This figure shows excellent agreement between the FRAPCON-3.3 predictions and the data.

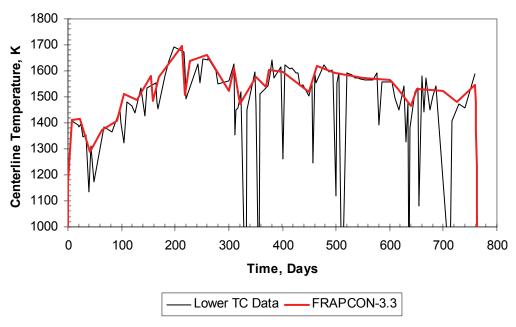


Figure 2.26 Measured and predicted centerline temperature for IFA-432r1 lower thermocouple (Burnup=45 GWd/MTU, as-fabricated radial gap=114μm)

Figure 2.27 shows the measured and predicted centerline temperature for IFA-432r3. This figure contains data from the lower thermocouple. This rod also contained an upper thermocouple, but it failed after 550 days. The comparisons to the upper thermocouple data are similar to the lower thermocouple. This figure shows excellent agreement between the FRAPCON-3.3 predictions and the data at beginning of life, and overprediction of about 100K at end of life. This overprediction may be due to FRAPCON-3.3 overpredicting the gas release, leading to higher predicted temperatures. As noted earlier, overprediction of gas release leads to lower gap conductivity and results in higher fuel temperature predictions.

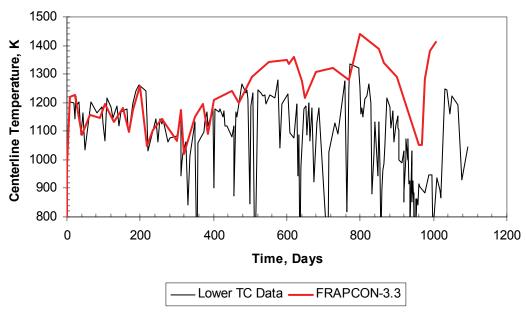


Figure 2.27 Measured and predicted centerline temperature for IFA-432r3 lower thermocouple (Burnup=45 GWd/MTU, as-fabricated radial gap=38μm)

Figure 2.28 shows the measured and predicted centerline temperature for IFA-513r1. This figure contains data from the upper and lower thermocouples. This figure shows reasonable agreement between the FRAPCON-3.3 predictions and the data.

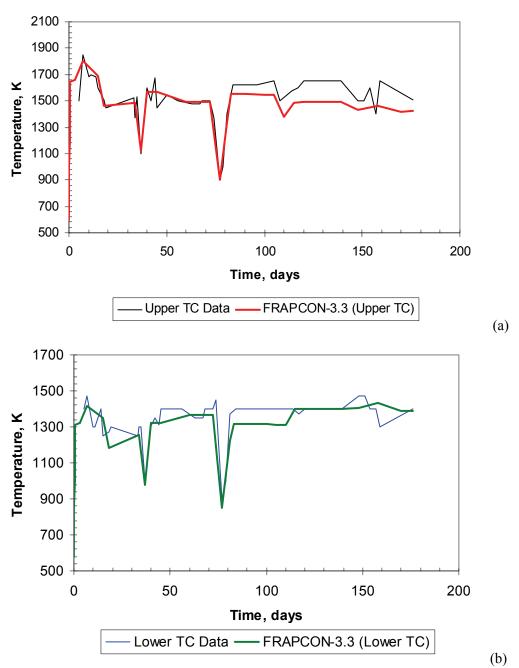


Figure 2.28 Measured and predicted centerline temperature for IFA-513r1 upper thermocouple (a) and lower thermocouple (b) (Burnup=10 GWd/MTU, as-fabricated radial gap=108μm)

Figure 2.29 shows the measured and predicted centerline temperature for IFA-513r6. This figure contains data from the upper and lower thermocouples. This figure shows reasonable agreement between the FRAPCON-3.3 predictions and the data.

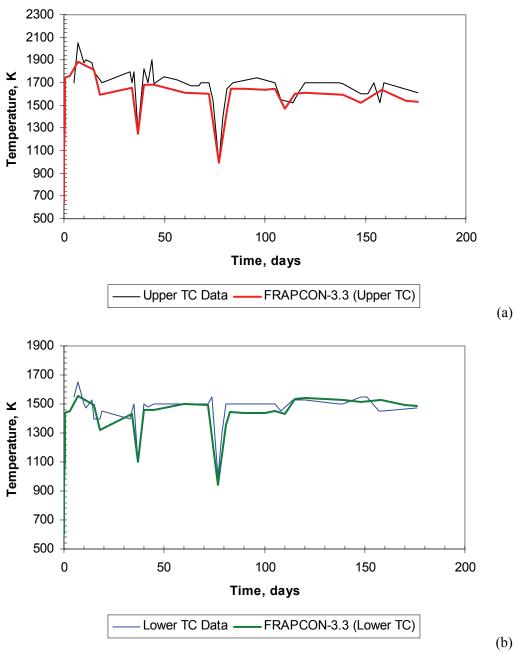


Figure 2.29 Measured and predicted centerline temperature for IFA-513r6 upper thermocouple (a) and lower thermocouple (b) (Burnup=10 GWd/MTU, as-fabricated radial gap=108μm)

Figure 2.30 shows the measured and predicted centerline temperature for IFA-562r18. This figure contains rod-average data from the expansion thermometer. This figure shows excellent agreement between the FRAPCON-3.3 predictions and the data.

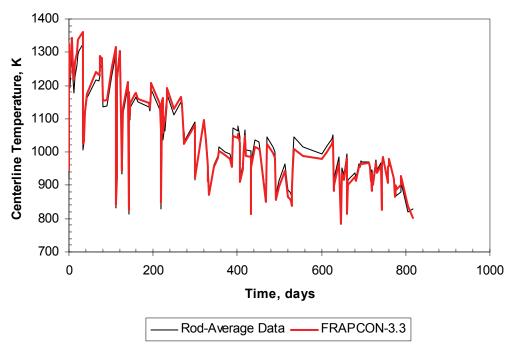


Figure 2.30 Measured and predicted rod-average centerline temperature for IFA-562r18 (Burnup=76 GWd/MTU, as-fabricated radial gap=50μm)

Figure 2.31 shows the measured and predicted centerline temperature for IFA-597r8. This rod was refabricated from a commercial rod that was irradiated to 68 GWd/MTU. This figure contains upper thermocouple data. This figure shows reasonable agreement between the FRAPCON-3.3 predictions and the data (±75K).

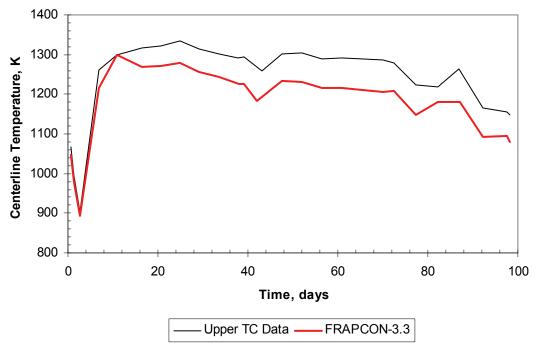


Figure 2.31 Measured and predicted centerline temperature for IFA-597r8 (starting burnup=68 GWd/MTU, ending burnup=71 GWd/MTU, as-fabricated radial gap=105μm).

This section demonstrates that FRAPCON-3.3 continues to provide a best-estimate prediction of centerline temperature for  $UO_2$  rods to within  $\pm 70$ K for recent experimental data.

### 2.1.7.2 UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> Temperature Comparisons

The adjustment for gadolinia in the thermal conductivity model has recently been assessed against centerline temperature predictions from three instrumented fuel assemblies irradiated at the Halden Reactor. The results of these comparisons are provided in this section.

Figures 2.32 and 2.33 show the measured and predicted centerline temperature for IFA-515.10. Rods A1 and B1 are UO<sub>2</sub> rods and rods A2 and B2 are UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> rods with depleted Gd. These rods were meant to show the difference only due to the thermal conductivity degradation from Gd<sub>2</sub>O<sub>3</sub>, not due to the difference in radial power profile. It can be seen from these figures that FRAPCON-3.3 predicts the centerline temperatures for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> rods as well as for UO<sub>2</sub> rods. In these figures the vertical line denotes where the thermocouple failed. Although data was reported after this point, it is not valid.

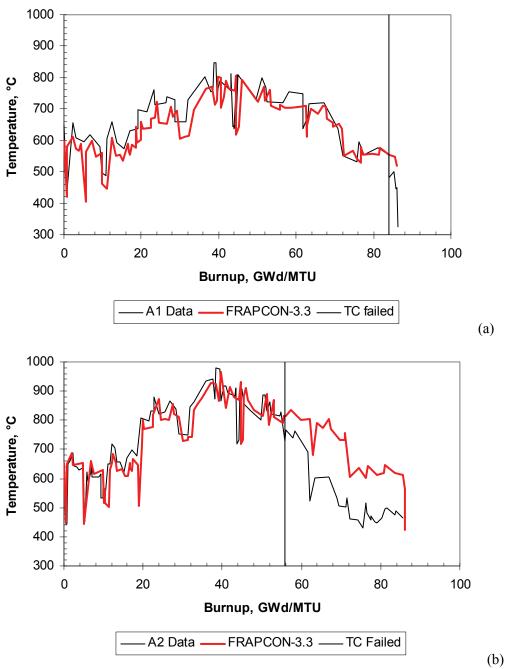


Figure 2.32 Measured and predicted centerline temperature for IFA-515.10 rod A1 (UO<sub>2</sub>) (a), and for IFA-515.10 rod A2 (UO<sub>2</sub>-8%Gd<sub>2</sub>O<sub>3</sub>) (b) (Burnup=80 GWd/MTU, as-fabricated radial gap=25μm)

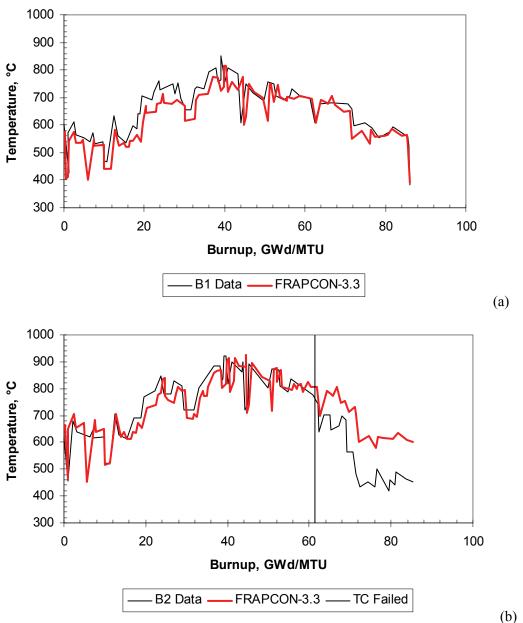


Figure 2.33 Measured and predicted centerline temperature for IFA-515.10 rod B1 (UO<sub>2</sub>) (a), and for IFA-515.10 rod B2 (UO<sub>2</sub>-8%Gd<sub>2</sub>O<sub>3</sub>) (b) (Burnup=80 GWd/MTU, as-fabricated radial gap=25µm)

Figures 2.34 and 2.35 show the measured and predicted centerline temperature for IFA-636 rod 2 and rod 4. These rods contain standard Gd. Because of this, it was necessary to modify FRAPCON-3 to use the radial power profiles provided by Halden for these rods. Rod 2 was equipped with a centerline thermocouple and the data from this thermocouple is shown in Figure 2.32. Rod 4 contains solid pellets, and the data shown in Figure 2.34 is estimated from Rod 2. Because of this, there is more uncertainty in the data from rod 4. In addition, during the first rise to power, as the Gd is burning out, there is a high level of uncertainty on the rod power. Because of this, FRAPCON-3.3 may not predict the centerline temperature well during this period. These

figures show excellent agreement between the FRAPCON-3.3 predictions and the data for rod 2 and reasonable agreement for rod 4 that has greater uncertainty.

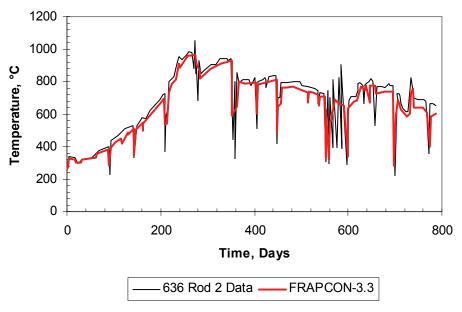


Figure 2.34 Measured and predicted centerline temperature for IFA-636r2 (UO<sub>2</sub>-8%Gd<sub>2</sub>O<sub>3</sub>) (Burnup=25 GWd/MTU, as-fabricated radial gap=77μm)

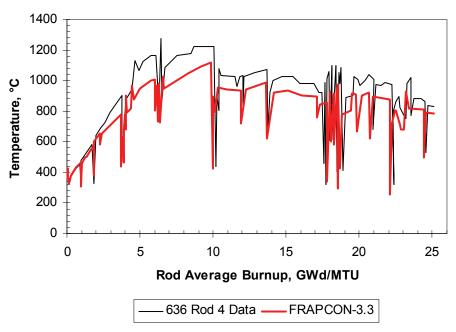


Figure 2.35 Measured and predicted centerline temperature for IFA-636r4 (UO<sub>2</sub>-8%Gd<sub>2</sub>O<sub>3</sub>) (Burnup=25 GWd/MTU, as-fabricated radial gap=77μm)

Figures 2.36 through 2.38 show the measured and predicted centerline temperature for IFA-681 rod 1, rod 2 and rod 3. Rods 4-6 are not shown here, because there are still some issues in regards to calibrating the data from these rods. Rod 1 is a UO<sub>2</sub> rod. Rods 2 and 3 contain standard Gd with 2 wt% and 8 wt% Gd<sub>2</sub>O<sub>3</sub>. Because of this, it was necessary to use the modified FRAPCON-3 discussed above to use the radial power profiles provided by Halden for these rods. During the

first rise to power, as the Gd is burning out, there is a high level of uncertainty on the rod power. Because of this, FRAPCON-3.3 may not predict the centerline temperature well during this period. These figures show excellent agreement between the FRAPCON-3.3 predictions and the data for all three rods, particularly after the Gd has burned out (~100 days for Figure 2.37, >175 days for Figure 2.38) and there is less uncertainty in the rod power.

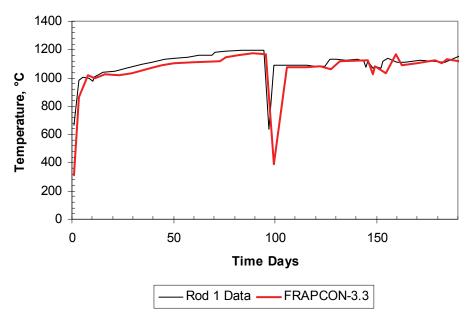


Figure 2.36 Measured and predicted centerline temperature for IFA-681r1 (UO<sub>2</sub>) (Burnup=12 GWd/MTU, as-fabricated radial gap=85µm)

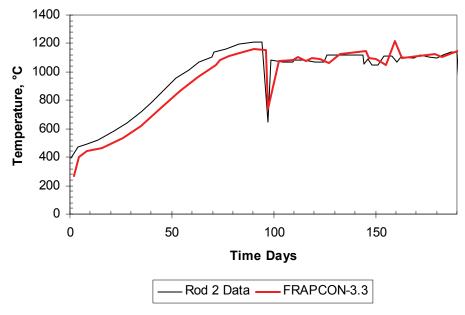


Figure 2.37 Measured and predicted centerline temperature for IFA-681r2 (UO<sub>2</sub> 2%Gd<sub>2</sub>O<sub>3</sub>) (Burnup=10 GWd/MTU, as-fabricated radial gap=85μm)

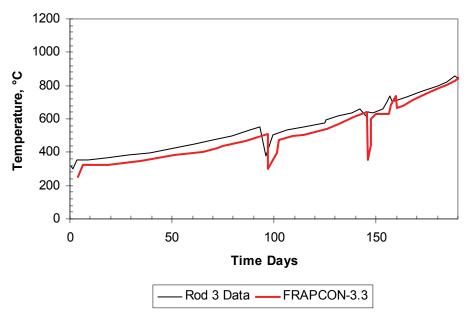


Figure 2.38 Measured and predicted centerline temperature for IFA-681r3 (UO<sub>2</sub> 8%Gd<sub>2</sub>O<sub>3</sub>) (Burnup=4 GWd/MTU, as-fabricated radial gap=85μm)

# 2.1.7.3 MOX Temperature Comparisons

FRAPCON-3.3 predictions have been benchmarked against centerline temperatures taken from five Halden tests with instrumented fuel assemblies containing 9 rods. The results of these comparisons are provided in this section.

Figure 2.39 shows the results of all nine rods as predicted centerline temperature vs. measured centerline temperature. It can be seen from this figure that although predictions of individual rods may be biased high or low, the overall predictions are in excellent agreement with the measurements ( $\pm 10\%$ ).

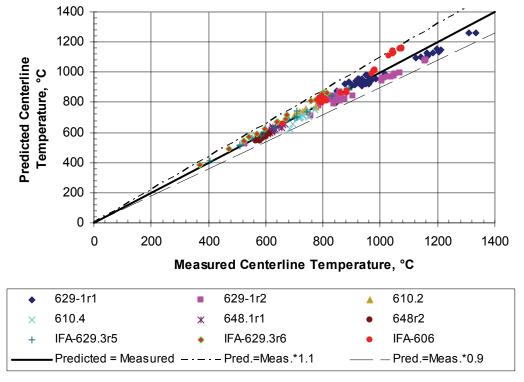


Figure 2.39 Predicted vs. measured centerline temperature for Halden MOX rods.

Figures 2.40 and 2.41 show the measured and predicted centerline temperatures for IFA-629-1 rods 1 and 2. These figures show good agreement between the FRAPCON-3.3 predictions and the data. The slight offset during parts of the irradiation could be due to power or thermocouple calibration changes at the end of each cycle.

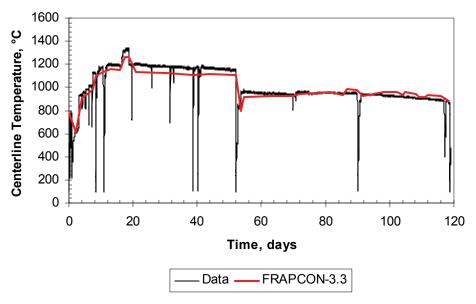


Figure 2.40 Measured and predicted centerline temperature for IFA-629-1 rod 1 (starting burnup=27 GWd/MTU, ending burnup=33 GWd/MTU, as-fabricated radial gap=84μm)

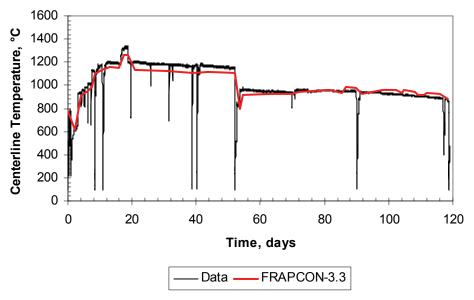


Figure 2.41 Measured and predicted centerline temperature for IFA-629-1 rod 2 (starting burnup=29 GWd/MTU, ending burnup=40 GWd/MTU, as-fabricated radial gap=84μm)

Figures 2.42 and 2.43 show the measured and predicted centerline temperature for IFA-610.2 and IFA-610.4. These figures show excellent agreement between the FRAPCON-3.3 predictions and the data.

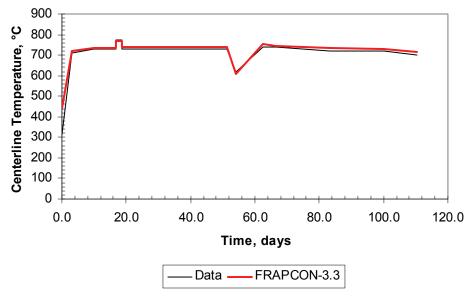


Figure 2.42 Measured and predicted centerline temperature for IFA-610.2 (starting burnup=55 GWd/MTU, ending burnup=56 GWd/MTU, as-fabricated radial gap=84μm)

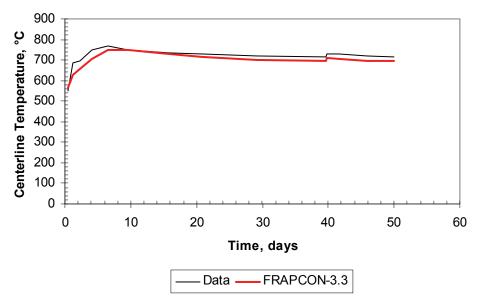


Figure 2.43 Measured and predicted centerline temperature for IFA-610.4 (starting burnup=56, ending burnup=57 GWd/MTU, as-fabricated radial gap=84μm)

Figures 2.44 and 2.45 show the measured and predicted centerline temperature for IFA-648.1 rods 1 and 2. These figures show excellent agreement between the FRAPCON-3.3 predictions and the data.

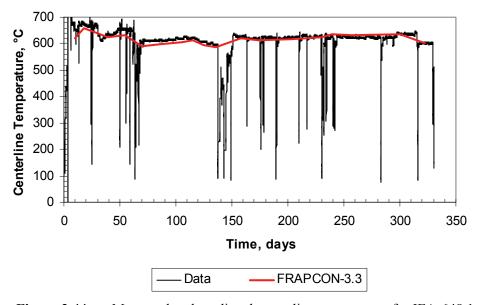


Figure 2.44 Measured and predicted centerline temperature for IFA-648.1 rod 1 (starting burnup=55 GWd/MTU, ending burnup=62 GWd/MTU, as-fabricated radial gap=84µm)

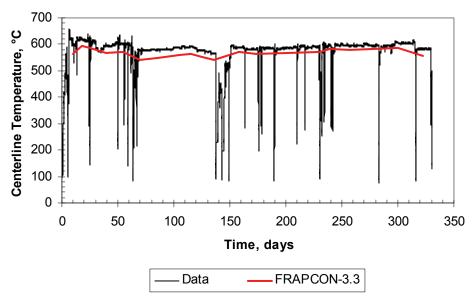


Figure 2.45 Measured and predicted centerline temperature for IFA-648.1 rod 2 (starting burnup=55 GWd/MTU, ending burnup=62 GWd/MTU, as-fabricated radial gap=84μm)

Figures 2.46 and 2.47 show the measured and predicted centerline temperature for IFA-629.3 rods 5 and 6. These figures show excellent agreement between the FRAPCON-3.3 predictions and the data.

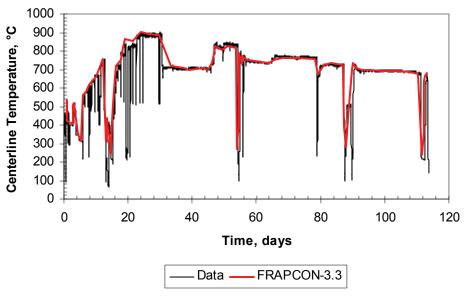


Figure 2.46 Measured and predicted centerline temperature for IFA-629.3 rod 5 (starting burnup=62 GWd/MTU, ending burnup=72 GWd/MTU, as-fabricated radial gap=84μm)

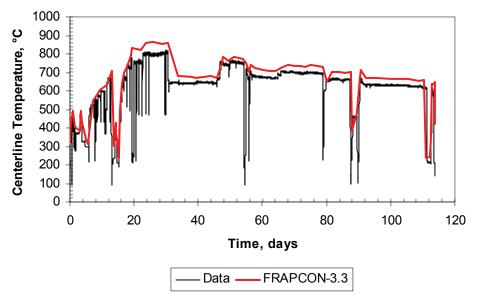
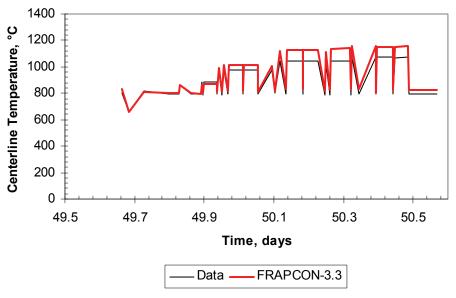


Figure 2.47 Measured and predicted centerline temperature for IFA-629.3 rod 6 (starting burnup=62 GWd/MTU, ending burnup=68 GWd/MTU, as-fabricated radial gap=84μm)

Figure 2.48 shows the measured and predicted centerline temperature for IFA-606 Phase 2. This figure shows reasonable agreement between the FRAPCON-3.3 predictions and the data (within  $\pm 75$ K).



**Figure 2.48** Measured and predicted centerline temperature for IFA-606 Phase 2 (starting burnup=50 GWd/MTU, as-fabricated radial gap=94μm)

# 2.2 Fission Gas Release Model and Assessment

The following section describes the fission gas release model in FRAPCON-3.3 and provides an assessment of the prediction. It is important to be able to predict fission gas release; especially at

high release levels as fission gas increases the rod internal pressure and degrades the gap thermal conductivity, increasing the fuel temperature.

# 2.2.1 Modeling

The fission gas release (FGR) model in FRAPCON-3.3 is a two-stage diffusion model. Gas is produced inside spherical grains at a rate proportional to power generation. Gas is allowed to diffuse from these grains to the grain boundaries that are considered to be an infinite sink for gas atoms. The diffusion of gas from the grains is controlled by a diffusion coefficient that is a function of temperature and burnup.

When the gas atoms arrive at the grain boundaries a fraction of these atoms are considered to be re-solved back into the grain. However, since the resolution depth is very small, these atoms are not added back into the atoms still in the grain, but are stored separately as resolved gas. The remaining gas accumulates on the grain boundary until the grain boundary saturation is exceeded. This saturation value is a function of temperature, external pressure, and grain size. When the saturation value is exceeded, both the gas on the grain boundary and the resolved gas are released to the rod void volume. The concentration of gas on the grain boundaries must then exceed the saturation value for further release to occur.

In addition to this thermally driven gas release, an athermal contribution is also determined that models the release of an additional 1% gas for every 10 GWd/MTU of rod average burnup above 40 GWd/MTU.

In order to accurately model MOX fuel, the diffusion coefficient is increased by an empirical constant factor to account for the observation of greater gas release from MOX than UO<sub>2</sub>.

Many of the parameters in this model are difficult to measure in-reactor. In order to develop this model, values are selected such that the model gives a best-estimate prediction of gas release for a wide variety of rod types and conditions.

In this model, the following parameters were selected to best predict measured FGR data from rods in the assessment database.

- Pre-exponential diffusion coefficient
- Activation energy for diffusion coefficient
- Burnup dependence of the diffusion coefficient
- Coefficient that defined the fraction of gas arriving on the grain boundaries that is resolved

There is no FGR model in FRAPTRAN-1.3 because it was thought that the time periods over which events are modeled in FRAPTRAN are too short for gas to diffuse and release to occur. However, in experimental programs performed in the Cabri reactor (Papin et al., 2003) large amounts of fission gas have been released during RIA events (5-33%). This is believed to be due to grain boundary cracking and separation during the fast transient. Because of this, it is important that a transient FGR model be developed for FRAPTRAN-1.3 and that the steady-state FGR in FRAPCON-3.3 be assessed and modified if necessary to initialize FRAPTRAN.

The following section will show the fit of the FGR model in FRAPCON-3.3 to the data from rods in the assessment database.

### 2.2.2 Assessment

The assessment of the  $UO_2$  model for fission gas release is documented in Lanning et al. (2005a). Figures 2.49 and 2.50 show the predicted fission gas release as a function of measured fission gas release for the steady-state rods and power ramped rods, respectively. Figures 2.51 and 2.52 show the predicted minus measured fission gas release as a function of burnup for the steady-state rods and power ramped rods, respectively. The standard deviation for the steady state predictions is 2.8 % FGR. The standard deviation for the power ramped cases is 5.3% FGR. These figures demonstrate that FRAPCON-3.3 provides a best-estimate calculation of fission gas over a wide range of burnup and gas release levels.

It has been observed that FRAPCON-3.3 seems to slightly underpredict power ramped rods with short hold times (<4 hours). In Figure 2.52 the rods with short hold times are noted. Although two of these rods are within the standard error of the predictions, the fact that all three rods with short hold time are underpredicted, leads to the conclusion that FRAPCON-3.3 may underpredict power ramped rods with short (<4 hours) hold times. In future versions of FRAPCON-3, this underprediction will be addressed. Until this time, PNNL has recommended that the hold time for power ramps less than 4 hours be increased by a factor of 3 to conservatively bound the expected fission gas release (Beyer, 2007).

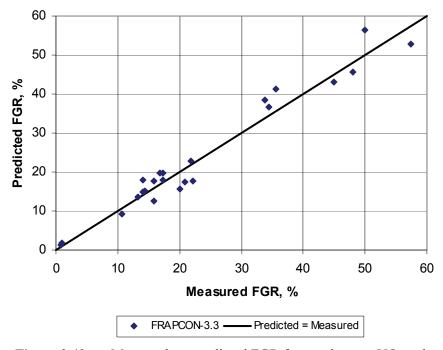


Figure 2.49 Measured vs. predicted FGR for steady-state UO<sub>2</sub> rods

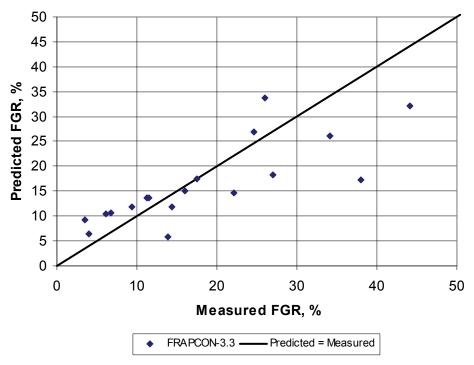


Figure 2.50 Measured vs. predicted FGR for power ramped UO<sub>2</sub> rods

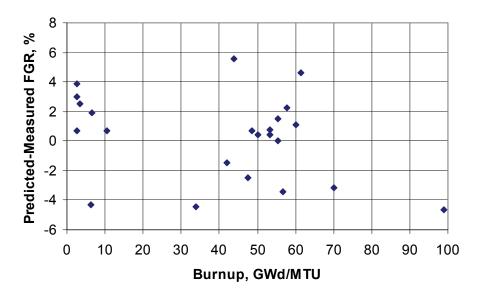


Figure 2.51 Predicted minus measured FGR as a function of burnup for steady-state UO<sub>2</sub> rods

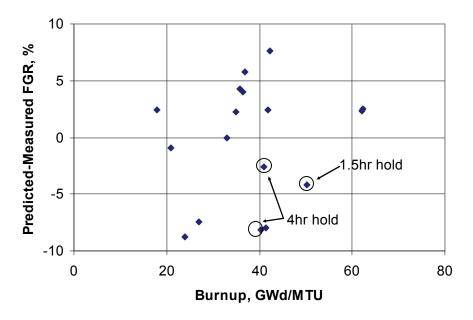


Figure 2.52 Predicted minus measured FGR as a function of burnup for power ramped UO<sub>2</sub> rods (Rods with hold time less than 4 hours marked)

A limited assessment of the MOX fission gas release model was performed by Lanning et al. (2005a). Since then, more MOX rods were added to the database and a more comprehensive assessment was performed and is documented in Lanning et al. (2005b) and Geelhood and Bever (2008). Figure 2.53 shows the predicted fission gas release as a function of measured fission gas release for the steady-state and power ramped rods. Figure 2.54 shows the predicted minus measured fission gas release as a function of burnup. It can be seen that there is a large degree of scatter in the predictions. However, for the rods with the large overprediction, (ATR phase I and II and M504) there are no measured temperatures available to verify that this overprediction is due solely to a deviation in the FGR model. In addition, these rods were irradiated in test reactors with small cores and consequently there could be considerable uncertainty in the reported power levels. However, for the cases with measured temperature below 62 GWd/MTU (IFA-651.1, IFA-629.1, IFA-606 phase 2, IFA-597.4,.5,.6,.7 and IFA-633.1 Rod 6) FRAPCON-3.3 provides a much better prediction of fission gas over a wide range of gas release levels up to a burnup of 58 GWd/MTU with a standard error of 4.2% FGR. For example, those rods that demonstrated a small underpredicition in fuel temperature also resulted in a small underprediction in FGR and for those rods with a small overprediction in FGR were similarly overpredicted. Figure 2.54 indicates that the model may underpredict FGR from MOX at high burnups (>60 GWd/MTU) based on the two rods from IFA-629.3 where fuel temperatures were predicted well (Rod 5 in Figure 2.46) or overpredicted (Rod 6 in Figure 2.47) and FGR was underpredicted. It is recommended that more high burnup FGR data be obtained as it becomes available and attempt to verify or refute behavior with MOX.

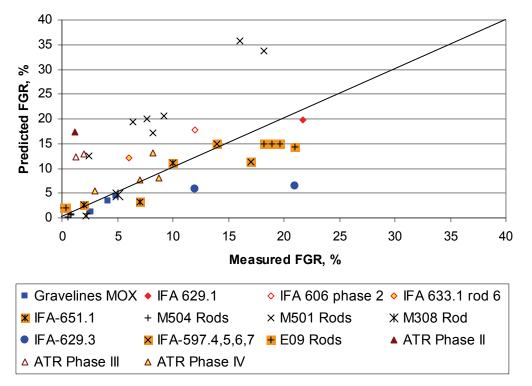
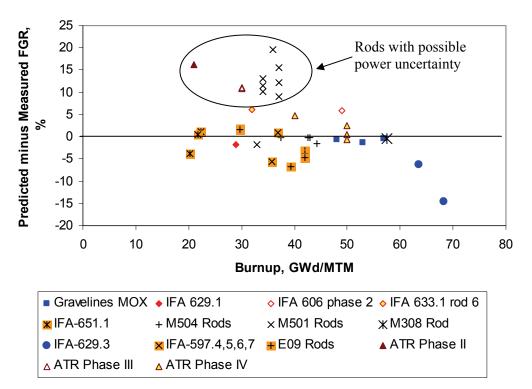


Figure 2.53 Measured vs. predicted FGR for steady-state and power ramped MOX rods



**Figure 2.54** Predicted minus measured FGR as a function of burnup for steady-state and power ramped MOX rods

Based on the above assessment, it can be concluded that FRAPCON-3.3 provides a best-estimate prediction of FGR for UO<sub>2</sub> rods and MOX rods up to 60 GWd/MTU. At higher burnup, more data is needed to assess if the MOX model still provides a best-estimate prediction of FGR.

A transient fission gas release model is being developed and implemented in FRAPTRAN-1.4. This model will be initialized with the new model in FRAPCON-3.4 that accurately predicts the concentration of gas in the grains and on the grain boundaries. This model is not presented in this report.

# 2.3 Cladding Corrosion and Hydriding Models

The following sections discuss the assessment of the cladding corrosion and hydriding models in FRAPCON-3.3 and FRAPTRAN-1.3. It is important to accurately predict oxidation to determine the temperature drop across the cladding. It is also important to accurately predict hydrogen pickup so cladding ductility can be calculated.

## 2.3.1 Cladding Corrosion

The corrosion model in MATPRO has been developed to model cladding corrosion in BWR rods. The cladding corrosion model in FRAPCON-3.3 has been modified from that of the MATPRO model, CORROS, because the MATPRO model underpredicted cladding corrosion by a factor of 4 to 5 for PWR rods. The new model is described in Lanning et al. (1997a) and is applicable for Zircaloy-2 and Zircaloy-4 in BWR and PWR environments. In addition, this model has recently been modified to account for the reduced corrosion seen in ZIRLO<sup>TM</sup> and M5<sup>TM</sup>. These modifications are described in Lanning, et al., (2005a)

FRAPTRAN-1.3 does not model low temperature corrosion because the time periods of the events that FRAPTRAN-1.3 is used for are are not long enough for a significant amount to occur. FRAPTRAN-1.3 does model high temperature corrosion such as occurs during a loss-of-coolant accident (LOCA). In FRAPTRAN-1.3, the user can select to model high temperature corrosion with either the Cathcart/Pawel (Cathcart et al., 1977) or the more conservative Baker/Just (Baker et al., 1962) model.

Figure 2.55 shows the comparisons of the FRAPCON-3.3 prediction to data for PWR Zircaloy 4 cladding and coolant conditions. Figure 2.56 shows the comparisons of the FRAPCON-3.3 prediction to data for BWR Zircaloy-2 cladding and coolant conditions from the original model assessment (Lanning et al., 1997b). Since this time, BWR vendors have switched to using cladding with controlled second phase precipitate (SPP) sizes and more tightly defined chemical compositions. Data on these newer Zircaloy-2 cladding types has been collected and compared to the model for Zircaloy-2 BWR corrosion (Yasuyuki et al., 2007, Sell et al., 2006, Hirano et al., 2005, Mutyala, 2004). Figure 2.57 shows the comparisons of the FRAPCON-3.3 prediction to data from newer Zircaloy-2 BWR cladding. It can be seen from these figures that FRAPCON-3.3 provides good predictions of oxide thickness for older and new Zircaloy-2 and Zircaloy-4 in both BWR and PWR conditions.

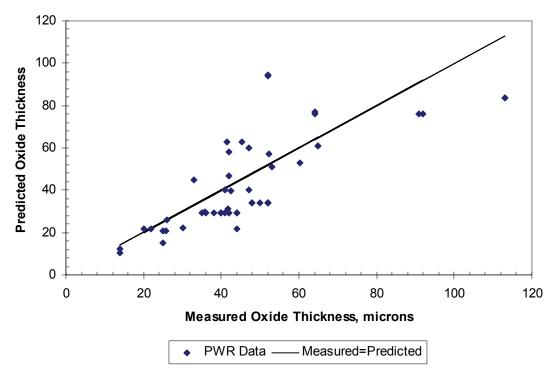
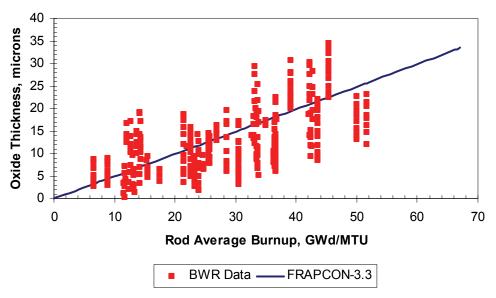


Figure 2.55 PWR Zircaloy-4 corrosion data and FRAPCON-3.3 PWR corrosion model (Smith et al., 1994, Pyecha, 1985, Newman, 1986, Balfour, 1982b, Dideon, 1983, Garde, 1986).



**Figure 2.56** BWR Zircaloy-2 corrosion data and FRAPCON-3.3 BWR corrosion model (West et al., 1983, Barner et al., 1990)

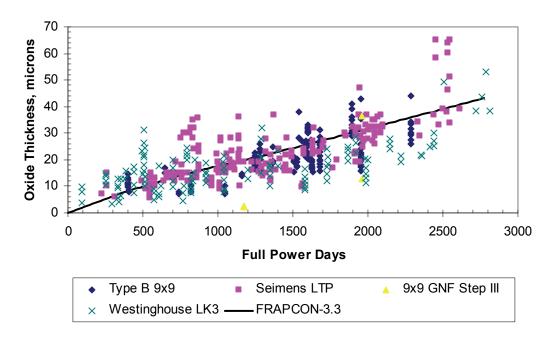
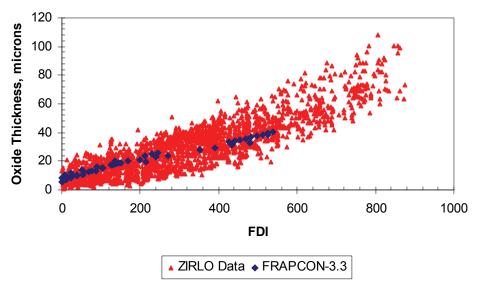
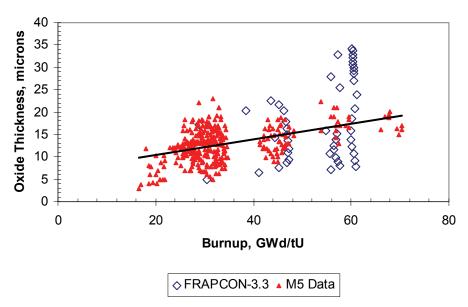


Figure 2.57 Zircaloy-2 BWR Corrosion Data for the Newer Cladding Types with Controlled SPP's and composition (Yasuyuki et al., 2007, Sell et al., 2006, Hirano et al., 2005, Mutyala, 2004)

As mentioned above, the corrosion model in FRAPCON-3.3 has recently been updated to include adjustments for the lower corrosion rates seen in the advanced cladding alloys ZIRLO<sup>TM</sup> and M5<sup>TM</sup>. This adjustment is simply a reduction of the current PWR model that fits the available data for ZIRLO<sup>TM</sup> (Knott et al., 2003) and M5<sup>TM</sup> (Mardon and Waeckel, 2003). Figures 2.58 and 2.59 show the corrosion data and model predictions for standard PWR cases using the ZIRLO<sup>TM</sup> and M5<sup>TM</sup> correlations, respectively. The ZIRLO data is plotted as a function of Fuel Duty Index (FDI) which is a function of power and time at power. Based on these comparisons FRAPCON-3.3 predicts the oxide thickness from ZIRLO<sup>TM</sup> and M5<sup>TM</sup> well.



**Figure 2.58** ZIRLO<sup>™</sup> data and FRAPCON-3.3 predictions as a function of fuel duty index (FDI) (Knott et al., 2003)



**Figure 2.59** M5<sup>TM</sup> data and FRAPCON-3.3 predictions as a function of burnup (Mardon and Waeckel, 2003)

However, recent data from high burnup Spanish and French rods clad in ZIRLO<sup>TM</sup> (CSN, ENUSA, 2002) and M5<sup>TM</sup> (Segura et al., 2002) indicate that the corrosion adjustments that have been recently made for these alloys underpredict the oxide thickness for ZIRLO<sup>TM</sup> at high burnup and overpredict the oxide thickness for M5<sup>TM</sup>. Figures 2.60 and 2.61 show the end of life oxide profile for two Spanish rods clad in ZIRLO<sup>TM</sup> irradiated to a rod average burnup of 68 GWd/MTU. Figure 2.62 shows the end of life oxide profile for a French rod clad in M5<sup>TM</sup> irradiated to 70 GWd/MTU. Also shown on these figures for reference is the FRAPCON-3.3 correlation for Zircaloy-4. These figures support the conclusions given above and emphasize the need to develop new correlations specifically for ZIRLO<sup>TM</sup> and M5<sup>TM</sup>, rather than just adding a multiplicative factor to the current correlation for Zircaloy. A new correlation will be developed

for M5<sup>™</sup> and ZIRLO<sup>™</sup> in FRAPCON-3.4 that will provide better predictions of the high burnup corrosion data. These new correlations are discussed in Section 3.1.

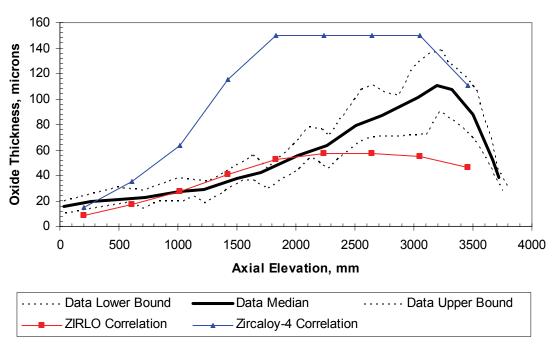


Figure 2.60 End of life oxide thickness and FRAPCON-3 predictions for Vandellos II rod A06, clad in ZIRLO<sup>TM</sup> and irradiated to 68 GWd/MTU (CSN, ENUSA, 2002).

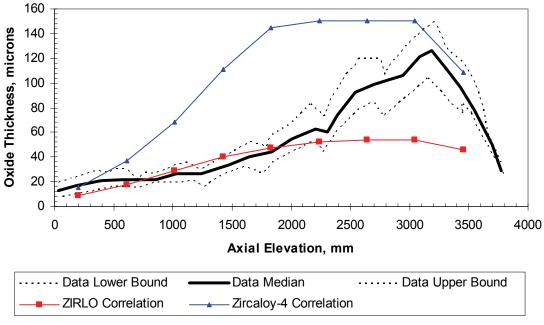


Figure 2.61 End of life oxide thickness and FRAPCON-3 predictions for Vandellos II rod A12, clad in ZIRLO<sup>TM</sup> and irradiated to 68 GWd/MTU(CSN, ENUSA, 2002).

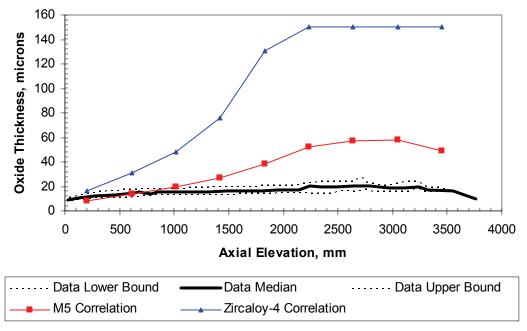


Figure 2.62 End of life oxide thickness and FRAPCON-3 predictions for Gravelines 5 rod N05, clad in M5<sup>TM</sup> and irradiated to 70 GWd/MTU (Segura et al., 2002).

Cunningham et al, (2001b) has assessed the Cathcart-Pawel and Baker-Just models in FRAPTRAN-1.3. The conclusion of this assessment is that the Cathcart-Pawel model is more accurate below 1800K, and the Baker-Just model is more accurate above 1800K. Experimental work is currently ongoing to determine the high temperature oxidation behavior for zirconium alloys as a function of burnup. It has been determined that fabrication and heat treatment as well as level of hydrides can drastically affect the high temperature oxidation performance. For example, it has been determined that M5 shows good oxidation performance, while E-110, which is nominally the same composition, shows very poor oxidation performance at high temperature in steam.

As more data become available, the high temperature oxidation models in FRAPTRAN-1.3 can be re-evaluated to determine if they provide a best-estimate calculation for high temperature corrosion. However, using the models currently in FRAPTRAN-1.3 with the above recommendations should provide close to a best-estimate prediction of high temperature oxidation behavior.

## 2.3.2 Hydrogen Pickup

FRAPCON-3.3 uses a hydrogen pickup fraction of 29% for BWR corrosion and 15% for PWR corrosion. These pickup fractions are valid for Zircaloy-2 and Zircaloy-4. The code has recently been changed to model the improved hydrogen pickup performance of ZIRLO<sup>TM</sup> and M5<sup>TM</sup>. The hydrogen pickup fraction for ZIRLO<sup>TM</sup> in a PWR is 12.5% while the hydrogen pickup fraction for M5<sup>TM</sup> in a PWR is 7.5%. No correlations for ZIRLO<sup>TM</sup> or M5<sup>TM</sup> in a BWR were developed since all the vendors currently use Zircaloy-2 cladding in BWRs.

FRAPTRAN does not model hydrogen pickup from low temperature corrosion, since it does not model low temperature corrosion. There has not been any data that indicated what the hydrogen

pickup would be during high temperature oxidation. Because of this, there is no hydrogen pickup model in FRAPTRAN.

Figure 2.63 shows the measured and predicted hydrogen data for PWR Zircaloy-4 rods. It can be seen from this figure that the model predicts the data well. Figure 2.64 shows the measured and predicted hydrogen pickup fraction for BWR Zircaloy-2 rods. Because there was such a limited number of BWR hydrogen pickup data, a literature search was performed to find more hydrogen pickup data for Zircaloy-2 in BWR conditions. A more recent data comparison of older Zircaloy-2 without controlled SPP sizes and compositions (Hayashi et al., 2003) and of newer Zircaloy-2 with controlled SPP sizes and compositions (Hayashi et al., 2003, Sell et al., 2006, Hirano et al., 2005, Ledberger et al., 2005) found that a constant hydrogen pickup fraction is not appropriate for hydrogen pickup in Zircaloy-2. Figure 2.65 shows the new data plotted as a function of local axial burnup along with the 29% hydrogen pickup fraction used in FRAPCON-3.3. In addition, it was found that the hydrogen pickup in new Zircaloy-2 where the vendors have better control over the alloy composition and second-phase precipitate (SPP) size is different from older Zircaloy. New correlations have been developed and will be included in FRAPCON-3.4 that provide a better prediction of the hydrogen pickup in older and new Zircaloy-2 as a function of burnup. These correlations are described in Section 3.1.

Figure 2.66 shows the measured and predicted hydrogen data for PWR ZIRLO™ rods (Tsukuda et al., 2003, Kitaguawa et al., 2005). It can be seen from this figure that the model predicts the data well. Figure 2.67 shows the measured and predicted hydrogen pickup fraction for PWR M5™. Also shown on this figure are hydrogen concentration values predicted by FRAPCON-3.3 for standard PWR rods. It can be seen from this figure that although there is significant scatter in the hydrogen content when plotted as a function of burnup, the model predicts the data well. This scatter is due to overprediction of oxide thickness and will be less for the new model described in Section 3.1

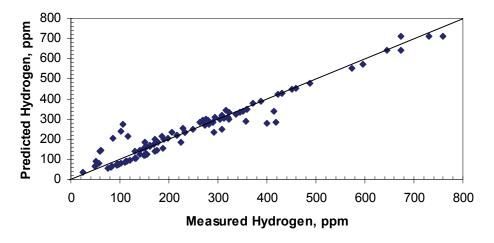
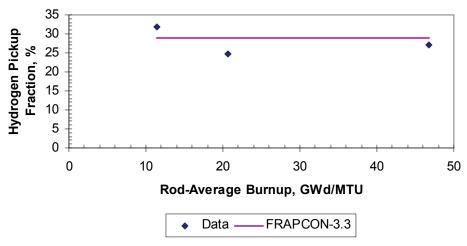


Figure 2.63 Measured and predicted hydrogen pickup for PWR rods with Zircaloy-4 cladding (Smith et al., 1994, Pyecha, 1985, Newman, 1986, Balfour, 1982b, Dideon, 1983, Garde, 1986)



**Figure 2.64** Measured and predicted hydrogen pickup for BWR rods with Zircaloy-2 cladding (Itagaki, 2003.)

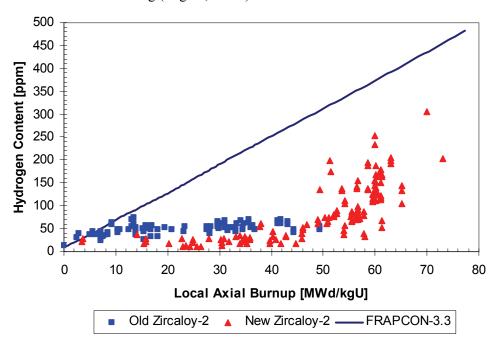
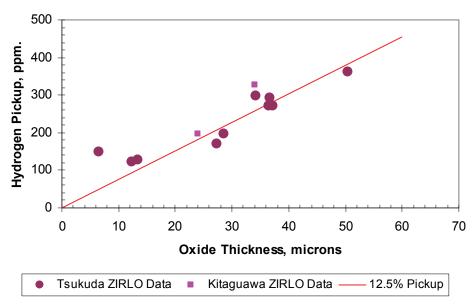
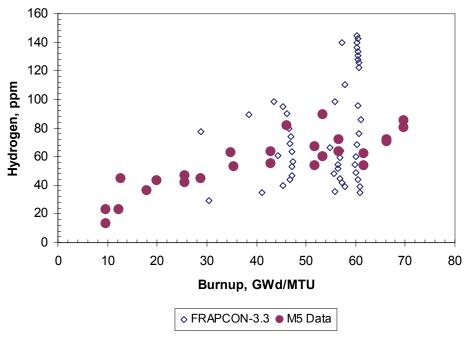


Figure 2.65 Measured and predicted hydrogen pickup from recent literature search for BWR rods with Zircaloy-2 cladding (Hayashi et al., 2003, Sell et al., 2006, Hirano et al., 2005, Ledberger et al., 2005)



**Figure 2.66** Measured and predicted hydrogen pickup for PWR rods with ZIRLO™ (Tsukuda et al., 2003, Kitaguawa et al., 2005)



**Figure 2.67** Measured and predicted hydrogen pickup for PWR rods with M5<sup>TM</sup> (Mardon and Waeckel, 2003)

# 2.4 Fuel Densification and Swelling

The following sections describe the fuel swelling and densification models in FRAPCON-3.3 and provides data comparisons for these models.

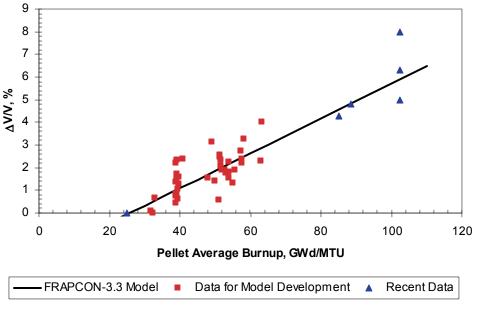
FRAPTRAN-1.3 does not contain a fuel densification or swelling model. This is acceptable because fuel densification and swelling are burnup-related phenomena and no significant burnup accumulates over the time periods of the events that are modeled in FRAPTRAN-1.3.

## 2.4.1 Fuel Swelling

The fuel swelling model in FRAPCON-3.3 has been modified from the model documented in MATPRO (Hagrman et al. 1981). This model is accurately described in Lanning et al (1997a). The swelling model in FRAPCON-3.3 is a function of pellet-average burnup only.

The swelling model is based on dimensional data obtained on UO<sub>2</sub> pellets and pellet stacks irradiated within cladding (i.e., constrained) in PWRs. Data obtained from ex-reactor, thermally-heated, unconstrained pellet swelling experiments were not included. Lanning et al. (1997a) provided data source references and plots of data compared to the modified FSWELL model. The PWR data of Dideon and Bain (1983), Garde (1986), Newman (1986), and Smith et al. (1994) were used to develop the swelling model in FRAPCON-3.3. A search was performed for recent fuel swelling data. Two references were found that included data for constrained UO<sub>2</sub> pellets irradiated in light water reactors (Zacharie et al., 1998, Lafchiev and Tverberg, 2005).

Figure 2.68 provides a comparison of the swelling model in FRAPCON-3.3, compared to the data on which it is based, up to the 70 GWd/MTU burnup limit specified by Lanning et al. (1997a). It can be seen from this figure that while there is considerable scatter in the swelling data, the FRAPCON-3.3 model seems to provide a best-estimate prediction of fuel swelling. A fuel swelling rate has been deduced from a number of Halden fuel assemblies (Lafchiev and Tverberg, 2005). These rates are shown in Figure 2.69 along with the FRAPCON-3.3 swelling rate of  $0.77\% \ \Delta V/V$  per 10 GWd/MTU. This figure shows that the swelling rate used on FRAPCON-3.3 is within the scatter of the swelling rates that have been observed at Halden, but slightly higher than the average rate from these data.



**Figure 2.68** FRAPCON-3.3 swelling model prediction and data as a function of burnup

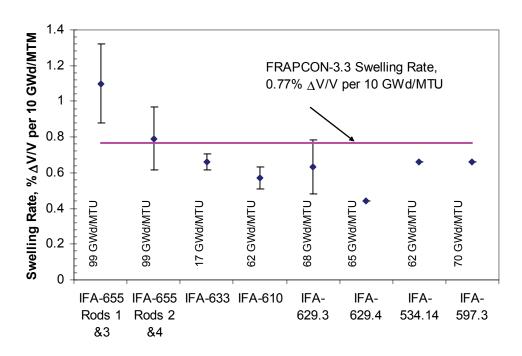


Figure 2.69 FRAPCON-3.3 swelling rate and observed swelling rates from Halden instrumented fuel assemblies (EOL burnups shown for each point)

#### 2.4.2 Fuel Densification

FRAPCON-3.3 uses the MATPRO model, FUDENS, to calculate fuel densification as a function of burnup and maximum densification. The code contains several methods for calculating maximum densification. The first and most commonly used method is to use the user-input value for maximum densification and simply convert this to a linear strain. The maximum densification can be estimated using a standard densification test (1700°C for 24 hours). This is the method recommended in US NRC Regulatory Guide 1.126 (1978) and has been shown to correlate well with observed maximum in-reactor densification. If the maximum densification is not input, FRAPCON-3.3 uses the equations given in the MATPRO subroutine FUDENS that are a function of fuel temperature, fuel density, and fuel sintering temperature.

The FUDENS model in FRAPCON-3.3 has been fit to provide the best fit to the data of Freshley et al. (1976). A search was performed for recent fuel densification data. Three new sources of data (Banks, 1974, Freshley et al., 1978, and Small, 1987) were obtained.

Figure 2.70 compares the predicted densification values to the experimental values from the data used to tune the model and from more recent data. In general, the model predicts the correct densification trends. However, there is a considerable amount of scatter in the densification data. In addition, FRAPCON-3.3 is not typically used to calculate the densification, but rather the maximum densification is often provided as an input variable to the code.

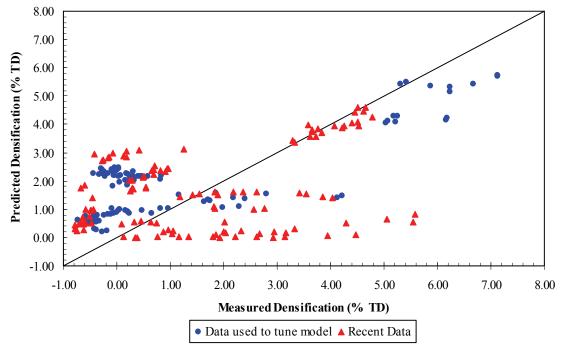


Figure 2.70 Comparison of FUDENS fuel densification predictions to the experimental data from which the fit coefficients were determined and to more recent published data.

Based on this comparison and the fact that maximum densification is typically provided as a code input as recommended by NRC (US NRC Regulatory Guide 1.126, 1978), it can be concluded that FRAPCON-3.3 provides a reasonable estimate of fuel densification.

# 2.5 Assessment of Mechanical Modeling and Properties

This section will discuss the modeling approach that is used in FRAPCON-3.3 and FRAPTRAN 1.3 to model the mechanical responses of the fuel and the cladding. In addition, each model for the mechanical properties of the fuel and cladding will be described and compared to applicable data.

#### 2.5.1 Modeling

Both FRAPCON-3.3 and FRAPTRAN-1.3 use the FRACAS-I finite difference model to calculate the stress and strain in the cladding due to fill gas pressure and pellet-cladding mechanical interaction. In this model, the stress induced deformation in the fuel is neglected and a rigid pellet assumption is used.

The code must account for two different loading conditions. The first occurs when the pellet-cladding gap is open. During this time, the rod internal gas pressure and coolant pressure exert forces on the cladding causing a stress in the cladding. The resultant strain in the cladding due to this stress is calculated by the FRACAS-I model. The second loading condition occurs after the pellet cladding gap is closed due to a combination of fuel swelling, thermal expansion, and cladding creepdown. During this time, the rigid pellet strains the cladding, and the resultant stress in the cladding is calculated by the FRACAS-I model. The FRACAS-I model in

FRAPCON-3.3 and FRAPTRAN-1.3 are described in greater detail by Berna et al. (1997) and by Cunningham et al (2001a).

# 2.5.2 Mechanical Properties

The mechanical properties of primary concern for modeling the stress and strain response of the cladding are irradiation creep, yield stress, and Young's modulus. These properties are discussed in detail and compared to data in the following section.

#### 2.5.2.1 Irradiation Creep

The irradiation creep model in FRAPCON-3.3 is the same model that was in FRAPCON-2. This model is not discussed in the documentation for FRAPCON-3. The model has, however, been documented for FRAPCON-2. This model is summarized below.

$$\dot{\varepsilon} = \frac{2(A1 * A2 * A3)^2}{\varepsilon} \cdot 3600 \cdot 1.1547$$

Where

 $\dot{\varepsilon}$  = creep strain rate, in/in/hr

$$A1 = 5.129 \times 10^{-29} \phi$$

 $\phi$  = fast neutron flux, n/m<sup>2</sup>/s

$$A2 = \exp\left(\frac{-10000}{1.987 \cdot T}\right)$$

T = temperature, K

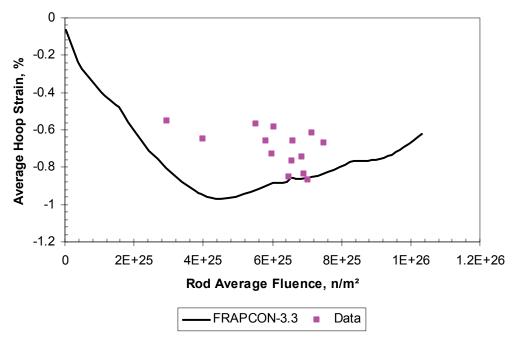
$$A3 = \sigma + 725.2 \exp(4.967 \times 10^{-8} \cdot \sigma)$$

 $\sigma$  = hoop stress, Pa

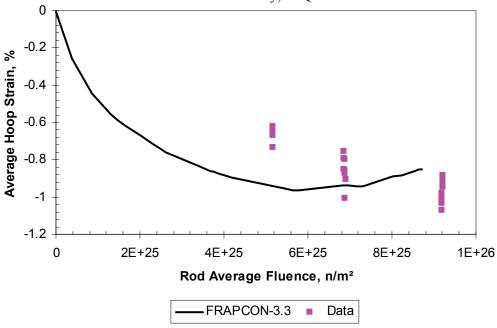
 $\varepsilon$  = creep strain from previous time step, in/in (if  $\varepsilon$  <0.0001, use  $\varepsilon$  =0.0001)

This model is a function of time, stress, fast neutron flux, and temperature. The time and stress dependence is based on Ibrahin (1973). The flux dependence is based on Ross-Ross and Hunt (1968). The temperature dependence is based on a value of q = 10000 cal/mole near 573K from Fidleris (1974).

Lanning et al. (1997b) compared the creep model to measurements from two PWR rod sets (Smith et al., 1994 and Newman, 1986). The results of these comparisons have changed due to the discovery of an error in the code with the calculation of fast neutron fluence. The results of these comparisons for end-of-life creepdown with FRAPCON-3.3 can be seen in Figures 2.71 and 2.72.



**Figure 2.71** Predicted and measured cladding creepdown from the 2<sup>nd</sup> and 3<sup>rd</sup> cycle rods in the ANO-2 PWR assembly, TSQ002.



**Figure 2.72** Predicted and measured cladding creepdown from the 3<sup>rd</sup>, 4<sup>th</sup>, and 5<sup>th</sup> cycle rods in the Oconee PWR assembly, 15309.

It can be seen from these comparisons that the current creep model may predict too high of a creep rate. Several organizations have stated that they believe the cladding creep model in FRAPCON-3.3 predicts creep to occur more rapidly than that normally exhibited. This causes FRAPCON-3.3 to predict gap closure before it might actually occur. A new cladding creep model has been developed to provide a best estimate model for cladding creepdown in FRAPCON-3.4. This model is described in Section 3.7.

There currently is no thermal creep model in FRAPCON-3.3 or FRAPTRAN 1.3. The impact of this lack of thermal creep is that stress relaxation due to thermal creep strain is not calculated. The new model described in Section 3.7 contains a thermal term. The impact of this inclusion will be discussed more in Section 3.7.

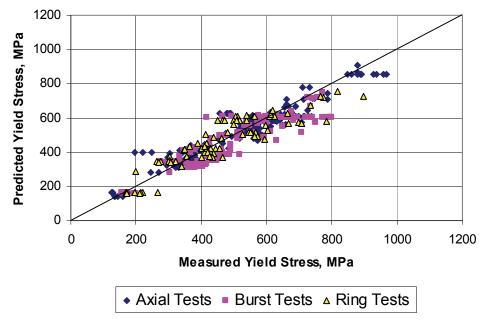
It should be acknowledged that many fabrication parameters can affect the irradiation creep in Zircaloy cladding. Because of this, different cladding vendors should have an irradiation creep model that accurately predicts cladding irradiation creep in cladding manufactured by their supplier.

FRAPTRAN-1.3 does not contain an irradiation creep model. This is acceptable because irradiation creep is a fast neutron fluence-related phenomena and no significant fluence accumulates over the time periods of the events that are modeled in FRAPTRAN-1.3.

## 2.5.2.2 Yield Strength

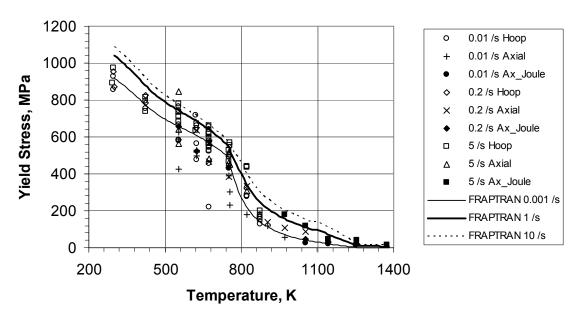
The plastic stress/strain relationship in FRAPTRAN and FRAPCON-3 is given by a power law relationship. The yield stress is the point where the plastic curve, represented by a power law relationship, intersects with the elastic curve, represented by a linear relationship. The coefficients used in the power law are a function of temperature, fast neutron fluence, cladding cold work, strain rate, and cladding type. These coefficients have been modified from those provided in MATPRO to provide a best-estimate prediction of yield stress and ultimate tensile strength from axial tube tensile tests and burst tests taken on irradiated cladding. The model used in FRAPCON-3.3 and FRAPTRAN-1.3 assumes the cladding behaves isotropically and is described in the release document for FRAPTRAN-1.3 (Geelhood, 2005a).

PNNL has compiled a large database of mechanical properties for irradiated and unirradiated Zircaloy-2 and Zircaloy-4 with fast neutron fluence levels up to  $12x10^{25}$  n/m<sup>2</sup>. Figure 2.73 shows the predicted yield stress as a function of the measured yield stress for these data. It can be seen from this figure that the model provides a best-estimate prediction of the cladding yield stress for Zircaloy-2 and Zircaloy-4.



**Figure 2.73** Predicted vs. measured yield stress from irradiated and unirradiated Zircaloy-2 and Zircaloy-4

In addition to these data, there has been data from the PROMETRA program that has been irradiated up to about  $8x10^{25}$  n/m<sup>2</sup>. These data, and the model predictions for three different strain rates are shown in Figure 2.74. It can be seen from this figure that the model accurately predicts the strain rate dependence as well as the yield stress at very high temperature.



**Figure 2.74** Measured and predicted yield stress for high burnup cladding from the PROMETRA database.

Based on these comparisons, it can be seen that the cladding yield stress model in FRAPCON and FRAPTRAN provides a best-estimate prediction of yield stress over a wide range of temperature, fluence, cold work, and strain rate.

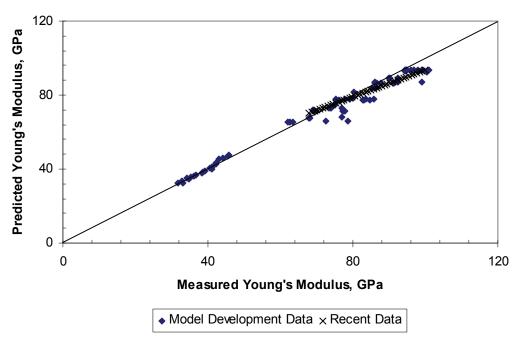
# 2.5.2.3 Young's Modulus

The model for Young's modulus of cladding material in FRAPCON-3.3 and FRAPTRAN-1.3 is the CELMOD model from MATPRO. This model is a function of temperature, cladding cold work, fluence and oxygen concentration and assumed the Zircaloy cladding behaves isotropically.

This model is based on data taken using the dynamic method from several different sources on unirradiated cladding (Bunnell, 1977, Armstrong and Brown, 1964, Padel and Groff, 1976, Busby, 1966, Spasic, 1968, Mehan, 1958, and Northwood, 1975). No Young's modulus data was available for irradiated cladding, so data from the Saxton Core II Fuel Performance Evaluation (Smalley, 1971) was used to estimate the effects of fast neutron fluence.

A search was performed to find more recent Young's modulus data. No data was found for irradiated Zicaloy, but one data source (Bolmaro, 1988) was found for unirradiated Zircaloy.

Figure 2.75 shows the predicted vs. measured values of Young's modulus for the data used for model development and the more recent data. It can be seen from this figure that the model in FRAPCON-3.3 and FRAPTRAN-1.3 continues to provide a best-estimate prediction of Young's modulus for Zircaloy cladding. The model may slightly underpredict Young's modulus for measured modulus of greater than 90 MPa. These measurements are taken at room temperature and are not relevant for fuel performance modeling.



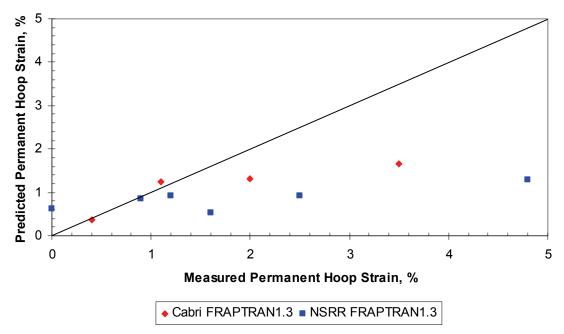
**Figure 2.75** Measured vs. predicted Young's modulus for model development data and recent data

# 2.5.3 Assessment of Power Ramped Rods

Power ramps that can be modeled in FRAPCON-3.3 are typically not severe enough to induce any permanent deformation due to plastic slip. Typically in FRAPCON-3.3, permanent deformation is due to cladding creep. However, the models for the elastic and plastic stress and strain relationships in FRAPCON-3.3 are identical to those in FRAPTRAN-1.3. Because of this,

the plastic deformation models in both FRAPCON-3.3 and FRAPTRAN-1.3 can be assessed based on the results from fast transients modeled in FRAPTRAN-1.3.

During a reactivity initiated accident (RIA), the fuel is heated at a rapid rate and expands against the cladding. During this type of accident, the fuel causes plastic deformation in the cladding in both the hoop direction and the axial direction. RIA accidents have been simulated in the Cabri reactor (Papin, et al, 2003) and in the NSRR reactor (Fuketa et al., 1997, Fuketa et al., 2001, Nakamura et al, 2002). Many have been simulated with FRAPTRAN-1.3, and the permanent strain predictions have been compared to the measured permanent strain. Figure 2.76 shows the predicted and measured hoop strain for the non-failed rods that have been modeled with FRAPTRAN-1.3. It can be seen that FRAPTRAN-1.3 does a good job of predicting the hoop strain when the permanent strain is below about 1.5%. However, at higher strain values, FRAPTRAN-1.3 underpredicts the measured permanent hoop strain. Some of this underprediction may be due to an underprediction of cladding temperature due to departure from nucleate boiling (DNB) occurring in the NSRR tests with stagnant water that cannot be modeled in FRAPTRAN-1.3 due to geometric complexities of the test capsule.



**Figure 2.76** Predicted and measured permanent hoop strain from Cabri and NSRR RIA tests.

Figure 2.77 shows the predicted and measured axial strain for the non-failed rods that have been modeled with FRAPTRAN-1.3. It can be seen that FRAPTRAN-1.3 overpredicts the axial strain for these rods. This is because in FRAPTRAN-1.3, when the fuel and cladding come in contact, they are assumed to be locked up radially and axially with each other. In reality, the fuel and cladding may slip axially in reference to one-another as the pellets expand. A finite element analysis (FEA) model that allows axial slip has been developed and included in FRAPTRAN 1.4 based on the recommendations of several assessment studies (Geelhood, 2005b, Geelhood, 2006). In addition, a representative friction coefficient between the pellet and the cladding will be developed to improved these predictions of axial strain. The final assessment and recommendations will be included in the FRAPCON-3.4/FRAPTRAN 1.4 release documents.

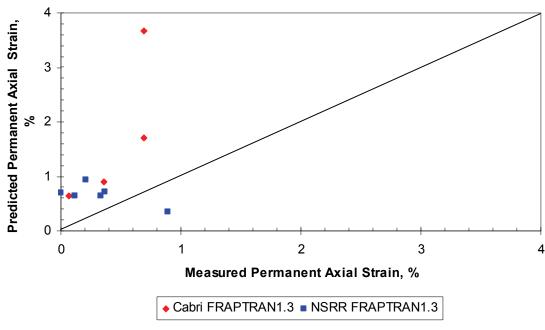


Figure 2.77 Predicted and measured permanent axial strain from Cabri and NSRR RIA tests.

## 2.6 Void Volume Model and Assessment

The rod void volume is primarily affected by the rod growth model and the fuel swelling model. This model and the plenum gas temperature model affect the gas pressure calculation. The rod growth model and plenum gas temperature models will be discussed in the sections below and compared to applicable data.

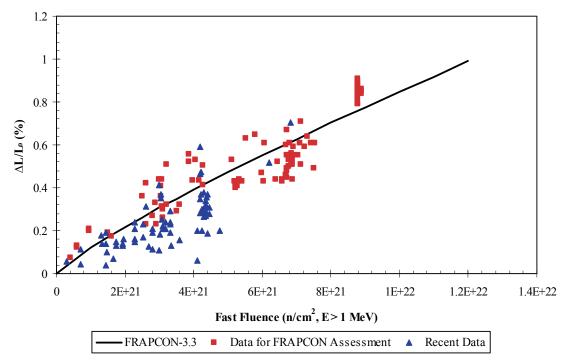
#### 2.6.1 Rod Growth

The cladding axial growth model in FRAPCON-3.3 has been updated from the CAGROW model documented in MATPRO. The updated model is documented in Lanning et al. (1997a). This model is a modified version of a model developed by Franklin (Franklin 1982). There is no axial growth model in FRAPTRAN-1.3 because cladding axial growth is a fluence (burnup) dependant phenomenon and there is no significant fluence accumulation over the time periods of the events that are modeled in FRAPTRAN-1.3. The model is reduced by a factor of 2 (half its size) for modeling BWR cladding, as the data shows a reduction of growth in BWR cladding. This is most likely due to the fact that most BWR cladding is recrystallized Zircaloy-2, while most PWR cladding is stress relieved Zircaloy-4. This model is valid for these two alloys. No comparison has been made for ZIRLO<sup>TM</sup> and M5<sup>TM</sup>. To model these two newer alloys, PNNL recommends using the PWR model for ZIRLO<sup>TM</sup> (stress-relief annealed) and the BWR model for M5<sup>TM</sup> (recrystallized).

The axial growth model in FRAPCON-3.3 is based on data obtained from post-irradiation examination (PIE) data resulting from experiments conducted by Combustion Engineering (CE) and Westinghouse (W) in five different PWRs (Franklin, 1982). The cladding material was coldworked stress relieved Zircaloy-4. Lanning et al. (1997a) compared the FRAPCON-3.3 model to PWR cladding growth data from six different irradiation experiments (Newman, 1986, Balfour, 1982a, Dideon, 1983, Smith, 1986, Smally, 1974, and Smith, 1983) and BWR cladding growth data (West et al., 1983 and Barner, 1990) from two irradiation experiments.

A search was performed for cladding axial growth data published recently. One data source was found (Gilbon, 2000), and more data was found in a Franklin paper (Franklin, 1982).

Figure 2.78 provides a comparison of the FRAPCON-3.3 model for PWR cladding to the data on which it is based and to the more recent PWR data. Figure 2.79 provides a comparison of the FRAPCON-3.3 model for BWR cladding to the data on which it is based and to the more recent BWR data.



**Figure 2.78** FRAPCON-3.3 model for axial growth in PWR cladding compared to data used for model development and recent data

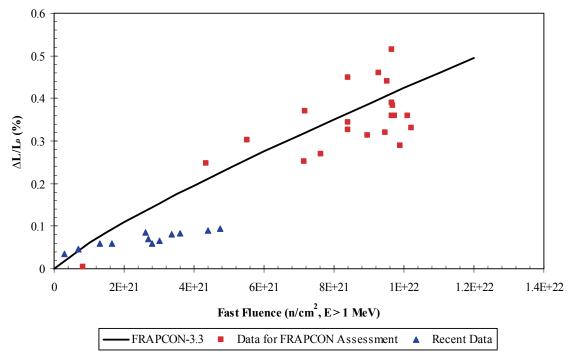


Figure 2.79 FRAPCON-3.3 model for axial growth in BWR cladding compared to data used for model development and recent data

It can be seen from these figures that the FRAPCON-3.3 model for cladding axial growth continues to provide a best-estimate prediction of cladding axial growth for PWR (stress relief annealed (SRA) Zircaloy-4) and BWR (recrystallized annealed RXA Zircaloy-2) cladding.

# 2.6.2 Plenum Gas Temperature

Since about 50-80% of the free volume of a fuel rod is contained in the upper plenum region, it is important for the gas pressure calculation to provide an accurate prediction of plenum gas temperature.

In FRAPCON-3.3, the gas temperature is calculated by calculating the heat transfer to the plenum gas from the end pellet, the hold-down spring, and the coolant. Gamma heating in the spring is considered in this calculation, but gamma heating in the cladding is not.

In FRAPTRAN-1.3 there are two options available for calculating plenum gas temperature. The first option is to assume that the plenum gas temperature is 10K greater than the coolant temperature at the top axial node based on the results of more detailed calculations. The second option is to employ a detailed calculation similar to the calculation performed in FRAPCON-3.3. However, in FRAPTRAN-1.3, the calculation accounts for gamma heating in the cladding.

All of these methods have provided reasonable and not widely disparate estimates of the plenum gas temperature in the past, and are judged to be acceptable for providing a best-estimate calculation of plenum gas temperature.

# 2.7 Time Dependent Models

In order to be consistent with each other, the two fuel performance codes, FRAPCON-3.3 and FRAPTRAN 1.3 use the same set of material properties and models when appropriate. Since FRAPCON-3 is a steady state code, changes that occur over the time period of milliseconds to minutes are not considered. However, FRAPTRAN is specifically designed to calculate changes in temperature and other parameters over such short intervals of time.

Because of this, there is some concern that the material properties or other models used to calculate the behavior of the fuel and cladding may not change instantly when the temperature of the material changes. An example of this would be a material property that requires some atom diffusion to occur when the temperature changes such as the cladding annealing or hydrogen solubility models.

The material properties of the fuel and cladding can be divided into 3 categories. (1) Those without time dependence that can be included in FRAPTRAN as given, (2) those with time dependence that can change over short time intervals (e.g. < 10 minutes) and should include a time dependence term in FRAPTRAN, and (3) those with a time dependence much greater than the time interval that is typically modeled in FRAPTRAN and can be ignored completely in FRAPTRAN. Tables 2.1-2.3 list the properties of fuel and cladding in their appropriate categories.

 Table 2.1
 Properties and models without time dependence

Property	Use		
Young's modulus	Calculate stress/strain behavior		
Thermal conductivity	Calculate flow of heat through fuel, gas,		
·	cladding and oxide		
Thermal expansion	Calculate size of fuel and cladding at various		
	temperature		
k, m, and n	Coefficients used to calculate plastic		
	stress/strain behavior		

**Table 2.2** Properties and models with time dependence that can change over short time intervals (e.g. < 10 minutes) and should be modeled in FRAPTRAN

Property	Use		
Zircaloy annealing	Calculate effective fluence and cold work as a		
	function of time and temperature for		
	mechanical properties, E, k, m, and n.		
Power law for plastic stress/strain behavior and	Calculates yield stress and plastic stress/strain		
thermal creep	behavior as a function of E, k, m, n, and strain		
	rate. Thermal creep not currently modeled in		
	FRAPCON-3.3		
Release of fission gas from grain boundary due	Calculate amount of fission gas residing on the		
to cracking	grain boundary to be released to the rod void		
	volume		
Hydrogen dissolution and precipitation	Used to calculate the excess hydrogen content		
	that is used to calculate failure strain		
Fuel melting	Calculates volume change due to melting		

**Table 2.3** Properties and models with time dependence much greater than the time period modeled in FRAPTRAN

Property	Use		
Fuel Relocation	Calculates size of irradiated pellet due to		
	relocation		
Recovery of fuel relocation	Percentage of fuel relocation to be recovered		
	upon gap closure		
Release of fission gas from grains to grain	Calculates amount of fission gas inside the		
boundaries	grains that is released to the grain boundaries		
Fuel swelling and densification	Calculates size of fuel pellet as a function of		
	burnup		
Cladding irradiation creep	Calculates creep induced in the cladding due to		
	irradiation and external stress		
Cladding irradiation growth	Calculates axial growth induced by irradiation		
	in the cladding		

The following section will examine each of these three types of properties and explain why each property is in this category and how the property is treated or should be treated in FRAPTRAN.

# 2.7.1 Properties and Models without time dependence

#### Young's Modulus

The Young's modulus is governed by the strength of inter-atomic forces. These forces are a function of the lattice temperature and are not expected to have any time dependence. Of course, during a transient, the local temperature will not immediately reach the steady-state temperature, but FRAPTRAN divides the fuel and the cladding into many radial nodes, and uses a transient temperature calculator to calculate the local temperature at each radial node. Given the local temperature as calculated by FRAPTRAN, it is not expected that the Young's modulus will have any time dependence.

There is the possibility of annealing changing the crystal structure by removing the effect of cold work and irradiation defects. The model for Young's modulus in FRAPTRAN is a function of cold work and fast neutron fluence. A separate annealing model calculates effective values of cold work and fast neutron fluence that are used as input to this model.

#### Thermal Conductivity

The fuel thermal conductivity of the fuel in FRAPTRAN is composed of two terms. The first is a phonon term that describes the heat transfer in the solid by lattice vibration. The ability of a lattice to transfer heat is not a function of time at temperature unless a phase change is expected. The extent of irradiation damage is a function of fluence and temperature, and impacts phonon heat transfer. FRAPCON-3.3 and FRAPTRAN 1.3 assume instantaneous change in the irradiation damage when the temperature changes such as a temperature transient but this is most likely not correct because the higher temperature will anneal the damage. In reality, the annealing of damage is most likely time dependent. There are some thermal diffusivity data that are measured above the irradiation temperature that may provide some information on how to model this damage as a function of time. The second term is an electronic term that describes

heat transfer by electrons. This term is not expected to have any time dependence of a rapid change with temperature.

## Thermal Expansion

Thermal expansion in both the fuel and the cladding is a function of the crystal lattice constant increasing due to increased temperature changing the inter-atomic bond energies. This change in lattice constant manifests itself as a macroscopic swelling of the material. There is no delay between the increase in temperature and the macroscopic swelling in the fuel or the cladding.

#### k, m, and n

The strength coefficient, k, strain rate exponent, m, and strain hardening exponent, n are used to determine the stress, strain behavior of the cladding. These coefficients are a function of temperature, cold work, fast neutron fluence, and alloy type. Although the effective cold work and fluence effects (due to irradiation damage) can change, this is modeled in the annealing model, and the stress strain correlation has strain rate dependence in it, the equations for k, m, and n should not change with time for a given set of temperature, cold work and fast neutron fluence.

# 2.7.2 Properties and models with time dependence that can change over short time intervals (e.g. < 10 minutes) and should be modeled in FRAPTRAN

## Zircaloy annealing

The current versions of both FRAPCON-3 and FRAPTRAN contain a Zircaloy annealing model. The mechanical properties in FRAPCON-3 and FRAPTRAN are a function of both cold work and fast neutron fluence. The effects that these parameters have on the mechanical properties of Zircaloy are reduced when the cladding temperature increases during a transient. In addition, the time at temperature affects the degree to which these effects are reduced. The annealing model in FRAPCON-3 and FRAPTRAN is the 'CANEAL' model from MATPRO-11. This model calculates effective values for the cladding cold work and fast neutron fluence based on the temperature history that the cladding has seen. In this way, the time dependence of temperature on cladding mechanical properties is accounted for.

The current annealing model is based on limited data. However, there is not currently significantly more data on cladding annealing. If more data become available, this model will be re-examined.

# Power law for plastic stress/strain behavior

The stress strain behavior of zirconium alloy cladding is affected by the strain rate as well as the cold work and neutron fluence. For example, it has been observed that the yield stress and ultimate tensile strength of irradiated Zircaloy is about 15% greater during tests at high strain rates such as 1-10 in/in/s than during tests at lows strain rates such as  $10^{-5}$  in/in/s.

FRAPTRAN calculates the strain rate in the cladding based on the strain rate from the previous time step. The power law that relates plastic stress and strain is a function of strain rate. In this way, the strain rate is accounted for in the cladding stress/strain behavior.

# Release of fission gas from grain boundary

Fission gas that is accumulated on the grain boundary can be released to the rod void volume if the fuel temperature were to increase rapidly. This is of particular concern for RIA accidents, where it has been observed that fission gas release on the order of 5-20% is observed over a time period of less than 1 second.

Currently, FRAPTRAN 1.3 has no transient fission gas release model. However, a new model has been developed for FRAPCON-3 that can be used to predict how much gas is on the grain boundaries, in addition to how much gas has been released during normal operation. A transient gas release model is under development that can use the gas on the grain boundary to predict how much gas will be released during a power transient. The release of grain boundary gas is expected to be nearly instantaneous with the temperature increase due to cracking and/or grain boundary separation. Additional diffusion of gas to the grain boundary is not expected over the time periods (< 10 minutes) modeled in FRAPTRAN.

# Hydrogen dissolution and precipitation

FRAPTRAN-1.3 contains a strain based failure model that is used for cladding failure due to PMCI at temperatures below 700K. This model is used to predict failure during RIA-type accidents. This model is a function of temperature and excess hydrogen in the cladding. During a RIA, the cladding temperature is rapidly heated up within less than a second. The rate of change in excess hydrogen is such that the level of hydrogen in the cladding does not change appreciably over such a short time period. Because of this the steady state (equilibrium) value of hydrogen solubility that increases as the cladding temperature increases should not be used to predict the excess hydrogen in the cladding for this transient. A rate dependent dissolution (Kearns 1968) and precipitation (Une et al. 2003) model of hydrogen in Zircaloy is included in FRAPTRAN-1.3, so that the excess hydrogen content can be determined as a function of time and temperature during heat-up of the cladding on the order of several seconds or minutes.

#### Fuel melting

As energy increases in the fuel and the temperature reaches the fuel melting point, the heat of fusion must be absorbed by the fuel before the fuel temperature will continue to increase. This will cause a delay in the fuel temperature as a function of energy deposited that must be modeled in FRAPTRAN. In FRAPTRAN-1.3, when the fuel reaches the fuel melting temperature, the fuel temperature is held at the melting temperature until the fuel absorbs the heat of fusion. During the period of time that the fuel is absorbing the heat of fusion, the code calculates the volume fraction of fuel that is molten and the volume fraction that is solid. This volume fraction is used to determine the fuel thermal expansion of the pellet given the two phase composition and the volume change associated with fuel melting.

# 2.7.3 Properties and models with time dependence much greater than the time period modeled in FRAPTRAN

#### **Fuel Relocation**

Fuel relocation is the term used to describe the cracking that occurs in a pellet as it expands and cracks and becomes larger than the solid pellet had been. This process is modeled in FRAPCON-3 as a power and burnup dependent phenomenon for the first 5 GWd/MTU of operation and remains constant for higher burnup. This model is based on beginning of life fuel temperature measurements taken in the Halden reactor.

Because burnup accumulation is not modeled in FRAPTRAN the evolution of relocation is not modeled in FRAPTRAN. FRAPTRAN uses a simplification of the FRAPCON-3 model. For unirradiated fuel, the relocation is assumed to be 30% of the gap size. For irradiated fuel, the relocation is assumed to be 45% of the gap size. If FRAPCON-3 is used to initialize FRAPTRAN, the relocation calculated in FRAPCON-3 for a burnup dependent case is passed to FRAPTRAN as a pellet strain and the simplified model discussed above is ignored.

#### Recovery of fuel relocation

In FRAPCON-3 when the pellet and cladding come in contact, 50% of the calculated relocation is accommodated back into the pellet, to account for the repacking of some of the fuel fragments. This assumption is based on beginning of life measurements of the onset of cladding axial elongation and Halden squeeze tests on fuel pellets. This accommodation process occurs over some length of time that is assumed to be greater than the time modeled in FRAPTRAN. In FRAPTRAN, hard contact is assumed to occur when the pellet and cladding first come into contact. This assumption was made so that the predicted hoop strains in FRAPTRAN compare well with measured hoop strains from RIA tests.

## Release of fission gas from grains to grain boundaries

Fission gas is produced within the fuel grains and diffuses out of the grains to the grain boundaries. Once these grain boundaries are saturated, the gas on the grain boundaries is released to the rod void. The rate of diffusion of Xe and Kr in  $UO_2$  is such that over the period of < 10 minutes significant diffusion will not occur. Because of this, the transient fission gas release model that will be developed for FRAPTRAN will not consider gas diffusion from the grains. The only source of fission gas for this transient model will be gas that has previously accumulated on the grain boundaries.

# Fuel swelling and densification

Solid fission product swelling and fuel densification happen over a long period of time. These changes are typically on the order of  $\pm$  1 %  $\Delta$ V/V per 10 GWd/MTU (>100 days). Since the period of time that is typically modeled in FRAPTRAN (< 10 minutes) is significantly shorter than this period of time, no fuel swelling or densification is modeled in FRAPTRAN. For a case with burnup dependent properties from FRAPCON-3, the deformed pellet radius from the final time step that includes changes due to densification and solid swelling is input to FRAPTRAN. No further swelling or densification is calculated in FRATPRAN for this case.

Gaseous swelling is not modeled in FRAPCON-3.3 or FRAPTRAN 1.3. Gaseous swelling may be important at high burnups (> 40 GWd/MTU) for high power increases on the order of several minutes at power. Gaseous swelling is diffusion dependent.

#### Cladding irradiation and thermal creep

Irradiation creep in the cladding is a process that causes strain in the cladding as a function of fast neutron flux, time, and temperature. The period of time that is typically modeling in FRAPTRAN (< 10 minutes) is significantly shorter than the time required to get significant irradiation creep. As with the swelling and densification, FRAPTRAN assumes that no irradiation creep occurs. For a case with burnup dependent properties from FRAPCON-3, the deformed cladding radius from the final time step is input to FRAPTRAN. No further cladding creep is calculated in FRAPTRAN for this case.

Thermal creep is not modeled in either FRAPCON-3.3 or FRAPTRAN 1.3 with the exception of cladding ballooning at very high temperature (>750°C) that is modeled in FRAPTRAN 1.3. Cladding ballooning can occur during a LOCA event. Thermal creep is diffusion dependent such that it takes several seconds to hours depending on cladding temperature to be significant. The new creep model that has been developed and implemented in FRAPCON-3.4 contains a thermal creep term. This model is described in Section 3.7.

#### Cladding irradiation growth

Irradiation growth in the cladding is a process that causes axial strain in the cladding as a function of fast neutron fluence. The period of time that is typically modeled in FRAPTRAN (< 10 minutes) is significantly shorter than the time required to get significant growth. As with the cladding creep, FRAPTRAN assumes that no irradiation growth occurs. For a case with burnup dependent properties from FRAPCON-3, the cladding elongation from the final time step is input to FRAPTRAN. No further cladding growth is calculated in FRAPTRAN for this case.

#### 2.7.4 Summary

The material properties and models for the fuel and cladding can be divided into three categories. These categories are; those with out time dependence, those with time dependence that can change over short time intervals (e.g. < 10 minutes) and should include a time dependence term in FRAPTRAN, and those with a time dependence much greater than the time interval that is typically modeled in FRAPTRAN that can be ignored completely in FRAPTRAN. The material properties and models of the fuel and cladding are divided up into each of these categories, and those in the second category have been examined to ensure that they are adequately modeled in FRAPTRAN.

For those material properties and models with time dependence that can change over short time intervals (e.g. < 10 minutes), all are assumed to be correctly modeled in FRAPTRAN, except for grain boundary release of fission gas. A model is currently under development to simulate this behavior. In addition, there are not much data to support the cladding annealing model, but no more is currently available. As more data become available, this model will be re-examined. No gaseous swelling model or thermal creep model exists in FRAPTRAN-1.3 or FRAPCON-3.3. A gaseous swelling model is currently under development. A thermal term has been included in the new creep model described in Section 3.7.

## 2.8 Conclusions

The conclusion of this assessment is that both FRAPCON-3.3 and FRAPTRAN 1.3 provide best-estimate predictions of fuel temperature (see Section 2.1.7), fission gas release (see Section 2.2.2) and cladding stress and strain (see Section 2.5.3). Several individual models have been identified as being biased over certain ranges, but the integral predictions of fuel and cladding temperature and cladding stress and strain in FRAPCON-3.3 and FRAPTRAN 1.3 are best-estimate. The following list includes individual models that have been re-examined, to improve the model's predictive capability in FRAPCON-3.4 and FRAPTRAN 1.4. These model improvements are discussed in Section 3.

- Cladding corrosion: Recent adjustments have been made to simulate corrosion on ZIRLO<sup>TM</sup> and M5<sup>TM</sup>. Some comparisons have shown that this adjustment may not be valid at high burnup for ZIRLO<sup>TM</sup>. This model has been reassessed and made to provide a better fit to ZIRLO<sup>TM</sup> corrosion data.
- BWR cladding hydrogen content: New data show the need for a new model for predicting BWR cladding hydrogen content. A model has been developed to calculate this.
- Radial power profile: The radial power profile should be assessed relative to the expected radial power profile in a HWR and a radial power model has been developed for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> fuel
- Fuel thermal expansion at high temperature: A new model has been developed to better fit the data at high temperature.
- Gas thermal conductivity: The gas conductivity models are not valid for most gasses beyond 1100K and new data are available for new model development. This will not affect most of the temperature predictions since the gas does not typically exceed 1000K. New models have been developed that better predict these data.
- Steam thermal conductivity: The models in both codes have been changed to match the ASME model. This is most important in FRAPTRAN 1.3 where the gap may be filled with steam after cladding rupture.
- Cladding irradiation creepdown: Some evidence indicates that the cladding irradiation creepdown model in FRAPCON-3.3 may predict creepdown to occur too rapidly. This has been assessed and a new irradiation creepdown model has been developed.
- Thermal creep impacts calculation of permanent strains below the yield stress for transients on the order of several minutes to hours. The new creep model contains a thermal creep term.
- Clad-coolant heat transfer models The models for clad-coolant heat transfer in FRAPTRAN were updated. These models are discussed elsewhere (Cuta, 2007).

The following list contains areas where modeling has not been done, but where new modeling capabilities could be added and possibly improve the codes' predictive capabilities.

- Fission gas release: There is no fission gas release model in FRAPTRAN 1.3. Significant gas release has been observed during RIAs. A model should be developed to simulate this release in FRAPTRAN 1.3, and if necessary, the model in FRAPCON-3.3 should be modified to provide initial conditions to this new model.
- Fission gas release: The fission gas release model in FRAPCON-3.3 underpredicts FGR for power ramped rods with hold times less than 4 hours. The model should be modified to account for this. Until this time, PNNL recommends that the hold time be increased by a factor of 3 for power ramp hold times less than 4 hours to conservatively bound the expected fission gas release behavior.

- Gaseous swelling is not modeled and may be important for transient in high burnup fuel lasting several minutes to hours.
- Time dependent change in thermal conductivity due to thermal annealing of irradiation defects during a slow temperature transient.
- Hydrogen pickup from high temperature oxidation not modeled in FRAPTRAN 1.3
- Axial and radial strain predictions in FRAPTRAN 1.3

# 3.0 UPDATES TO MODELS

This section discusses the models that have been found to be biased in Section 2.0 and have been updated to provide a best-estimate fit to the available data. Since these models are new, they will be validated relative to the available data and standard deviation will be calculated relative to the available data. All of these models will be included in the new code versions, FRAPCON-3.4 and FRATPRAN 1.4, when they are released. The release of FRAPCON-3.4 and FRAPTRAN 1.4 will each be accompanied by a document that describes the changes that have been made since the previous version as well as providing the results of the integral assessment comparisons for integral effects such as centerline temperature and rod internal pressure. The integral effects may be impacted by the changes made to models described in this section as well as other changes made since the previous code release. The overall code validation will be performed in the documents accompanying the release of each code.

# 3.1 Corrosion and Hydrogen Pickup in Cladding Alloys

Section 2.3 identified that the corrosion and hydrogen pickup models in FRAPCON-3.3 are deficient in the areas of hydrogen pickup in Zircaloy-2 in BWR conditions, corrosion of ZIRLO<sup>TM</sup> at high burnup, and corrosion of M5<sup>TM</sup> at high burnup. This section will discuss how these models have been changed to provide a best-estimate prediction for these alloys.

# 3.1.1 Hydrogen pickup in Zircaloy-2

The recent data comparison shown in Section 2.3.2 found that a constant hydrogen pickup fraction is not appropriate for hydrogen pickup in Zircaloy-2. In addition, it was found that the hydrogen pickup in new Zircaloy-2 where the vendors have better control over the alloy composition and second-phase precipitate (SPP) size is different from older Zircaloy. Correlations were developed for the hydrogen pickup in older and new Zircaloy-2 as a function of burnup. These correlations are given below.

For older Zircaloy-2:

$$H_{Tot}$$
 47.8 exp $\left(\frac{-1.3}{1+Bu}\right)$  + 0.316 ·  $BU$ 

Where:

 $H_{Tot}$  = total hydrogen, ppm (wt)

BU = local axial burnup, MWd/kgU (only valid to 50 MWd/kgU)

For new Zircaloy-2:

$$H_{Tot} = 22.8 + \exp(0.117(BU - 20))$$

Where:

 $H_{Tot}$  = total hydrogen, ppm (wt)

BU = local axial burnup, MWd/kgU (valid up to 70 MWd/kgU)

It is noted that the correlation for older Zircaloy-2 is only valid to 50 MWd/kgU. This is because there is no data available above 50 MWd/kgU. For older Zircaloy, when the burnup exceeds 50 MWd/kgU, it is recommended that the correlation for newer Zircaloy plus 6.1 (the difference between these correlations at 50 MWd/kgU) be used. FRAPCON-3.4 will be modified to include these equations for hydrogen pickup in Zircaloy-2 cladding under BWR conditions. In addition, a new variable will be added to select between new Zircaloy-2 and older Zircaloy-2.

Figure 3.1 shows the data and the correlations that have been developed for hydrogen pickup in old and new Zircaloy-2 as well as the previous model used in FRAPCON-3.3. The data for the older fuel types is primarily from Japanese reactors. The standard deviation,  $\sigma$ , of this correlation is 9.69 ppm that appears to remain relatively constant up to 45 MWd/kgU. The standard deviation for the correlation for newer Zircaloy-2 can be seen to be burnup dependent with the scatter in the data significantly increasing above a local burnup of 49 MWd/kgU. Therefore, the calculation of standard deviation has been broken into two separate burnup ranges of 0 to 49 MWd/kgU where  $\sigma$  = 10.76 ppm and for burnups between 49 to 65 MWd/kgU where  $\sigma$  = 60.62 ppm. The distribution of the predicted-minus-measured is close to a normal distribution within a given burnup range such that use of normal statistics is assumed to be valid.

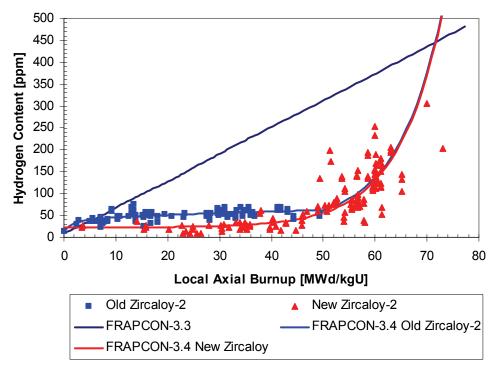


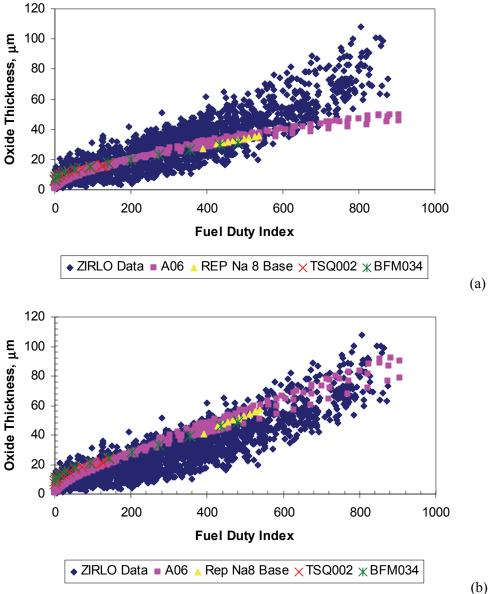
Figure 3.1 Comparison of recent Zircaloy-2 hydrogen pickup data to new correlations for old and new Zircaloy-2 cladding

#### 3.1.2 Corrosion in ZIRLO<sup>TM</sup>

The data comparison in Section 2.3.1 where the ZIRLO<sup>TM</sup> model in FRAPCON-3.3 was compared to two high exposure rods (A06 & A12) (CSN, ENUSA, 2002) found that the model underpredicts oxide thickness at high burnup (>70 GWd/MTU). The model in FRAPCON-3.3 for ZIRLO<sup>TM</sup> had been the same as the model for Zircaloy-4, but the final oxide thickness was reduced by a factor of 2.0 (Lanning et al, 2005a). In order to provide a better fit to the data, the following changes were made to the Zircaloy-4 model for the modeling of ZIRLO<sup>TM</sup>.

- The value used for weight gain from the previous time step was increased by a factor of 2.0.
- The calculated thickness for the current time step was decreased by a factor of 2.0.
- The activation energy for post transition oxidation, Q<sub>2</sub>, was decreased by a factor of 0.99.

Figure 3.2 shows the FRAPCON predictions of oxide thickness as a function of fuel duty index (FDI) using the old model (FRAPCON-3.3) and the new model (FRAPCON-3.4). The FRAPCON-3 predictions are performed for one of the high exposure rods, A06, and for several other typical PWR rods where power history and design information is known that allowed cladding temperatures and fuel duty index (FDI) to be calculated for a given PWR design assuming ZIRLO<sup>TM</sup> cladding. Also shown in this figure is a large quantity of ZIRLO<sup>TM</sup> oxide thickness data (Knott et al., 2003).

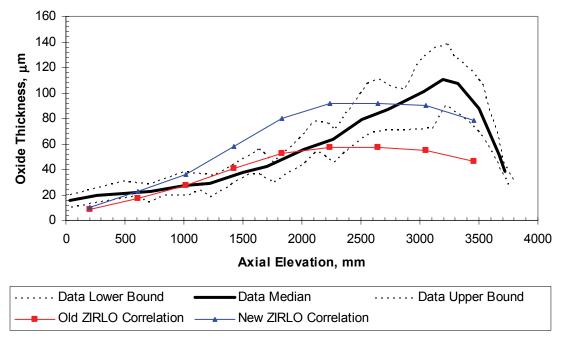


**Figure 3.2** ZIRLO<sup>™</sup> data vs. burnup and (a) FRAPCON-3.3 and (b) FRAPCON-3.4 model predictions for several sample PWR rods

It can be seen from this figure that the model in FRAPCON-3.3 begins to underpredict the oxide thickness by a FDI of 700. However, the new model shows good predictions out to a FDI of 900. It is difficult to calculate the uncertainty of this model as the actual temperature and time for each

data point in Figure 3.2 is not known. However, a standard deviation of 20% is estimated based on the data comparisons seen here and in Figures 3.3 and 3.4.

The new end of life predictions for the high burnup rods, A06 and A12 are shown in Figures 3.3 and 3.4 with the measured oxide thickness at end of life. It can be seen from these figure that the new correlation provide significantly better prediction of the oxide layer thickness for these rods. FRAPCON-3.4 was modified to include these adjustments to the equations for corrosion in ZIRLO<sup>TM</sup> cladding under PWR conditions. With the new ZIRLO<sup>TM</sup>, corrosion model, the hydrogen pickup predictions still predicted the data very well. Therefore, the ZIRLO<sup>TM</sup> was kept the same in FRAPCON-3.4 as it was in FRAPCON-3.3.



**Figure 3.3.** Old and New ZIRLO<sup>TM</sup> model predictions for end of life oxide thickness for rod A06

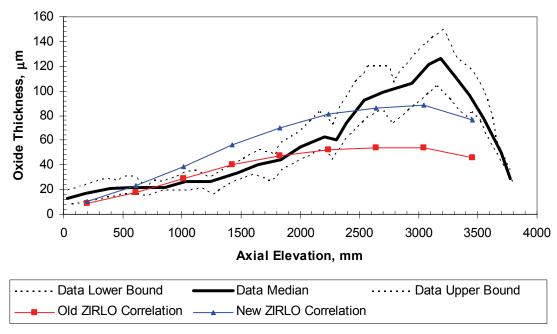


Figure 3.4 Old and New ZIRLO™ model predictions for end of life oxide thickness for rod A12

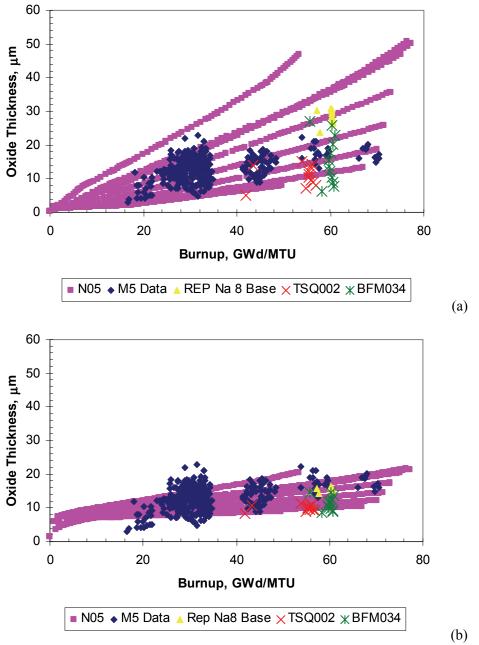
# 3.1.3 Corrosion and Hydrogen Pickup in M5<sup>TM</sup>

The data comparison in Section 2.3.1 where the M5<sup>TM</sup> model in FRAPCON-3.3 was compared to a high exposure rod (N05) (Segura, 2002) found that the model overpredicts oxide thickness at high burnup (>70 GWd/MTU). The model in FRAPCON-3.3 for M5<sup>TM</sup> had been the same as the model for Zircaloy-4, but the final oxide thickness was reduced by a factor of 2.3. In order to provide a better fit to the data, the following changes were made to the Zircaloy-4 model for the modeling of M5<sup>TM</sup>.

- The activation energy for pre transition oxidation,  $Q_1$ , was reduced by a factor of 0.85.
- The onset of post transition oxidation was increase from 2  $\mu$ m to 7  $\mu$ m.
- The activation energy for post transition oxidation, Q<sub>2</sub>, was increased by a factor of 1.09.

Figure 3.5 shows the FRAPCON predictions of oxide thickness as a function of burnup using the old model (FRAPCON-3.3) and the new model (FRAPCON-3.4). The FRAPCON-3 predictions are performed for the high exposure rod, N05, and for several other typical PWR rods assuming M5<sup>TM</sup> cladding. Also shown in this figure is a large quantity of M5<sup>TM</sup> oxide thickness data (Mardon and Waeckel, 2003).

It can be seen from Figure 3.5 that the model in FRAPCON-3.3 began to overpredict the oxide thickness by 30-40 GWd/MTU. However, the new model shows good predictions out to 70 GWd/MTU. It is difficult to calculate the uncertainty of this model as the actual temperature and time for each data point in Figure 3.5 is not known. However, a standard deviation of 20% is estimated based on the data comparisons seen here and in Figure 3.6.



**Figure 3.5** M5<sup>TM</sup> data vs. burnup and (a) FRAPCON-3.3 and (b) FRAPCON-3.4 model predictions for several sample PWR rods

The new end of life predictions for the high burnup rod, N05 are shown in Figure 3.6 with the measured oxide thickness at end of life. It can be seen from this figure that the new correlation provide an excellent prediction of the oxide layer thickness for this rod. FRAPCON-3.4 was modified to include these adjustments to the equations for corrosion in M5<sup>TM</sup> cladding under PWR conditions.

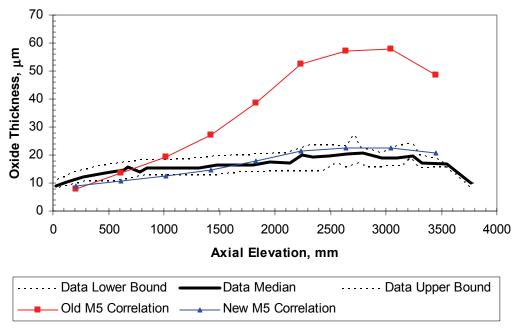
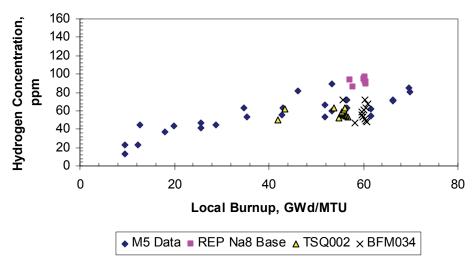


Figure 3.6 Old and New M5<sup>TM</sup> model predictions for end of life oxide thickness for rod N05

In FRAPCON-3.3, the hydrogen pickup fraction for M5 was 7.5%. However, this pickup fraction was based on comparisons to hydrogen concentration data plotted as a function of burnup. Hydrogen concentration is not directly a function of burnup, but rather of oxide thickness and hydrogen pickup fraction. Since the FRAPCON-3.3 model overpredicted oxide thickness, it was reduced as described above. Therefore, in order to get the same hydrogen concentrations at a given burnup, the pickup fraction had to be increased for the new model. A pickup fraction of 10% was found to provide the best fit to these data. Figure 3.7 shows a plot of the hydrogen concentration data with FRAPCON-3.4 hydrogen concentration predictions at end of life at various axial elevations for three typical PWR cases. FRAPCON-3.4 was modified to use a pickup fraction of 10% for hydrogen pickup in M5<sup>TM</sup> cladding under PWR conditions. It is difficult to calculate the uncertainty of this model as the oxide thickness for each data point in Figure 3.7 is not known. However, a standard deviation of 20 ppm is estimated based on the data comparisons seen in Figure 3.7.



**Figure 3.7** Hydrogen concentration data for M5™ and FRAPCON-3.4 predictions of hydrogen for typical PWR cases

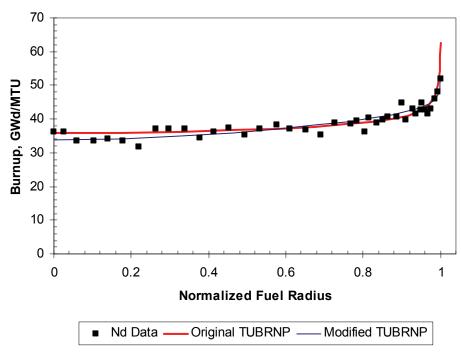
#### 3.2 Radial Power Profile in HWR

The TUBRNP (Lassman et al. 1994) model in FRAPCON-3.3 predicts the radial power profiles within the fuel pellet as a function of uranium and plutonium isotopic concentration and burnup. The version of this subroutine contains one parameter that is modified to account for HWR conditions. The constant  $p_1$  is changed from 3.45 to 2.45 for HWR conditions. Comparison to data and other neutronic code predictions have demonstrated that this adjustment does not correctly account for the differences in heavy water and light water reactor conditions.

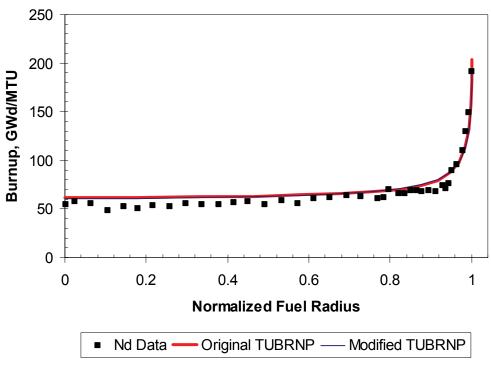
Since the original release of FRAPCON-3, a second paper has been published on the modifications to TUBRNP to correctly model HWR conditions (Lassman et al. 1998). This paper stated that the original TUBRNP model could be modified to be applicable to HWR conditions if the fission and capture cross sections for each uranium and plutonium isotopes were updated based on a HWR neutron spectrum and if the constant p<sub>1</sub> was changed from 3.45 to 2.21. The neutron spectrum in a HWR has relatively more neutrons in the thermal region and relatively fewer neutrons in the fast region. Therefore the spectrum-averaged fission and capture cross sections will be different for LWR and HWR conditions.

Lassman et al. (1998) did not provide the spectrum-averaged cross sections that they used to update this model. The current TRANSURANUS code developers were contacted and the cross section values that are used in TUBRNP for HWR conditions were provided.

The internal version of FRAPCON-3.4 was modified to use the recommended value of p<sub>1</sub> and fission and capture cross sections for HWR conditions. The predictions of this modified version of FRAPCON-3.4 were compared to rods that had electron probe microanalysis (EPMA) data of the fission product, Nd (Lassmann et al., 1998). This fission product is immobile in UO<sub>2</sub> and the concentration of Nd is related to the fission density and thus can be converted to burnup. Figures 3.8 and 3.9 show the original TUBRNP and the modified TUBRNP predictions of radial burnup distribution for two different rod sections irradiated at Halden and DR3.

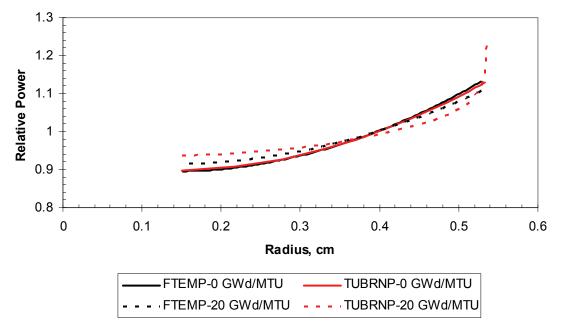


**Figure 3.8** Burnup distribution in rod section F9-3-44 with U-235 enrichment of 5%, irradiated to 39 GWd/MTU in the Halden reactor



**Figure 3.9** Burnup distribution in rod section AF21-2-8 with U-235 enrichment of 1.5%, irradiated to 72.2 GWd/MTU in the DR3 reactor

Figure 3.10 shows a comparison of the predictions of the TUBRNP model for a rod with 7% U-235 irradiated in the Halden reactor compared to the Halden predictions made using FTEMP.



**Figure 3.10** Radial power profile in IFA-558 as predicted by FTEMP and TUBRNP with U-235 enrichment of 7%, irradiated in the Halden reactor

It can be seen from these figures that the modified version of TUBRNP provides slightly better predictions of the edge peaking, particularly for the lower burnup section seen in Figure 3.8. For the comparison in Figure 3.9, the modified version of TUBRNP only provides slightly less edge peaking. It can also be seen that the TUBRNP predictions are almost identical to the FTEMP predictions at beginning of life and similar thereafter. The modified version of TUBRNP was added to FRAPCON-3.4. Based on data comparisons and comparisons to other codes, it can be estimated that the radial power profile model in FRAPCON-3.4 has a standard deviation of about 2.5%. The modified version of TUBRNP will be compared to a more detailed neutronics code (such as WIMS) calculation of radial power in HWR prior to the release of FRAPCON-3.4.

# 3.3 Radial Power Profile in UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub>

Based on the success of using TUBRNP to model the radial power profile for UO<sub>2</sub> and MOX under LWR and HWR conditions, it was thought that if the model was modified to track the neutron absorption and quantity of the neutron absorbing isotopes of gadolinium, Gd-155 and Gd-157 then this model could be used to predict the radial power profile of UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> fuel.

This approach was attempted, but the results predicted by TUBRNP were not reasonable in that they did not match neutronic code predictions done at Halden (Klecha 2005, Volkov et al. 2002) and the centerline temperature predictions in FRAPCON-3 did not match centerline temperature measurements from Halden test rods with centerline thermocouples.

The centerline temperature comparisons for Halden UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> rods shown in Section 2.1.7.2 were performed using the radial power profiles provided by Halden for various burnups and radial positions. A lookup and interpolation routine was used to calculate the radial power for each time step and location in FRAPCON-3. This approach provided good predictions of

centerline temperature for these rods, however, the radial power profiles used here were specific for these rods and the Halden reactor and could not be independently verified.

In order to model the radial power profile for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub>, a typical rod was modeled in WIMS for 0, 2, 4, 6, 8, and 10 wt% Gd<sub>2</sub>O<sub>3</sub> at various burnup levels for LWR and HWR conditions. The results of these calculations were put into FRAPCON-3.4 as a data table and a lookup and interpolation routine was used to calculate the radial power profile. This lookup table is used for burnup values less than 7 GWd/MTU in FRAPCON-3.4. The WIMS calculations for the case with 10 wt% Gd<sub>2</sub>O<sub>3</sub> showed that all the Gd-155 was gone (<0.1%) by about 7 GWd/MTU and all the Gd-157 was gone by about 5 GWd/MTU. Beyond this burnup level, the neutron absorbing isotopes, Gd-155 and Gd-157, have converted to non-neutron absorbing isotopes and the radial power profile is very similar to the radial power profile for UO<sub>2</sub>. For burnup levels greater than 7 GWd/MTU, the TUBRNP model is used to calculate the radial power profile for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub>.

The burnup values output by WIMS do not directly correspond with those in FRAPCON-3. In WIMS, a constant power of 40 MW/MTU (5.73 kW/ft) was used for these calculations. However, in reality, while the gadolinium is burning out in a fuel rod, the power level is much less than this due to neutron absorption by gadolinium. The power level and burnup in WIMS best corresponds to the power level and burnup in the neighboring  $UO_2$  fuel rods. The power profiles provided by WIMS are best described as a function of time. In order to account for this, an effective burnup is calculated in FRAPCON-3.4 to use in the interpolation routine where the burnup increment for each time step is the burnup calculated by FRAPCON-3 times the ratio of 5.73 kW/ft to the actual fuel rod power.

The FRAPCON-3.4 predictions were compared to those made using the radial power profiles calculated by Halden and to the measured temperature data from IFA-636 (Tverberg et al 2005, Volkov et al 2002, Tolonen & Tverberg, 2005) and from IFA-681 (Tolonen & Tverberg, 2005, Tolonen & Andres 2005, Klecha 2005). Plots of these comparisons are shown in Figures 3.11-3.16. It is noted that the measured temperature for IFA-636 Rod 4 (solid pellets) was estimated by Halden from IFA-636 Rod 2 thermocouple measurements. It can be seen from these figures that using the new data table to calculate radial power profile, FRAPCON-3.4 predicts centerline temperature values as well as those using the Halden data tables. It is concluded that the new data table is well within the accuracy of measured rod power and temperatures.

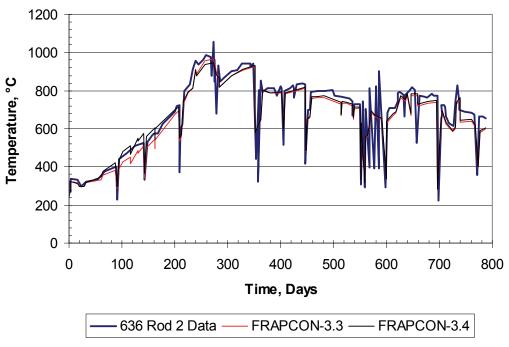


Figure 3.11 Centerline temperature measurements and predictions for IFA-636 Rod 2 with hollow pellets and 8 wt% Gd<sub>2</sub>O<sub>3</sub>. The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

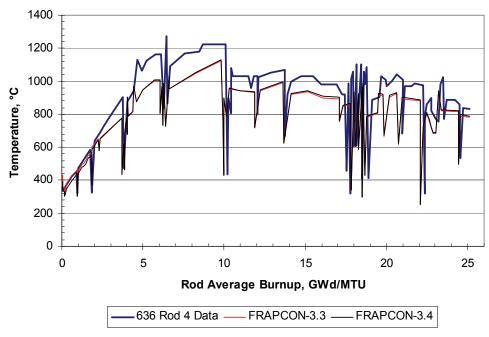


Figure 3.12 Centerline temperature measurements and predictions for IFA-636 Rod 4 with solid pellets and 8 wt% Gd<sub>2</sub>O<sub>3</sub> (Solid pellet temperatures are estimated from measurements made on hollow pellets in IFA-636 Rod 2.) The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

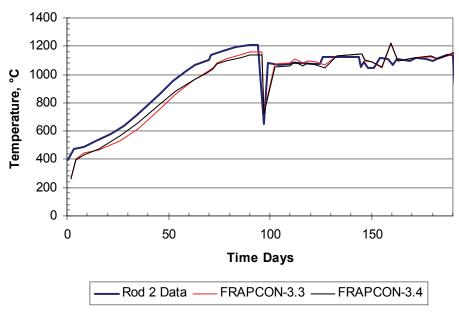


Figure 3.13 Centerline temperature measurements and predictions for IFA-681 Rod 2 with solid pellets and 2 wt% Gd<sub>2</sub>O<sub>3</sub>. The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

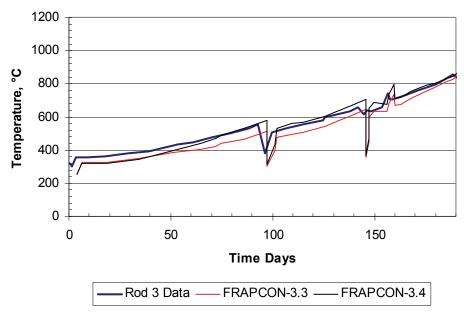


Figure 3.14 Centerline temperature measurements and predictions for IFA-681 Rod 3 with solid pellets and 8 wt% Gd<sub>2</sub>O<sub>3</sub>. The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

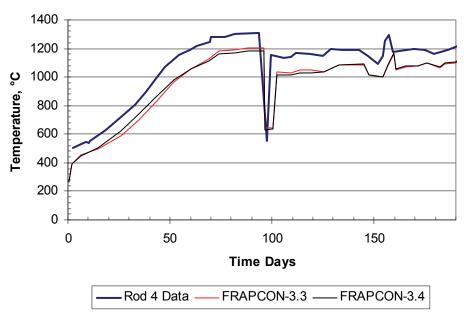


Figure 3.15 Centerline temperature measurements and predictions for IFA-681 Rod 4 with hollow pellets and 2 wt% Gd<sub>2</sub>O<sub>3</sub>. The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

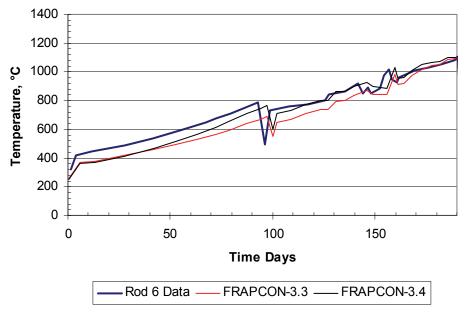


Figure 3.16 Centerline temperature measurements and predictions for IFA-681 Rod 6 with hollow pellets and 8 wt% Gd<sub>2</sub>O<sub>3</sub>. The FRAPCON-3.3 prediction uses the Halden table of radial power profiles. The FRAPCON-3.4 prediction uses the new table of radial power profiles

# 3.4 Fuel Thermal Expansion at High Temperature

The original model in FRAPCON-3.3 and FRAPTRAN 1.3 for UO<sub>2</sub> thermal expansion is given below.

$$\frac{\Delta L}{L_0} = K_1 T - K_2 + K_3 \exp\left(\frac{-E_D}{kT}\right)$$

Where:

$$\frac{\Delta L}{L_0}$$
 = linear strain caused by thermal expansion with a reference of 300K

 $K_1 = 1.0 \times 10^{-5}$ 

 $K_2 = 3.0 \times 10^{-3}$ 

 $K_3 = 4.0 \times 10^{-2}$ 

 $E_D = 6.9 \times 10^{-20}$ 

 $k = 1.38 \times 10^{-23}$ 

This model was found to underpredict data above 2200K in Section 2.1.4. The coefficients in this model were updated to provide a better fit of all the data. The updated coefficients are given below.

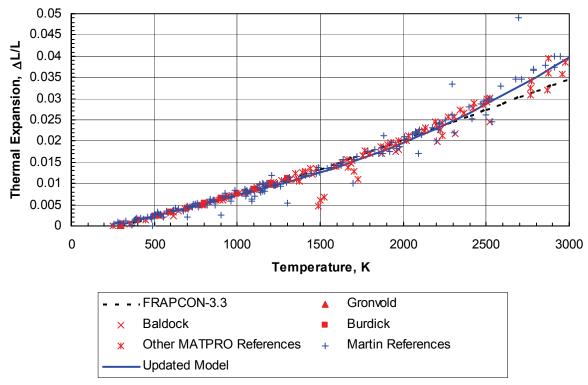
 $K_1 = 9.80 \times 10^{-6}$ 

 $K_2=2.61\times10^{-3}$ 

 $K_3=3.16\times10^{-1}$ 

 $E_D=1.32x10^{-19}$ 

Figure 3.17 shows a plot of the original and the new model with all the available data as a function of temperature. It can be seen that the modified model provides a better fit to the data above 2300K. This new models has been added to FRAPCON-3.4 and FRAPTRAN 1.4. The standard deviation of this model relative to the data in Figure 3.16 is  $0.0015 \Delta L/L$ .



**Figure 3.17** Original and modified UO<sub>2</sub> thermal expansion model with available data as a function of temperature.

# 3.5 Gas Thermal Conductivity at High Temperature

The original model for gas thermal conductivity used in FRAPCON-3.3 and FRAPTRAN 1.3 is given below.

 $k = AT^B$ 

Where:

k = thermal conductivity, W/m-K

T = temperature, K

The coefficients A and B that are used for each gas species is given in Table 3.1.

 Table 3.1
 Original A and B coefficients used in FRAPCON-3.3 and FRAPTRAN 1.3

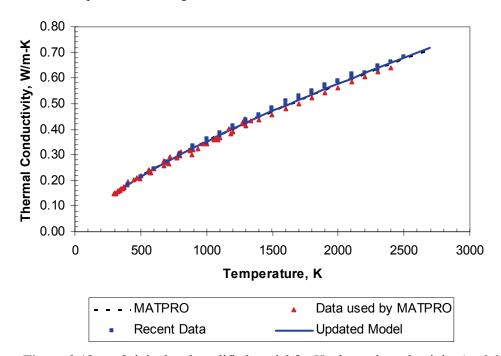
Gas	A	В
Не	$2.639 \times 10^{-3}$	0.7085
Ar	2.986x10 <sup>-4</sup>	0.7224
Kr	8.247x10 <sup>-5</sup>	0.8363
Xe	4.351x10 <sup>-5</sup>	0.8616
$H_2$	1.097x10 <sup>-3</sup>	0.8785
$N_2$	5.314x10 <sup>-4</sup>	0.6898

This model was found to underpredict gas conductivity at high temperature. Because of this the model parameters, A and B were updated to provide a better fit to the data. The updated coefficients for each gas are shown in Table 3.2.

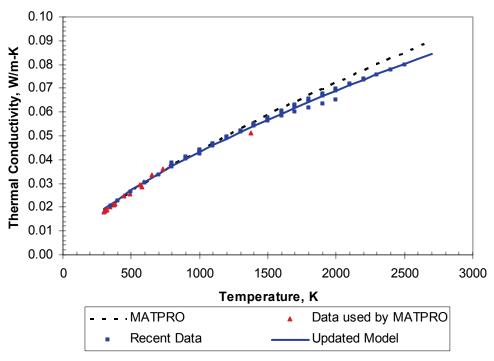
**Table 3.2** Modified A and B coefficients

Gas	A	В
Не	2.531x10 <sup>-3</sup>	0.7146
Ar	$4.090 \times 10^{-4}$	0.6748
Kr	1.966x10 <sup>-4</sup>	0.7006
Xe	9.825x10 <sup>-5</sup>	0.7334
$H_2$	1.349x10 <sup>-3</sup>	0.8408
$N_2$	2.984x10 <sup>-4</sup>	0.7799

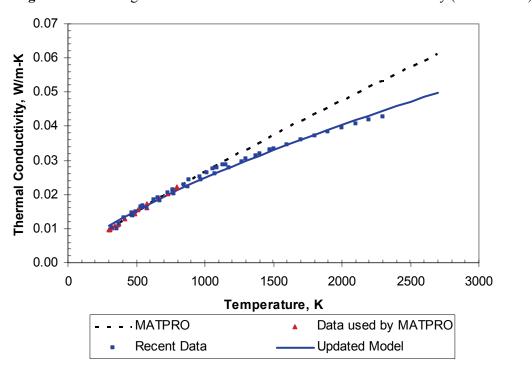
Figures 3.18-3.23 show plots of the original and the new models with all the available data as a function of temperature. It can be seen that the modified models provides a better fit to the high temperature Ar, Kr, Xe,  $H_2$  and  $N_2$  data. These updated models have been added to FRAPCON-3.4 and FRAPTRAN 1.4. The standard deviation for each of these models relative to the data is stated in the caption for each figure.



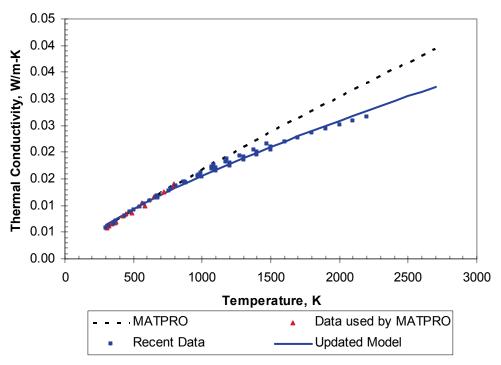
**Figure 3.18** Original and modified model for He thermal conductivity ( $\sigma$ =0.00899)



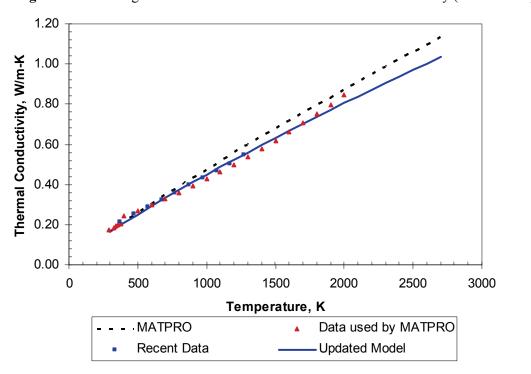
**Figure 3.19** Original and modified model for Ar thermal conductivity ( $\sigma$ =0.000966)



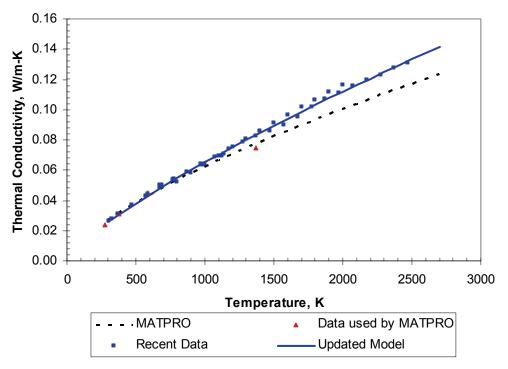
**Figure 3.20** Original and modified model for Kr thermal conductivity ( $\sigma$ =0.000886)



**Figure 3.21** Original and modified model for Xe thermal conductivity ( $\sigma$ =0.000534)



**Figure 3.22** Original and modified model for  $H_2$  thermal conductivity ( $\sigma$ =0.0167)



**Figure 3.23** Original and modified model for  $N_2$  thermal conductivity ( $\sigma$ =0.000197)

# 3.6 Steam Conductivity

The steam conductivity model in FRAPCON-3.3 is

$$k_{steam} = 1.76 \times 10^{-4} + 5.87 \times 10^{-5} (T - 273.15) + 1.04 \times 10^{-7} (T - 273.15)^{2} - 4.51 \times 10^{-11} (T - 273.15)^{3}$$

Where:

 $k_{steam}$  = the steam conductivity, W/m-K T = the gas temperature, K.

The steam conductivity model employed in FRAPTRAN-1.3 for temperatures less than or equal to 973.15K is

$$k_{steam} = \left(-2.8516 \times 10^{-8} + 9.424 \times 10^{-10} T - 6.005 \times 10^{-14} T^2\right) \frac{p}{T} + \frac{1.009 p^2}{T^2 \left(T - 273.15\right)^{4.2}} - 8.4083 \times 10^{-3} - 1.19998 \times 10^{-5} T - 6.706 \times 10^{-8} T^2 - 4.51 \times 10^{-11} T^3$$

Where:

p = gas pressure, Pa.

For temperatures above 973.15K, the model employed in FRAPTRAN-1.3 is

$$k_{steam} = 4.44 \times 10^{-6} T^{1.45} + 9.45 \times 10^{-5} \left( \frac{2.1668 \times 10^{-9} p}{T} \right)^{1.3}$$

The steam conductivity model in MATPRO is

$$k_{steam} = \left(-2.8516 \times 10^{-8} + 9.424 \times 10^{-10} T - 6.005 \times 10^{-14} T^{2}\right) \frac{p}{T} + \frac{1.009 p^{2}}{T^{2} (T - 273)^{4.2}} + 17.6 \times 10^{-4} + 5.87 \times 10^{-5} (T - 273) + 1.08 \times 10^{-7} (T - 273)^{2} - 4.51 \times 10^{-11} (T - 273)^{3}$$

for temperatures less than or equal to 973.15K, and

$$k_{steam} = 4.44 \times 10^{-6} T^{1.45} + 9.5 \times 10^{-5} \left( \frac{2.1668 \times 10^{-9} p}{T} \right)^{1.3}$$

for temperatures above 973.15

The models in FRAPCON-3.3, FRAPTRAN-1.3 and MATPRO were compared to the ASME adopted value of steam conductivity at 10<sup>7</sup> Pa. These comparisons are shown in Figure 3.24. It can be seen from this figure that the MATPRO model predicts the conductivity well, while the models in FRAPCON-3.3 and FRAPTRAN 1.3 do not. Because of this, the model described above was used for steam conductivity in both FRAPCON and FRAPTRAN.

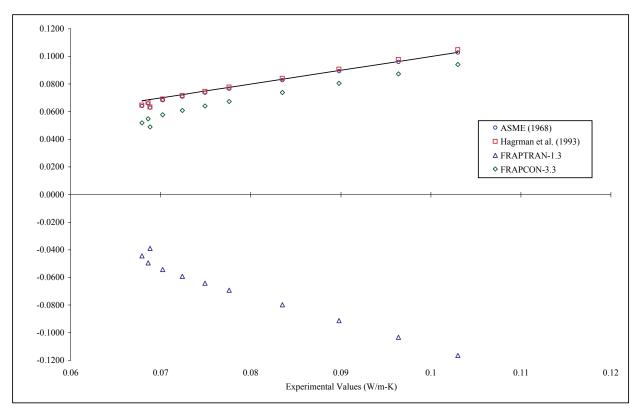


Figure 3.24 Comparison of low temperature steam conductivity models from MATPRO, FRAPTRAN-1.3, and FRAPCON-3.3 with adopted values of experimental data from ASME.

This updated model has been added to FRAPCON-3.4 and FRAPTRAN 1.4.

#### 3.7 **Cladding Irradiation Creep**

The data comparisons in Section 2.5.2.1 identified that the cladding creep model in FRAPCON-3.3 over-predicts the irradiation creep rate in PWR SRA cladding. In addition, this model is used for both SRA and RXA cladding, despite the observations of different creep behavior between the two types of cladding. A literature search was performed to select a model that provides a bestestimate prediction of cladding irradiation creep for both SRA and RXA cladding tubes.

The model given by Limback and Andersson (Limback et al., 1996) was selected for cladding irradiation creep in FRAPCON-3.4. This model uses a thermal creep model described by Matsuo (1987) and an empirical irradiation creep rate with tuned model parameters that were fit to data set by Franklin et al. (1983). This model was modified by PNNL to use effective stress rather than hoop stress as an input so that the difference in creep behavior during tensile and compressive creep would be modeled correctly. Several of the fitting coefficients were consequently changed to accommodate this modification. In addition, a temperature dependent term was added to the formula for irradiation creep strain rate. This model has different parameters for SRA and RXA cladding types, and provides much more reasonable creep strains in the LWR range of temperature and cladding hoop stresses than the current model in FRAPCON-3.3. This model is described below.

The steady state thermal and irradiation creep rates are given by:

$$\dot{\varepsilon}_{th} = A \frac{E}{T} \left( \sinh \frac{a_i \sigma_{eff}}{E} \right)^n \exp \left( \frac{-Q}{RT} \right)$$

$$\dot{\varepsilon}_{irr} = C_0 \cdot \phi^{C_1} \cdot \sigma_{eff}^{C_2} \cdot f(T)$$

Where

 $\dot{\mathcal{E}}_{th}, \dot{\mathcal{E}}_{irr}$  - thermal and irradiation strain rate, respectively (in/in/hr)

These rates are added together so:

$$\dot{\mathcal{E}}_{th+irr} = \dot{\mathcal{E}}_{th} + \dot{\mathcal{E}}_{irr}$$

The saturated primary hoop strain is given by:

$$\varepsilon_p^s = 0.0216 \cdot \dot{\varepsilon}_{th+irr}^{0.109} \left( 2 - \tanh(35500 \cdot \dot{\varepsilon}_{th+irr}) \right)^{-2.05}$$

The total thermal strain is given by:
$$\varepsilon_{H} = \varepsilon_{p}^{s} \left( 1 - \exp\left(-52 \cdot \sqrt{\dot{\varepsilon}_{th+irr} \cdot t}\right) \right) + \dot{\varepsilon}_{th+irr} \cdot t$$

In FRAPCON-3.4, strain rate is used. Taking the derivative with respect to time of the expression above gives:

$$\dot{\varepsilon}_{H} = \frac{52 \cdot \varepsilon_{p}^{s} \cdot \dot{\varepsilon}_{th+irr}^{\frac{1}{2}}}{2 \cdot t^{\frac{1}{2}}} \exp\left(-52 \cdot \sqrt{\dot{\varepsilon}_{th+irr} \cdot t}\right) + \dot{\varepsilon}_{th+irr}$$

Where:

T – temperature (K)

t – time (hours)

 $\sigma_{\rm eff}$  – effective stress, MPa

 $\phi$  – fast neutron flux, n/m<sup>2</sup>-s

Table 3.3 lists the parameters used in these equations for SRA and RXA cladding types

 Table 3.3
 Parameters for FRAPCON-3.4 creep equation for SRA and RXA cladding

Parameter	Units	Values for SRA Cladding	Values for RXA Cladding
A*	K/MPa/hr	1.08E9*	5.47E8*
E	MPA	1.149E5-59	.9*T
$a_i$	MPa <sup>-1</sup>	650{1-0.56[1-exp(-1.	$4E-27*\Phi^{1.3})]$
		$\Phi$ = fast neutron flu	ence (n/cm²)
n	unitless	2.0	3.5
Q	kJ/mole	201	
R	kJ/mol-K	0.008314	4
$C_0$	(n/m²-s) <sup>-C1</sup> MPa <sup>-C2</sup>	4.0985E-24	1.87473E-24
$C_1$	unitless	0.85	
$C_2$	unitless	1.0	
f(T)*	unitless	T<570K 0.7283	0.7994
		570 <t<625k -7.0237+0.0136t<="" th=""><th>-3.18562+0.00699132T</th></t<625k>	-3.18562+0.00699132T
		T>625K 1.4763	1.1840

<sup>\*</sup>Parameters changed from original Limback equation

The effective stress in the cladding is found using the principal stresses at the midwall radius using the thick wall formula as follows:

$$\sigma_{r} = \frac{P_{i}r_{i}^{2} - P_{o}r_{o}^{2} + \frac{r_{i}^{2}r_{o}^{2}(P_{o} - P_{i})}{r^{2}}}{r_{o}^{2} - r_{i}^{2}}$$

$$\sigma_{t} = \frac{P_{i}r_{i}^{2} - P_{o}r_{o}^{2} - \frac{r_{i}^{2}r_{o}^{2}(P_{o} - P_{i})}{r^{2}}}{r_{o}^{2} - r_{i}^{2}}$$

$$\sigma_{t} = \frac{P_{i}r_{i}^{2} - P_{o}r_{o}^{2}}{r_{o}^{2} - r_{i}^{2}}$$

$$\sigma_{t} = \frac{P_{i}r_{i}^{2} - P_{o}r_{o}^{2}}{r_{o}^{2} - r_{i}^{2}}$$

Where:

P<sub>i</sub> – inner pressure

P<sub>o</sub> – outer pressure

r<sub>i</sub> – inner radius

r<sub>o</sub> – outer radius

r – radius within tube

 $\sigma_r$  – radial stress

 $\sigma_t$  – tangential stress

 $\sigma_l$  – longitudinal stress

The effective stress,  $\sigma_{\text{eff}},$  is then given by:

$$\sigma_{eff} = \sqrt{0.5 \left( (\sigma_l - \sigma_t)^2 + (\sigma_t - \sigma_r)^2 + (\sigma_r - \sigma_l)^2 \right)}$$

This equation has been added to FRAPCON-3.4 for the calculation of creep strain rate. The model predictions were compared to creep data from two PWR rods that were used in the original FRAPCON-3 model assessment (Lanning et al., 1997). The creep predictions using the original creep model in FRAPCON-3.3 and using the modified Limback creep model in FRAPCON-3.4 are shown in Figures 3.25 and 3.26. These data are taken from actual fuel rods at the end of each cycle. However, for these rods, no data was taken at the end of the first cycle. The linear decrease in hoop strain ends when the fuel and cladding come in contact and no further creepdown is possible. It can be seen from these figures that the new cladding creep model provides better prediction of creep than the original creep model in FRAPCON-3.3. Over the range of fluences in which data are available, the new model appears to predict these data well.

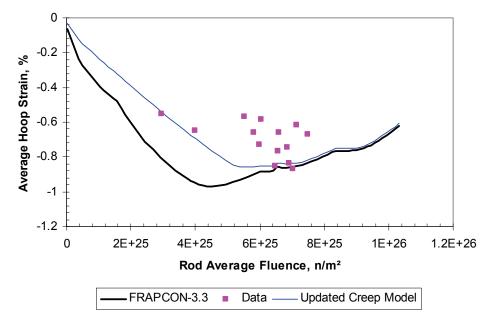
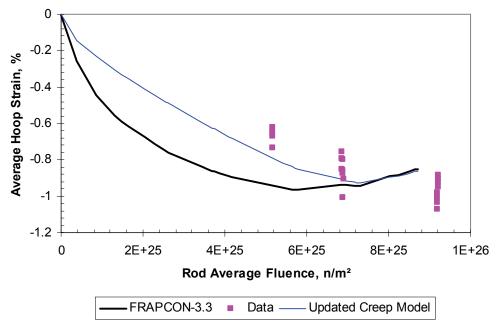
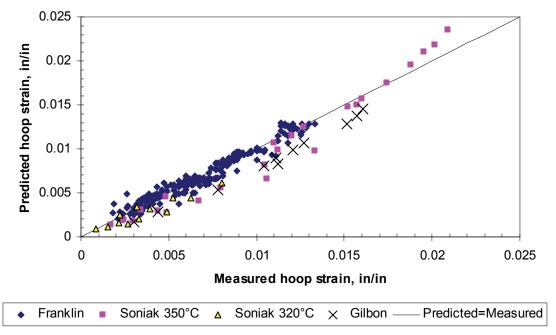


Figure 3.25 Predicted and measured cladding creepdown using the original and new creep models from the 2<sup>nd</sup> and 3<sup>rd</sup> cycle rods in the AN0-2 PWR assembly, TSQ002

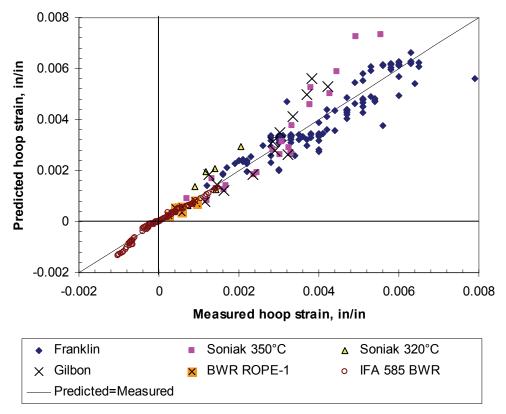


**Figure 3.26** Predicted and measured cladding creepdown using the original and new creep models from the 3<sup>rd</sup>, 4<sup>th</sup>, and 5<sup>th</sup> cycle rods in the Oconee PWR assembly, 15309

Creep data was obtained from irradiated tubes in order to further validate the selected creep model. Data was found on irradiated SRA cladding tubes (Franklin, 1983, Soniak et al., 2002 and Gilbon et al., 2000) and on irradiated RXA cladding tubes (Franklin, 1983, Soniak et al., 2002, Gilbon et al., 2000, and Sontheimer et al., 1994). These data span a temperature range of 570K to 625K, an effective stress range of 40-130 MPa, and a fast neutron flux range of  $1 \times 10^{17} - 2 \times 10^{18}$  n/m²-s that comes the range of LWR fuel rod operation. Figures 3.27 and 3.28 show the results of these predictions. It appears that the uncertainty in Figure 3.28 is increasing with increasing strain. It should be noted however, that the strain values in Figure 3.28 are significantly less than those in Figure 3.27. A relative standard error for the predictions is 14.5% for SRA cladding and 21.6% for RXA cladding. FRAPCON-3.4 will be modified to use the creep model described in this section.



**Figure 3.27** Predicted vs. measured cladding creepdown using the new creep model from creepdown data from irradiated SRA tubes



**Figure 3.28** Predicted vs. measured cladding creepdown using the new creep model from creepdown data from irradiated RXA tubes

# 4.0 Sensitivity Analysis

Material properties modeled in FRAPCON-3.3 include fuel thermal conductivity, fuel thermal expansion, cladding oxide thermal conductivity, cladding thermal conductivity, gas thermal conductivity, fission gas release, cladding corrosion, fuel swelling, thermal and irradiation creep of irradiated cladding, cladding yield strength, Young's modulus of cladding, cladding axial growth, and cladding thermal expansion. By modeling material properties, important fuel rod performance parameters, such as rod internal gas pressure, peak fuel centerline temperature, and cladding permanent (i.e. plastic) hoop strain, can be predicted up to high burnup levels (65 GWd/MTU). These parameters are used for licensing analyses.

Models incorporated in FRAPCON-3.3 are based on both physical and empirical relationships that are continuously compared and adapted to experimental data as it becomes available. Experimental data can exhibit scatter and may be scarce under certain conditions like high burnup or high temperature. Consequently, there is uncertainty in the derived models. In addition to model uncertainty, manufacturing and power history parameters are also sources for uncertainty that may influence the code output. Since fuel performance predictions generated by FRAPCON-3.3 are based on interdependent material response models, manufacturer metrics, and power histories, uncertainty does not propagate linearly to the code output. Nevertheless, the influence of each type of uncertainty can be evaluated by iteratively biasing individual parameters both positively and negatively and comparing the subsequent output with a baseline case. This has been the approach taken by fuel vendors in their fuel performance methodologies that have been approved by NRC. Individual parameters are readily categorized by the three types of uncertainty considered here. Another approach of sampling multiple uncertainties in a Monte Carlo approach could also be used and has been proposed by one fuel vendor (Arimescu, 2008). Prior to applying an approach such as this, it is necessary to know what uncertainties will have an impact on the outputs of interest so those uncertainties can be included in the sampling. In order to determine this a study similar to the study performed below would have to first be performed.

Other researchers have done work to examine the sensitivity of various models and predictions in FRAPCON-3 and FRAPTRAN (Vallejo et al. 2004, del Barrio et al. 2006, del Barrio et al. 2007). These studies provided valuable insight into the sensitivity of these codes to changes in various parameters. This report will show the sensitivity of selected model uncertainties, manufacturing uncertainties, and power uncertainties on the code prediction of rod internal gas pressure, fuel centerline temperature, and cladding strain for sample BWR and PWR cases. It should be noted that the sensitivity to these parameters could change based on differences in power history or fuel rod design.

The manufacturing uncertainties used in this report represent an average value of the tolerances given by fuel rod fabricators. Individual parameters influenced by manufacturing uncertainty include cladding inner diameter, cladding thickness, cladding roughness, pellet outer diameter, theoretical pellet density, pellet re-sinter density, pellet roughness, pellet dish diameter and depth, rod fill gas pressure, and rod plenum length. The model uncertainties used in this report are based on uncertainty in parameters used to fit the aforementioned material property models to experimental data as demonstrated in Section 2.0, which may significantly influence output values generated by FRAPCON-3.3. Finally, power uncertainty includes uncertainties associated with the measurement of steady state power and anticipated operational occurrences (AOOs), which typically result in brief power pulses above the steady state power output that last for varying lengths of time. Although these power transients are anticipated, the uncertainty

associated with their intensity and duration may influence the fuel performance predicted by FRAPCON-3.3

The purpose of this study is to evaluate the influence of manufacturing, model, and power uncertainties on fuel performance parameter outputs of interest generated by FRAPCON-3. Establishing the effects of these sources of uncertainty will facilitate more accurate comparisons between modeled and experimentally observed fuel performance. In addition, they will establish which uncertainties are important for inclusion in licensing analyses. This study was performed using the released version of FRAPCON-3.3 as discussed in Section 2.

# 4.1 Outputs of Interest

Material response models incorporated in FRAPCON-3 enable three important fuel rod performance parameters of regulatory interest to be predicted. These output parameters include the rod internal gas pressure, peak fuel centerline temperature, and cladding permanent hoop strain. Each parameter is significant as the predicted value may indicate whether or not the fuel rod will exceed the specific acceptable fuel design limits under designated conditions for licensing analyses. The significance of each parameter is discussed in the following subsections.

#### 4.1.1 Rod Internal Gas Pressure

Rod internal gas pressure is predicted by FRAPCON-3 through models that account for the thermal expansion of the cladding and the fuel. Fission gas release from the fuel pellets is also considered in the rod internal pressure calculation. Rod internal pressure is a critical parameter in fuel rod performance because it contributes to the development of hoop strains endured by the cladding, which may lead to excessive pressure in the rod that could cause cladding lift off (pellet/cladding gap re-opening at high burnup), hydride reorientation (circumferential hydrides reorienting to radial hydrides that embrittle the cladding), and/or cladding failure.

### 4.1.2 Peak Fuel Centerline Temperature

Peak fuel centerline temperature is a critical parameter predicted by FRAPCON-3. By modeling the conductivity of the fuel, gap, cladding, and corrosion layer, the fuel centerline temperature can be predicted. Low gap conductivity resulting from cladding lift off or excessive fission gas release results in significant increase in fuel centerline temperature. When the peak fuel centerline temperature predicted by FRAPCON-3 exceeds the melting temperature of the fuel, FRAPCON-3 will indicate that fuel failure has occurred based on NRC design criteria.

#### 4.1.3 Cladding Permanent Hoop Strain

Fuel rod cladding, which is typically composed of a zirconium-based alloy, surrounds the fuel and prevents fuel from entering the reactor coolant system. Should the cladding fail, fuel may be transported from the fuel rod to the reactor vessel contaminating the entire primary coolant loop with fissile material. Fuel rod cladding typically fails by cracking due to pellet-clad mechanical loads, or bursting due to gas pressure (preceded by ballooning) during a power transient or LOCA, respectively. In order for a cladding to balloon and eventually burst, a significant amount of plastic circumferential, or hoop, strain (i.e.,  $\epsilon_{hoop}$ ) must manifest within the cladding. By predicting the hoop strain in the cladding, FRAPCON-3 can identify conditions that would be conducive for cladding failure. The standard review plan (Standard Review Plan Section 4.2,

2007) states that transient induced uniform deformation (elastic + plastic) should not exceed 1% strain.

## 4.1.4 Other Outputs of Interest

Although the outputs listed above are significant fuel rod performance parameters, there are several other outputs of regulatory interest. Among these are the volume-average fuel temperature (i.e. stored energy), gap conductance, and the cladding hydrogen concentration. Hydrogen concentration is important for determining the cladding strain capability and propensity for failure. The significance of choosing rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain as outputs of interest is that these are directly measured and generally representative of fuel rod performance.

## 4.2 Selection of Base Cases

In order to evaluate the influence of the different types of uncertainty on the output of FRAPCON-3, a base case must be established for both PWR and BWR fuel performance calculations. The purpose of this section is to describe the fuel design parameters, power histories, and axial power profiles that are used as code input to define these base cases.

The base cases employed in this study utilized a 17x17 PWR and a 10x10 BWR with typical design parameters required for FRAPCON-3 code input published in NUREG-1754 (O'Donnell et al, 2001) and are presented in Table 4.1.

Table 4.1 Typical fuel design parameters used for base case code input (NUREG-1754)

	PWR	BWR
Description of Design Parameter	17x17	10x10
Pitch (mm, <i>in</i> )	12.6, <i>0.4</i> 98	13.0, <i>0.510</i>
Cladding OD (mm, <i>in</i> )	9.4, 0.370	10.0, <i>0.395</i>
Cladding Thickness (mm, in)	0.610, <i>0.024</i>	0.660, <i>0.026</i>
Cladding ID (mm, in)	8.18, <i>0.322</i>	8.68, <i>0.343</i>
Gap Thickness (mm, in)	0.084, 0.0033	0.089, <i>0.0035</i>
Fuel Pellet Diameter (mm, in)	8.0, <i>0.315</i>	8.5, <i>0.336</i>
Plenum Spring Diameter (mm, in)	8.0, <i>0.315</i>	8.5, <i>0.336</i>
Pellet Length (mm, in)	11.4, <i>0.45</i>	11.4, <i>0.45</i>
Dish Diameter (mm, in)	4.01, <i>0.158</i>	0, 0
Dish Depth (mm, in)	0.287, 0.0113	0, 0
Plenum Length (mm, in)	254, 10	254, 10
Turns in Plenum Spring	28	31
Plenum Spring Wire Diameter (mm, in)	1.27, <i>0.05</i>	1.27, <i>0.05</i>
Helium Fill Gas Pressure (MPa, psi)	2.41, 350	0.69, 100
Active Fuel Length (m, in)	3.66, <i>144</i>	3.66, <i>144</i>
System Coolant Pressure (MPa, psi)	15.5, <i>2250</i>	7.14, 1035
Coolant Inlet Temperature (°C, °F)	288, <i>550</i>	277, 530
Coolant Flow Rate (x10 <sup>6</sup> kg/m <sup>2</sup> , x10 <sup>6</sup> lb/ft <sup>2</sup> )	12.47, <i>2.55</i>	5.13, <i>1.05</i>
Enrichment (atom %)	4.5	4
Pellet Density (% TD)	95	95
Limit on Pellet Density Increase (% TD)	0.9	0.9
Fuel Surface Roughness (μm, in)	2.0, 3x10 <sup>-5</sup>	2.0, 3x10 <sup>-5</sup>
Cladding Surface Roughness (μm, in)	0.5, 2x10 <sup>-5</sup>	0.5, 2x10 <sup>-5</sup>
Cladding Material	Zircaloy-4	Zircaloy-2
Cold Work (%)	50	0

It is acknowledged that the fill gas pressure of 350 psi that was used for the PWR case is higher than the fill gas pressure for many modern rods (175 psi). A brief study was performed to confirm that relative differences caused by biasing other parameters were the same for both initial fill gas pressures.

In addition to selecting prototypical fuel design parameters for the desired base cases, the power histories and axial power profiles were also designated specific input values. Both the PWR and BWR cases were evaluated up to a rod average burnup of 65 GWd/MTU. Although different factors, such as core management, may introduce uncertainty, the power histories and axial power profiles presented here are assumed to be representative and employed for comparison. In order to evaluate the influence of power uncertainties at various levels of burnup, individual conditions were examined in which AOOs were implemented at 30, 40, and 50 GWd/MTU. At the time of the AOO, the output power was increased 50% for a period of 4hrs. This AOO was selected as the more limiting AOO for temperature, pressure and strain than an overpower of 25% that is held for 12 hrs. Power histories for the PWR and BWR base cases are presented in Figure 4.1 without an AOO. A symmetrical power profile was selected for both the PWR and BWR base cases and is presented in Table 4.2. A modern BWR power profile is more peaked than this profile, but a brief study confirmed that the relative effects of the uncertainties would be the same by running several of the cases discussed in the following section using a more peaked axial power profile.

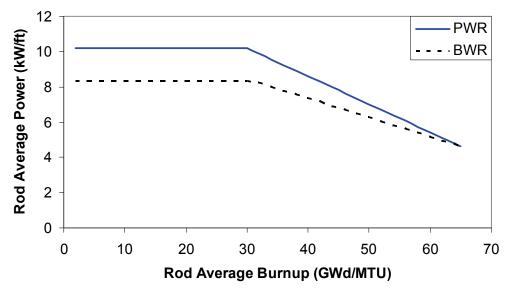


Figure 4.1 Power histories for PWR and BWR base cases without AOO

 Table 4.2
 Axial power profile used for PWR and BWR base case input

Axial	Axial
Elevation	Power
(mm)	Profile
0	0.63
305	0.83
610	1.03
914	1.08
1219	1.08
2438	1.08
2743	1.08
3048	1.03
3353	0.83
3660	0.63

# 4.3 Effects of Manufacturing Uncertainties

Manufacturing uncertainties stem from the range of tolerances used in fuel rod fabrication. Variation in cladding and pellet metrics, such as cladding thickness and pellet diameter, can influence geometric relationships between the cladding and the fuel like the pellet-cladding gap. Consequently, the end of life rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain ( $\epsilon_{hoop}$ ) predictions generated by FRAPCON-3 may be influenced by manufacturing uncertainties. The purpose of this section is to present and discuss comparisons between base cases and cases biased by manufacturing uncertainty. Tolerances presented in this section were not chosen arbitrarily, and are considered typical of industry. Comparisons for PWR and BWR cases are presented in Tables 4.3 and 4.4, respectively, and discussed in the following subsections.

If tolerances are greater than those assumed in these tables, this may change the conclusions from this sample calculation on sensitivity. Also, this sample calculation only examined individual changes in manufacturing tolerances rather than the combined effects from all sources. Combined effects of manufacturing uncertainties will have a more significant impact on fuel performance.

Comparison between unbiased output and output biased by manufacturing uncertainty for a 17x17 PWR Table 4.3

			Cladding In	<b>Cladding Inner Diameter</b>	Cladding	Cladding Thickness	Cladding	Cladding Roughness
Condition	Responses	Unbiased	+ 0.04 mm	- 0.04 mm	+ 0.04 mm	- 0.04 mm	+ 0.3 mm	- 0.3 mm
No AOO	Rod Internal Pressure (MPa)	12.16	12.81	11.57	12.17	12.07	12.24	12.02
	Peak Fuel Centerline T (°C)	1590	1586	1594	1591	1588	1594	1586
30	Rod Internal Pressure (MPa)	13.25	13.83	12.69	13.34	13.24	13.29	13.16
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2314	2325	2321	2317	2325	2314
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.4354	0.4343	0.4365	0.4323	0.4384	0.4378	0.4325
40	Rod Internal Pressure (MPa)	14.13	14.75	13.44	14.15	14.13	14.19	14.00
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2074	2084	2080	2077	2085	2073
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.3570	0.3579	0.3550	0.3604	0.3598	0.3552
50	Rod Internal Pressure (MPa)	14.20	14.71	13.61	14.32	14.17	14.33	14.19
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1783	1793	1789	1787	1793	1782
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2672	0.2661	0.2680	0.2656	0.2692	0.2693	0.2655
			Pellet Outer Diameter	Diameter	Pellet Density	Neit*	Pellet Re-Sinter Density	er Densitv
Condition	Responses	Unbiased	+ 0.013 mm	- 0.013 mm	+ 0.91% TD	- 0.91% TD	+ 0.4% TD	- 0.4% TD
No AOO	Rod Internal Pressure (MPa)	12.16	12.02	12.35	11.93	12.28	11.82	12.42
	Peak Fuel Centerline T (°C)	1590	1590	1589	1571	1609	1581	1599
30	Rod Internal Pressure (MPa)	13.25	13.03	13.48	13.02	13.48	12.98	13.49
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2320	2318	2295	2344	2308	2331
	Cladding Permanent $arepsilon_{ ext{hoop}}$ (%)	0.4354	0.4365	0.4336	0.4285	0.4425	0.4318	0.4384
40	Rod Internal Pressure (MPa)	14.13	13.92	14.29	13.93	14.14	13.79	14.36
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2080	2077	2056	2101	2068	2090
	Cladding Permanent $arepsilon_{hoop}$ (%)	0.3575	0.3587	0.3562	0.3517	0.3634	0.3546	0.3605

14.52 1798 0.2700

13.96 1778 0.2646

14.25 1807 0.2726

14.05 1768 0.2617

14.45 1787 0.2658

14.01 1789 0.2682

14.20 1788 0.2672

Rod Internal Pressure (MPa) Peak Fuel Centerline T (°C) Cladding Permanent  $\epsilon_{\text{hoop}}$  (%)

50 GWd/MTU

Table 4.3 (continued). Comparison between unbiased output and output biased by manufacturing uncertainty for a 17x17 PWR

			Pellet Roughness	ghness	Pellet Dish Diameter & Depth	neter & Depth	Rod Fill Pressure	essure
Condition	Responses	Unbiased	+ 0.5 mm	- 0.5 mm	+ 0.5 &0.05 mm	- 0.5 &0.05 mm	+ 69 kPa	- 69 kPa
No AOO	Rod Internal Pressure (MPa)	12.16	12.26	12.03	12.00	12.35	12.30	12.03
	Peak Fuel Centerline T (°C)	1590	1597	1583	1589	1590	1589	1590
30	Rod Internal Pressure (MPa)	13.25	13.32	13.08	13.31	13.47	13.44	13.06
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2329	2309	2318	2320	2318	2320
	Cladding Permanent $arepsilon_{hoop}$ (%)	0.4354	0.4397	0.4302	0.4322	0.4356	0.4345	0.4356
40	Rod Internal Pressure (MPa)	14.13	14.20	13.90	14.07	14.36	14.31	13.95
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2089	2068	2078	2079	2078	2080
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.3613	0.3535	0.3512	0.3578	0.3573	0.3579
20	Rod Internal Pressure (MPa)	14.20	14.33	14.03	14.08	14.39	14.39	14.04
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1797	1778	1787	1788	1787	1789
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2672	0.2711	0.2634	0.2589	0.2673	0.2669	0.2676

			Rod Plenum Length	n Length	
Condition	Responses	Unbiased	+1 Pellet Length -1 Pellet Length	-1 Pellet Length	
No A00	Rod Internal Pressure (MPa)	12.16	11.96	12.38	
	Peak Fuel Centerline T (°C)	1590	1589	1590	
30	Rod Internal Pressure (MPa)	13.25	12.92	13.59	
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2319	2320	
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.4354	0.4349	0.4353	
40	Rod Internal Pressure (MPa)	14.13	13.79	14.41	
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2078	2079	
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.3573	0.3577	
50	Rod Internal Pressure (MPa)	14.20	13.96	14.58	
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1788	1788	
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2672	0.2671	0.2676	

Comparison between unbiased output and output biased by manufacturing uncertainty for a 10x10 BWR Table 4.4

Condition	9000000	Inhiaead	Cladding Inner Diameter	er Diameter	Cladding + 0.04 mm	Cladding Thickness	Cladding Roughness	oughness
No AOO	Rod Internal Pressure (MPa)	5.37	5.56	4.99	5.37	5.37	5.36	5.41
	Peak Fuel Centerline T (°C)	1234	1266	1237	1235	1232	1237	1230
30	Rod Internal Pressure (MPa)	5.30	5.63	4.94	5.31	5.29	5.30	5.13
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1864	1874	1870	1866	1876	1860
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.1902	0.3253	0.3158	0.3202	0.3231	0.3134
40	Rod Internal Pressure (MPa)	6.56	6.84	6.28	6.57	6.56	69.9	6.56
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1723	1735	1730	1727	1738	1721
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.2599	0.2733	0.2660	0.2714	0.2736	0.2643
20	Rod Internal Pressure (MPa)	6.73	7.00	6.46	6.74	6.73	68.9	99.9
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1525	1535	1532	1528	1538	1522
	Cladding Permanent Ehoop (%)	0.2067	0.1997	0.2121	0.2051	0.2083	0.2109	0.2020
					:	:		:
	1	:	Pellet Outer Diameter	Diameter	Pellet Density	ensity	Pellet Re-Sinter Density	er Density
Condition	Responses	Unbiased	+ 0.013 mm	- 0.013 mm	+ 0.91% 1D	- 0.91% TD	+ 0.4% 1D	- 0.4% ID
No AOO	Rod Internal Pressure (MPa)	5.37	5.24	5.46	5.18	4.83	5.28	5.40
	Peak Fuel Centerline T (°C)	1234	1234	1233	1218	1248	1231	1240
30	Rod Internal Pressure (MPa)	5.30	5.18	5.41	5.13	5.45	5.23	5.35
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1869	1867	1843	1893	1857	1879
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3213	0.3102	0.3097	0.3263	0.3068	0.3234
40	Rod Internal Pressure (MPa)	6.56	6.43	6.67	6:29	6.63	6.47	6.62
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1730	1728	1705	1750	1719	1738
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.2708	0.2653	0.2614	0.2743	0.2634	0.2726
20	Rod Internal Pressure (MPa)	6.73	6.59	6.84	6.59	6.78	6.64	6.94
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1532	1528	1511	1548	1521	1539
	Cladding Permanent $arepsilon_{ ext{hoop}}$ (%)	0.2067	0.2094	0.2031	0.2009	0.2113	0.2016	0.2113

Table 4.4 (continued). Comparison between unbiased output and output biased by manufacturing uncertainty for a 10x10 BWR

Condition	Responses	Unbiased	Pellet Roughness	yhness - 0.5 mm	Pellet Dish Diameter & Depth + 0.5 & 0.05 mm - 0.5 & 0.05 mm	eter & Depth - 0.5 & 0.05 mm	Rod Fill Pressure + 69 kPa - 69 k	essure - 69 kPa
No AOO	Rod Internal Pressure (MPa)	5.37	5.11	5.45	Ϋ́	ΑN	5.67	5.25
	Peak Fuel Centerline T (°C)	1234	1240	1227	Ϋ́	Ϋ́	1230	1235
30	Rod Internal Pressure (MPa)	5.30	5.30	5.12	Ϋ́Z	Ϋ́	5.36	5.08
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1884	1852	ΑN	ΑN	1862	1872
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3270	0.3077	Ϋ́	Ϋ́	0.3134	0.3197
40	Rod Internal Pressure (MPa)	6.56	69.9	6.56	Ϋ́	Ϋ́	6.80	6.46
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1744	1711	ΑN	ΑN	1725	1734
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.2759	0.2585	Ϋ́	Ϋ́	0.2664	0.2704
50	Rod Internal Pressure (MPa)	6.73	98.9	6.51	Ϋ́	Ϋ́Z	6.82	6.63
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1543	1515	Ϋ́	Ϋ́	1525	1534
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2067	0.2136	0.1979	Ϋ́	N A	0.2024	0.2089

			Rod Plenum Lenath	n Lenath	
Condition No AOO	Responses Rod Internal Pressure (MPa)	Unbiased 5.37	+1 Pellet Length -1 Pellet Length 5.18 5.62	-1 Pellet Length 5.62	
	Peak Fuel Centerline T (°C)	1234	1233	1234	
30	Rod Internal Pressure (MPa)	5.30	5.11	5.51	
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1867	1869	
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3174	0.3194	
40	Rod Internal Pressure (MPa)	6.56	6.31	6.84	
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1728	1730	
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.2676	0.2693	
50	Rod Internal Pressure (MPa)	6.73	6.62	6.95	
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1530	1530	
	Cladding Permanent Ehoop (%)	0.2067	0.2069	0.2059	

## 4.3.1 Cladding Inner Diameter

## **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting cladding inner diameter by the manufacturing tolerance of ±0.04mm are presented in Table 4.3 for comparison. The average variance in rod internal pressure is 4.5% and ranges from 3.60% at the positively biased 50 GWd/MTU condition to 5.40% at the positively biased no AOO condition. Peak fuel centerline temperature and cladding permanent hoop strain values varied from the base case by less than 0.3% and 0.4%, respectively. Based on these observations, it appears that manufacturing uncertainty in cladding inner diameter has the potential to influence the rod internal pressure generated by FRAPCON-3. A tendency for rod internal pressure to increase and decrease with cladding inner diameter was observed. However, peak fuel centerline temperatures and cladding permanent hoop strains varied inversely with cladding inner diameter.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting cladding inner diameter by the manufacturing tolerance of ±0.04mm are presented in Table 4.4 for comparison. The average variance in rod internal pressure is 5.0% and ranges from 3.64% to 7.00% under the positively and negatively biased no AOO conditions, respectively. Although the other peak fuel centerline temperatures varied by less than 0.4%, the positively biased peak fuel centerline temperature with no AOO exceeded the base case by 2.6%. In addition, an outlying variation in cladding permanent hoop strain of 40.2% was observed at the positively biased 30 GWd/MTU condition. This is likely due to the gap not being closed in this case at the time of the AOO. With exception of this case, the average variance of the permanent cladding hoop strain is 2.7% and ranges from 1.86% under the negatively biased 40 GWd/MTU condition to 3.39% under the positively biased 50 GWd/MTU condition. It appears that manufacturing uncertainty in cladding inner diameter has no significant influence on rod internal pressure and no effect on peak fuel centerline temperature or an increase in cladding permanent hoop strain predictions. A tendency for rod internal pressure to increase and decrease with cladding inner diameter was observed. However, peak fuel centerline temperatures and cladding permanent hoop strains typically varied inversely with cladding inner diameter.

# 4.3.2 Cladding Thickness

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting cladding thickness by the manufacturing tolerance of ±0.04mm are presented in Table 4.3 for comparison. The maximum variance for each of the three outputs of interest is less than 1.0% from the base case, which indicates that manufacturing uncertainty in cladding thickness does not significantly affect outputs of interest generated FRAPCON-3. Although the variance is negligible, a tendency for rod internal pressure and peak fuel centerline temperature to increase and decrease with cladding thickness was observed. However, cladding permanent hoop strain values tended to vary inversely with cladding thickness.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting cladding thickness by the manufacturing tolerance of  $\pm 0.04$ mm are presented in Table 4.4 for comparison. The average variance each of these outputs of interest is less than 1% from the base BWR case. It appears that manufacturing uncertainty in cladding thickness has no influence on outputs of interest from FRAPCON-3. Although the differences were negligible, a tendency for rod internal pressure and peak fuel centerline temperature to increase and decrease with cladding thickness was observed. However, cladding permanent hoop strain values tended to vary inversely with cladding thickness.

## 4.3.3 Cladding Roughness

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting cladding roughness by the manufacturing tolerance of  $\pm 0.3 \mu m$  are presented in Table 4.3 for comparison. The maximum variance for each of the three outputs of interest is less than 1.2% from the base PWR case, which indicates that manufacturing uncertainty in cladding roughness does not have an effect on outputs of interest from FRAPCON-3. Although the variance was negligible, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with cladding roughness was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting cladding roughness by the manufacturing tolerance of ±0.3µm are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 1.2% on average and range from 0.02% to 3.24% at the positively and negatively biased 30 GWd/MTU conditions, respectively. Peak fuel centerline temperatures vary from the base case by less than 1%. Cladding permanent hoop strain exhibits an average variance of 1.8%, ranging from 1.45% at the negatively biased 30 GWd/MTU condition to 2.27% at the negatively biased 50 GWd/MTU conditions. Based on these observations, it appears that manufacturing uncertainty in cladding roughness has no influence on the outputs of interest generated by FRAPCON-3. Although the variance was negligible, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with cladding roughness was observed.

#### 4.3.4 Pellet Outer Diameter

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting pellet outer diameter by the manufacturing tolerance of ±0.013mm are presented in Table 4.3 for comparison. The average variance for rod internal pressure is 1.5% and ranges from 1.11% at the negatively biased 40 GWd/MTU condition to 1.80% at the negatively biased 50 GWd/MTU condition. Peak fuel centerline temperature and permanent cladding hoop strain values typically differ from the base case by less than 0.5%. Based on these observations, it appears that manufacturing uncertainty in pellet outer diameter has no effect on the outputs of interest from FRAPCON-3. Although the variance was small, a tendency for rod internal pressure to vary inversely with pellet outer

diameter was observed. However, a tendency for peak fuel centerline temperature and cladding permanent hoop strain to increase and decrease with pellet outer diameter was also observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting pellet outer diameter by the manufacturing tolerance of ±0.013mm are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 2.0% on average. This variance ranges from 1.66% at the negatively biased 50 GWd/MTU condition to 2.29% at the positively biased no AOO and 30 GWd/MTU conditions. Fuel centerline temperatures differ from the base case by less than 0.1% on average. The average variance between cladding permanent hoop strains predicted from the base case and cases biased by uncertainty in pellet outer diameter is 1.4%. This variance ranges from 0.93% under the positively biased 40 GWd/MTU conditions to 2.45% under the negatively influenced 30 GWd/MTU condition. Based on these observations, it appears that manufacturing uncertainty in the pellet outer diameter has no effect on the outputs of interest generated by FRAPCON-3. Although the variance was small, a tendency for rod internal pressures to vary inversely with increasing and decreasing pellet outer diameter was observed. However, a tendency for peak fuel centerline temperature and cladding permanent hoop strain to increase and decrease with pellet outer diameter was also observed.

# **4.3.5** Theoretical Pellet Density PWR

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting theoretical pellet density (TD) by the manufacturing tolerance of ±0.91%TD are presented in Table 4.3 for comparison. The average variance for rod internal pressure is 1.2% and ranges from 0.05% at the negatively biased 40 GWd/MTU condition to 1.91% at the positively biased no AOO condition. Peak fuel centerline temperature varies from the base case by 1.1% on average and ranges from 1.04% at the positively biased 30 GWd/MTU condition to 1.23% at the negatively biased no AOO condition. Cladding permanent hoop strain values vary by 1.8% on average and ranges from 1.58% at the positively biased 30 GWd/MTU condition to 2.06% at the positively biased 50 GWd/MTU condition. Based on these observations, it appears that manufacturing uncertainty in theoretical pellet density has no influence on the outputs of interest generated by FRAPCON-3. Although the variation was insignificant, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with pellet theoretical density was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting theoretical pellet density (TD) by the manufacturing tolerance of  $\pm 0.91\%$  are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 2.0% on average excluding an outlier at the negatively biased no AOO condition, which varied by 10%. This variance is most likely due to less gas release in this case, which resulted in less pressure. Variance in rod internal pressure ranged from 0.47% in the positively biased 40 GWd/MTU condition to 3.43% in the positively biased no AOO condition. Peak fuel centerline temperature varied by 1.3% on average and ranged from 1.17% at the negatively biased no AOO condition to 1.39% at the positively biased 40 GWd/MTU condition. Cladding permanent hoop strain varied by 2.5% on average and ranged from 2.23% to 2.81% at the negatively and positively biased 50

GWd/MTU conditions, respectively. Overall, it appears that manufacturing uncertainty in theoretical pellet density has low to moderate influence on outputs of interest generated by FRAPCON-3. A tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with pellet theoretical density was observed.

# 4.3.6 Pellet Re-Sinter Density

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting pellet re-sinter density by the manufacturing tolerance of ±0.4% TD are presented in Table 4.3 for comparison. In-reactor densification can have significant consequences for fuel performance and is described in greater detail in U.S. NRC Regulatory Guide 1.126 (U.S. NRC, 1978). The average variance for rod internal pressure is 2.1% and ranges from 1.62% at the negatively biased 40 GWd/MTU condition to 2.78% at the positively biased no AOO condition. Peak fuel centerline temperature and cladding hoop strain values differ from the base case by less than 1%. Based on this, it appears that manufacturing uncertainty in pellet re-sinter density has a small influence on outputs of interest generated by FRAPCON-3. Although the variation was small, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with pellet re-sinter density was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting pellet re-sinter density by the manufacturing tolerance of  $\pm 0.4\%$  TD are presented in Table 4.4 for comparison. In-reactor densification can have significant consequences for fuel performance and is described in greater detail in U.S. NRC Regulatory Guide 1.126. Rod internal pressure values vary from the base case by 1.4% on average and range from 0.68% in the negatively biased no AOO condition to 3.23% in the negatively biased 50 GWd/MTU condition. Peak fuel centerline temperatures differ from the base case by 0.6% or less. Cladding permanent hoop strain exhibited an average variance of 2.2% ranging from 1.60% in the negatively biased 40 GWd/MTU condition to 3.52% in the positively biased 30 GWd/MTU condition. Based on this, it appears that manufacturing uncertainty in pellet re-sinter density has a small influence on outputs of interest generated by FRAPON-3. Although the variation was small, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with pellet re-sinter density was observed.

# 4.3.7 Pellet Roughness

#### <u>PWR</u>

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting pellet roughness by the manufacturing tolerance of  $\pm 0.5 \mu m$  are presented in Table 4.3 for comparison. The average variances in rod internal pressure, peak fuel centerline temperature, and permanent cladding values are 1.0, 0.47, and 1.2%, respectively. The maximum variance detected for any value was 1.69% for rod internal pressure at the negatively biased 40 GWd/MTU condition. Based on this, it appears that manufacturing uncertainty in pellet roughness has no influence on FRAPCON-3 output. Although the variation was insignificant, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with pellet roughness was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting pellet roughness by the manufacturing tolerance of ±0.5µm are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 2.1% on average and range from 0.08% at the negatively biased 40 GWd/MTU conditions to 4.78% at the positively biased no AOO condition. Peak fuel centerline temperatures differ by less than 1.00% from the base. Cladding permanent hoop strain exhibited an average variance of 3.4% ranging from 2.83% at the positively biased 30 GWd/MTU and 40 GWd/MTU conditions to 4.26% at the negatively biased 50 GWd/MTU condition. Based on this, it appears that manufacturing uncertainty in pellet roughness has a low to moderated influence on FRAPCON-3 output. A tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with pellet roughness was observed.

# 4.3.8 Pellet Dish Diameter and Depth PWR

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting pellet dish diameter and depth by the manufacturing tolerances of ±0.5 and 0.05mm, respectively, are presented in Table 4.3 for comparison. Rod internal pressure varied by 1.2% on average and ranged from 0.41% at the positively biased 30 GWd/MTU condition to 1.62% at the negatively biased no AOO condition. Peak fuel centerline temperature values vary at most by 0.05% at the positively biased 50 GWd/MTU condition. Cladding permanent hoop strain values vary, on average, by 1.0% and range from 0.04% to 3.11% at the negative and positive 50 GWd/MTU conditions, respectively. These results indicate that manufacturing uncertainty in pellet dish diameter and depth has no influence on the outputs of interested generated by FRAPCON-3. Although the variation was insignificant, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with pellet dish diameter and depth was observed.

#### **BWR**

The fuel design used in this study were not dished on-end. Therefore, the influence of manufacturing uncertainty in pellet dish diameter and depth were not evaluated for the BWR base case. For dished BWR pellets, the effect of variation in the dish dimnsions are expected to be similar to the PWR case.

## 4.3.9 Rod Fill Pressure

### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting rod fill pressure by the manufacturing tolerances of  $\pm$  10psi ( $\approx$  0.07MPa) are presented in Table 4.3 for comparison. Rod internal pressure varies by 1.3% on average and ranges from 1.06% in the negatively biased no AAO condition to 1.44% in the negatively biased 30 GWd/MTU condition. Peak fuel centerline temperatures and cladding hoop strain values vary by less than 0.5%. Overall, it appears that manufacturing uncertainty in rod fill pressure has no influence on rod the outputs of interest generated by FRAPCON-3. Although the variation was insignificant, a tendency for rod

internal pressure to increase and decrease with rod fill pressure was observed. However a tendency for peak fuel centerline temperatures and cladding permanent hoop strains to vary inversely with rod fill pressure was also observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting rod fill pressure by the manufacturing tolerance of  $\pm$  10psi ( $\approx$  0.07MPa) are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 2.7% on average and range from 1.13% at the positively biased 30 GWd/MTU condition to 5.71% in the positively biased no AOO condition. Fuel centerline temperatures, on the other hand, varied by 0.33% or less. Cladding permanent strain variances averaged 1.1% and range from 0.53% at the negatively biased 30 GWd/MTU condition to 2.08% at the positively biased 50 GWd/MTU condition. Based on these observations, it appears that manufacturing uncertainty in rod fill pressure has low to moderate influence on the outputs of interest generated by FRAPCON-3. A tendency for rod internal pressure to increase and decrease with rod fill pressure was observed. However a tendency for peak fuel centerline temperatures and cladding permanent hoop strains to vary inversely with rod fill pressure was also observed.

# 4.3.10 Rod Plenum Length PWR

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting rod plenum length by the manufacturing tolerances of  $\pm 1$  pellet length are presented in Table 4.3 for comparison. Rod internal pressure varies by 2.2% on average and ranges from 1.59% in the positively biased no AOO condition to 2.69% in the negatively biased 50 GWd/MTU condition. Peak fuel centerline temperatures and cladding hoop strain values vary by less than 0.5%. Overall, it appears that manufacturing uncertainty in rod plenum length has no influence on outputs of interest generated by FRAPCON-3. Although variances were insignificant, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with rod plenum length was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting rod plenum length by the manufacturing tolerance of  $\pm$  1 pellet length are presented in Table 4.4 for comparison. Rod internal pressure values vary from the base case by 3.6% on average and range from 1.55% in the positively biased 50GWd/MTU condition to 4.64% in the negatively biased no AOO condition. Peak fuel centerline temperatures and cladding permanent hoop strains, on the other hand, varied by 0.44% or less. Based on these observations, it appears that uncertainty in rod plenum length has low to moderate influence on the outputs of interest generated by FRAPCON-3. A tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with rod plenum length was observed.

### 4.4 Effects of Model Uncertainties

Model uncertainties stem from uncertainties in the models used to simulate the material response of the fuel rod in service. Uncertainty in model fitting parameters resulting from scatter in experimental data may significantly influence fuel rod performance predictions generated by FRAPCON-3. The purpose of this section is to present and discuss comparisons between base

cases and cases biased by model uncertainty. Comparisons for PWR and BWR cases are presented in Tables 4.5 and 4.6, respectively, and discussed in the following subsections.

Comparison between unbiased output and output biased by model uncertainties for a 17x17 PWR Table 4.5

<b>Condition</b> No AOO	Responses Rod Internal Pressure (MPa)	Unbiased 12.16	Fuel Thermal Conductivity + 0.5 W/m-K - 0.5 W/m- 9.77 18.46	Conductivity - 0.5 W/m-K 18.46	Fuel Thermal Expansion * 1.15 12.19 12.09	: <b>xpansion</b> /1.15 12.09	Oxide Conductivity + 0.5 W/m-K - 0.5 12.03	ctivity - 0.5 W/m-K 12.76
	Peak Fuel Centerline T (°C)	1590	1345	2012	1590	1590	1584	1601
30	Rod Internal Pressure (MPa)	13.25	9.77	18.34	13.26	13.21	13.14	13.65
GWd/MTU	Peak Fuel Centerline T (°C)	2319	1952	2772	2318	2320	2313	2333
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.4354	0.3169	0.5531	0.5163	0.3645	0.4343	0.4381
40	Rod Internal Pressure (MPa)	14.13	10.56	18.66	14.01	14.05	13.96	14.65
GWd/MTU	Peak Fuel Centerline T (°C)	2079	1731	2549	2078	2079	2068	2106
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.2463	0.4938	0.4277	0.2966	0.3551	0.3633
50	Rod Internal Pressure (MPa)	14.20	10.40	18.96	14.08	14.21	14.06	14.80
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1484	2260	1787	1788	1771	1852
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2672	0.1693	0.4145	0.3239	0.2165	0.2643	0.2885
			Cladding Conductivity	nductivity	Gas Conductance	ctance	Fission Gas Release	s Release
Condition	Responses	Unbiased	+ 5 W/m-K	- 3 W/m-K	+ 0.02 W/m-K	- 0.02 W/m-K	<b>~</b>	/2
No AOO	Rod Internal Pressure (MPa)	12.16	11.81	12.19	12.02	12.26	14.17	10.60
	Peak Fuel Centerline T (°C)	1590	1573	1604	1588	1591	1599	1583
30	Rod Internal Pressure (MPa)	13.25	12.96	13.56	13.24	13.29	14.93	11.86
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2301	2336	2317	2321	2324	2315
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.4354	0.4283	0.4400	0.4345	0.4362	0.4321	0.4366
40	Rod Internal Pressure (MPa)	14.13	13.84	14.28	14.11	14.13	15.83	12.76
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2063	2093	2077	2081	2085	2073
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.3504	0.3606	0.3571	0.3582	0.3556	0.3583
20	Rod Internal Pressure (MPa)	14.20	13.82	14.38	14.22	14.28	16.14	12.72
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1774	1800	1786	1790	1795	1781
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2672	0.2605	0.2702	0.2668	0.2678	0.2671	0.2659

Table 4.5 (continued) Comparison between unbiased output and output biased by model uncertainties for a 17x17 PWR

			ing	Corrosion	Fuel Swelling	elling	Irradiation Creep	Creep
Condition	Responses	Unbiased	* 1.4	/1.4	+ 0.3	- 0.3	* 1.1	/1.4
No AOO	Rod Internal Pressure (MPa)	12.16	12.73	12.03	12.19	12.16	12.16	12.31
	Peak Fuel Centerline T (°C)	1590	1601	1583	1589	1590	1590	1590
30	Rod Internal Pressure (MPa)	13.25	13.36	13.11	13.35	12.89	13.22	13.39
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2333	2312	2319	2319	2319	2319
	Cladding Permanent $\epsilon_{\text{hoop}}$ (%)	0.4354	0.4390	0.4336	0.4379	0.4331	0.4355	0.4352
40	Rod Internal Pressure (MPa)	14.13	14.64	13.92	14.16	13.46	14.07	14.27
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2108	2066	2079	2079	2079	2079
	Cladding Permanent $\epsilon_{\text{hoop}}$ (%)	0.3575	0.3651	0.3542	0.3626	0.3506	0.3575	0.3575
50	Rod Internal Pressure (MPa)	14.20	14.80	13.76	14.27	13.73	14.19	14.30
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1848	1768	1787	1788	1788	1788
	Cladding Permanent Ehoop (%)	0.2672	0.2920	0.2629	0.2760	0.2541	0.2672	0.2668

			Yield Stre		Young's N	Modulus	Axial Gr	owth
Condition	Responses	Unbiased		1.1	+ 5 MPa	•	* 1.5	/1.5
No AOO	Rod Internal Pressure (MPa)	12.16	12.16		12.16		11.53	12.61
	Peak Fuel Centerline T (°C)	1590	1590		1590	1590	1590 1	1590
30	Rod Internal Pressure (MPa)	13.25	13.21	13.25	13.25	13.25	12.43	13.75
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2317	2320	2319	2319	2319	2319
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.4354	0.4322	0.4364	0.4354	0.4354	0.4352	0.4350
40	Rod Internal Pressure (MPa)	14.13	14.14	14.13	14.13	14.13	13.32	14.58
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2077	2079	2079	2079	2079	2078
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3575	0.3542	0.3587	0.3575	0.3575	0.3574	0.3574
20	Rod Internal Pressure (MPa)	14.20	14.20	14.20	14.20	14.20	13.54	14.76
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1786	1788	1788	1788	1788	1787
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.2672	0.2642	0.2683	0.2672	0.2672	0.2676	0.2669

Table 4.5 (continued) Comparison between unbiased output and output biased by model uncertainties for a 17x17 PWR

			Cladding Thermal Expansion	al Expansion
Condition	Responses	Unbiased	* 1.0	/1.3
No AOO	Rod Internal Pressure (MPa)	12.16	12.11	12.18
	Peak Fuel Centerline T (°C)	1590	1590	1590
30	Rod Internal Pressure (MPa)	13.25	13.21	13.27
GWd/MTU	Peak Fuel Centerline T (°C)	2319	2319	2319
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.4354	0.4315	0.4383
40	Rod Internal Pressure (MPa)	14.13	14.06	14.15
GWd/MTU	Peak Fuel Centerline T (°C)	2079	2079	2079
	Cladding Permanent $\epsilon_{\text{hoop}}$ (%)	0.3575	0.3532	0.3607
50	Rod Internal Pressure (MPa)	14.20	14.13	14.22
GWd/MTU	Peak Fuel Centerline T (°C)	1788	1788	1788
	Cladding Permanent $arepsilon_{ ext{hoop}}$ (%)	0.2672	0.2620	0.2711

Comparison between unbiased output and output biased by model uncertainties for a 10x10 BWR Table 4.6

1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		7	Fuel Thermal Conductivity	onductivity	Fuel Thermal Expansion	xpansion	Oxide Conductivity	ctivity
No AOO	Rod Internal Pressure (MPa)	<b>Unblased</b> 5.37	+ 0.5 W/m-A 3.93	- 0.5 W/m-K 9.59	5.42	5.22	+ 0.5 W/m-A 5.38	- 0.5 W/m-K 5.37
	Peak Fuel Centerline T (°C)	1234	1104	1572	1232	1234	1232	1236
30	Rod Internal Pressure (MPa)	5.30	4.35	11.49	5.22	5.30	5.29	5.30
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1524	2359	1866	1869	1866	1872
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.1811	0.4883	0.3868	0.2546	0.3174	0.3190
40	Rod Internal Pressure (MPa)	6.56	4.65	12.52	6.59	6.55	6.56	6.57
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1410	2215	1728	1729	1726	1733
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.1555	0.4243	0.3274	0.2154	0.2688	0.2686
50	Rod Internal Pressure (MPa)	6.73	4.68	12.80	6.92	6.85	6.74	06.9
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1251	1994	1527	1531	1527	1535
	Cladding Permanent $arepsilon_{hoop}$ (%)	0.2067	0.1093	0.3531	0.2525	0.1649	0.2063	0.2073
			Cladding C	Cladding Conductivity	Gas Conductance	ctance	Fission G	Fission Gas Release
Condition	Responses	Unbiased	+ 5 W/m-K	- 3 W/m-K	+ 0.02 W/m-K	- 0.02 W/m-K	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	/2
No A00	Rod Internal Pressure (MPa)	5.37	5.16	4.86	5.38	5.37	6.87	3.91
	Peak Fuel Centerline T (°C)	1234	1219	1247	1232	1235	1258	1218
30	Rod Internal Pressure (MPa)	5.30	5.11	5.51	5.29	5.30	7.41	5.41
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1845	1889	1865	1871	1885	1851
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3086	0.3249	0.3164	0.3199	0.3135	0.3119
40	Rod Internal Pressure (MPa)	6.56	6.24	6.73	6.56	6.57	8.14	5.16
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1709	1746	1726	1732	1741	1712
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.2683	0.2621	0.2725	0.2675	0.2698	0.2602	0.2700
20	Rod Internal Pressure (MPa)	6.73	6.62	6.84	6.73	6.89	8.45	5.35
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1512	1545	1527	1533	1543	1516
	Cladding Permanent $\varepsilon_{hoop}$ (%)	0.2067	0.2003	0.2107	0.2050	0.2088	0.2012	0.2067

Table 4.6 (continued) Comparison between unbiased output and output biased by model uncertainties for a 10x10 BWR

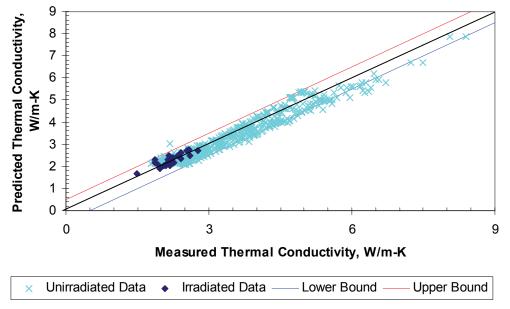
			Cladding (	Corrosion	Fuel Swelling	relling	Irradiation Creep	Creep
Condition	Responses	Unbiased	*1.4	4.1/	+ 0.3	- 0.3	* 1.1	/1.4
No AOO	Rod Internal Pressure (MPa)	5.37	5.37	5.38	5.45	4.91	5.35	5.40
	Peak Fuel Centerline T (°C)	1234	1237 1231	1231	1233	1235	1234	1234
30	Rod Internal Pressure (MPa)	5.30	5.30	5.29	5.28	5.12	5.29	5.35
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1873	1865	1867	1869	1868	1868
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3193	0.3172	0.3264	0.2643	0.3187	0.3124
40	Rod Internal Pressure (MPa)	6.56	6.57	6.56	09:9	6.32	6.54	6.62
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1734	1725	1728	1729	1729	1729
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2683	0.2690	0.2685	0.2819	0.2545	0.2688	0.2658
50	Rod Internal Pressure (MPa)	6.73	6.90	6.73	6.93	09.9	6.71	6.78
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1536	1526	1527	1531	1530	1531
	Cladding Permanent $arepsilon_{hoop}$ (%)	0.2067	0.2076	0.2061	0.2238	0.1880	0.2072	0.2042
			Yield Strenath	enath	Young's N	lodulus	Axial Growth	owth
Condition	Responses	Unbiased	* 1.3	/1.1	+ 5 MPa	- 10 MPa	* 1.5	
No AOO	Rod Internal Pressure (MPa)	5.37	5.37	5.37	5.37	5.37	5.17	5.52
	Peak Fuel Centerline T (°C)	1234	1234	1234	1234 1234	1234	1234	1234
30	Rod Internal Pressure (MPa)	5.30	5.21	5.30	5.30	5.30	5.11	5.43
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1865	1869	1868	1868	1868	1868
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.3180	0.3126	0.3199	0.3180	0.3180	0.3181	0.3181
40	Rod Internal Pressure (MPa)	6.56	6.56	6.56	6.56	6.56	6.32	6.73
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1725	1730	1729	1729	1729	1729
	Cladding Permanent $arepsilon_{hoop}$ (%)	0.2683	0.2679	0.2703	0.2683	0.2683	0.2682	0.2691
50	Rod Internal Pressure (MPa)	6.73	6.65	6.73	6.73	6.73	6.64	6.91
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1520	1532	1530	1530	1531	1529
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.2067	0.1942	0.2091	0.2067	0.2067	0.2073	0.2063

Table 4.6 (continued) Comparison between unbiased output and output biased by model uncertainties for a 10x10 BWR

Condition	Responses	Unbiased	Cladding Thermal Expansion *1.3	al Expansion /1.3
No AOO	Rod Internal Pressure (MPa)	5.37	5.34	5.39
	Peak Fuel Centerline T (°C)	1234	1234	1234
30	Rod Internal Pressure (MPa)	5.30	5.30	5.29
GWd/MTU	Peak Fuel Centerline T (°C)	1868	1868	1868
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.3180	0.3123	0.3212
40	Rod Internal Pressure (MPa)	6.56	6.56	6.55
GWd/MTU	Peak Fuel Centerline T (°C)	1729	1729	1729
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.2683	0.2653	0.2706
20	Rod Internal Pressure (MPa)	6.73	6.71	6.65
GWd/MTU	Peak Fuel Centerline T (°C)	1530	1531	1530
	Cladding Permanent $arepsilon_{ ext{hoop}}$ (%)	0.2067	0.2039	0.2079

# 4.4.1 Fuel Thermal Conductivity

The fuel thermal conductivity model was biased by  $\pm 0.5$  W/m-K, which bounds most of the experimental data below 4.7 W/m-K that is in the temperature range if interest (T>400°C) presented in Figure 4.2.



**Figure 4.2** Predicted and measured thermal conductivity data with  $\pm 0.5$  W/m-K as upper and lower bounds

## **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the fuel thermal conductivity model by  $\pm$  0.5 W/m-K are presented in Table 4.5 for comparison. Rod internal pressure varies by 31.7% on average and ranges from 19.66% to 51.83% at the positively and negatively biased no AOO conditions, respectively. Peak fuel centerline temperatures vary by 20.0% on average and range from 15.37% at the positively biased no AOO condition to 26.59% at the negatively biased no AOO condition. Cladding permanent hoop strain values averaged 35.9% and ranged from 27.03% at the negatively biased 30 GWd/MTU condition to 55.13% at the negatively biased 50 GWd/MTU condition. Based on these observations, it is clear that model uncertainty in the fuel thermal conductivity model significantly influences the outputs of interest generated by FRAPCON-3. A trend for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values to vary inversely with thermal conductivity was observed.

### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting fuel thermal conductivity model by  $\pm$  0.5 W/m-K are presented in Table 4.6 for comparison. Rod internal pressure values vary from the base case by 60.1% on average and range from 17.91% to

116.79% at the positively and negatively biased 30 GWd/MTU conditions, respectively. Peak fuel centerline temperatures vary from the unbiased case by 22.2% on average and range from 10.51% at the positively biased no AOO condition to 30.35% at the negatively biased 50 GWd/MTU condition. Cladding permanent hoop strains vary by 52.5% on average and range from 42.04% at the positively biased 40 GWd/MTU condition to 70.83% at the negatively biased 50 GWd/MTU condition. Based on these observations, it is clear that model uncertainty in the fuel thermal conductivity model significantly influences the outputs of interest generated by FRAPCON-3. A trend for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values to vary inversely with thermal conductivity model bias was observed.

# 4.4.2 Fuel Thermal Expansion

The fuel thermal expansion model was biased by  $\pm 15\%$ , which bounds nearly all the data presented in Figure 4.3.

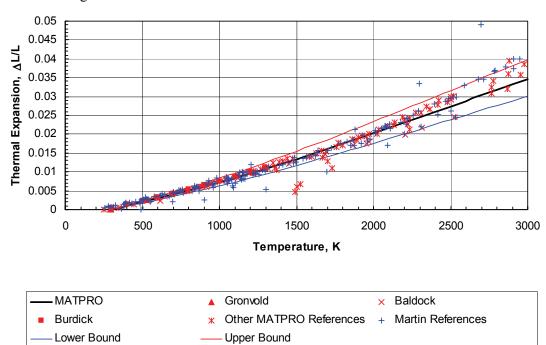


Figure 4.3 UO<sub>2</sub> thermal conductivity model and available data with  $\pm 15\%$  as upper and lower bounds

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the fuel thermal expansion model by either multiplying or dividing by a factor of 1.15 are presented in Table 4.5 for comparison. Rod internal pressure and peak fuel centerline temperature values vary from the unbiased condition by less than 1% and 0.1%, respectively. The small variation is because the gap is closed at high power and/or high burnup for the cases considered. Thermal expansion effects on fuel temperature will be important near BOL and at lower rod powers when the gap is open. Cladding permanent hoop strain values vary by 18.6% on average and range form 16.28% at the negatively biased 30 GWd/MTU condition to 21.22% at the positively biased 50 GWd/MTU condition. Although model uncertainty in the fuel thermal expansion model does not

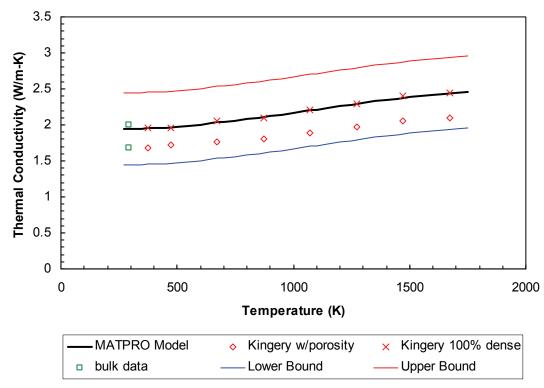
appear to influence rod internal pressure or peak fuel centerline temperature at the burnups and rod powers considered, it does appear to affect the cladding permanent hoop stress values predicted by FRAPCON-3. Since the gap was closed, it is difficult to determine the quantitative influence of fuel thermal expansion model uncertainty on rod internal pressure and peak fuel centerline temperature when the gap is open near BOL. However, a trend for cladding permanent hoop strain to increase and decrease with the fuel thermal expansion model was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting fuel thermal expansion model by either multiplying or dividing by a factor of 1.15 are presented in Table 4.6 for comparison. Rod internal pressure and peak fuel centerline temperature values vary by less than 2.81 and 0.2% from the base case, respectively. The small variation is because the gap is closed at high power and/or high burnup for the cases considered. Cladding permanent hoop strain values vary from the base case by 21.0% on average and range from 19.72% at the negatively biased 40 GWd/MTU case to 22.16% at the positively biased 50 GWd/MTU condition. Although uncertainty in fuel thermal expansion model does not appear to influence rod internal pressure or peak fuel centerline temperature, it does appear to significantly influence the cladding permanent hoop stress values predicted by FRAPCON-3. Since the gap was closed, it is difficult to determine the quantitative influence of fuel thermal expansion model uncertainty on rod internal pressure and peak fuel centerline temperature when the gap is open near BOL. However, a trend for cladding permanent hoop strain to increase and decrease with the fuel thermal expansion model was observed.

## 4.4.3 Cladding Oxide Conductivity

The cladding oxide conductivity model was biased by  $\pm 0.5$  W/m-K, which bound the experimental data presented in Figure 4.4.



**Figure 4.4**  $ZrO_2$  thermal conductivity model and available data with  $\pm 0.5$  W/m-K as upper and lower bounds

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the cladding oxide conductivity model by ±0.5 W/m-K are presented in Table 4.5 for comparison. Rod internal pressure values varied from the base case by 2.5% on average and ranged from 0.82% at the positively biased 30 GWd/MTU condition to 4.26% in the negatively biased 50 GWd/MTU condition (68 µm oxide). Peak fuel centerline temperatures varied from the base case by 1.0% and ranged from 0.28% in the positively biased 30 GWd/MTU condition to 3.59% in the negatively based 50 GWd/MTU condition. Cladding permanent hoop strain values varied by 2.0% on average and ranged from 0.25% at the positively biased 30 GWd/MTU condition to 7.97% in the negatively biased 50 GWd/MTU condition. Overall it appears that uncertainty in oxide thermal conductivity has a small influence on the outputs of interest generated by FRAPCON-3. Although the variance was small, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with cladding oxide conductivity was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the cladding oxide conductivity model by  $\pm 0.5$  W/m-K are presented in Table 4.6 for comparison. Average variance in rod internal pressure between the unbiased and biased model conditions is 0.4%, which includes a larger variance of 2.51% at the negatively biased 50 GWd/MTU condition (21  $\mu$ m oxide). Excluding that larger variance, the rod internal pressure varies from the

unbiased base case by 0.01% at the positively biased 40 GWd/MTU condition to 0.24% at the positively biased no AOO condition. Peak fuel centerline temperature and cladding permanent hoop strain values vary from the base case by less than 0.5%. Overall, it appears that uncertainty in the oxide conductivity does not influence the rod internal pressure, fuel centerline temperature, or cladding permanent hoop strain values predicted by FRAPCON-3. Since the variance is very small, it is difficult to discern trends between rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain with cladding oxide conductivity. However, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with cladding oxide conductivity was observed.

## 4.4.4 Cladding Conductivity

The cladding conductivity model was biased by +5/-3 W/m-K, which bounds nearly all the experimental data presented in Figure 4.5.

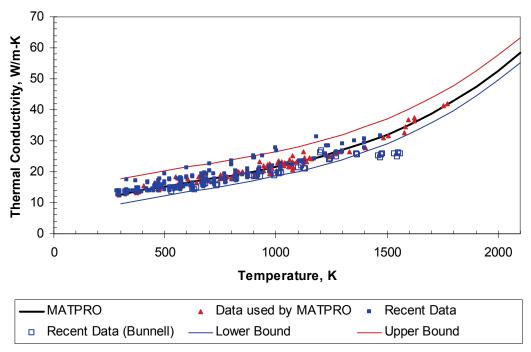


Figure 4.5 Zircaloy thermal conductivity model and available data with +5/-3 W/m-K as upper and lower bounds

## **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the cladding conductivity model by +5 W/m-K and -3 W/m-K are presented in Table 4.5 for comparison. Rod internal pressure values varied from the base case by 1.8% on average and range from 0.28% to 2.84% at the negatively and positively biased no AOO conditions, respectively. Peak fuel centerline temperatures varied from the base case by less than 1%. Cladding permanent hoop strain values varied by 1.5% on average and range from 0.87% at the negatively biased 40 GWd/MTU case to 2.51% at the positively biased 50GWd/MTU case. Overall, it appears that model uncertainty in the cladding conductivity model has no significant influence on the outputs of interest generated by FRAPCON-3. Despite the lack of a significant influence, a tendency for

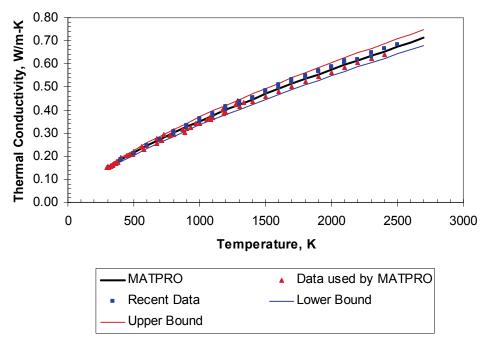
rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to vary inversely with cladding conductivity was observed.

## **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the cladding conductivity model by +5 W/m-K and -3W/m-K are presented in Table 4.6 for comparison. Rod internal pressure values vary from the unbiased case by 4.0% on average and range from 1.57% in the positively biased 50 GWd/MTU condition to 9.51% in the negatively biased no AOO condition. Peak fuel centerline temperatures vary from the based case by 1.1% on average and range form 1.00% in the negatively biased 50 GWd/MTU condition to 1.22% in the positively biased 30 GWd/MTU condition. The cladding permanent hoop strain values varied from the base case by 2.4% on average and ranged from 1.57% at the negatively biased 40 GWd/MTUcondition to 3.10% at the positively biased 50 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding conductivity model has no significant influence on the outputs of interest generated by FRAPCON-3. Although the variance was small, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values to vary inversely with cladding conductivity was observed.

#### 4.4.5 Gas Conductance

The gas conductance model was biased by  $\pm 5\%$ , which bounds nearly all the experimental data presented in Figure 4.6.



**Figure 4.6** Helium thermal conductivity model and available data with  $\pm 5\%$  as upper and lower bounds

## **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the gas conductance model by ±5% are presented in Table 4.5 for comparison. Rod internal pressure, peak fuel

centerline temperature, and cladding permanent hoop strain values varied by less than 1.15%. Based on this, it appears that model uncertainty in the gas conductance model has no significant influence over the outputs of interest generated by FRAPCON-3. Despite the lack of a significant effect, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to decrease with enhanced gas conductivity was observed.

## **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the gas conductance model by  $\pm 5\%$  are presented in Table 4.6 for comparison. Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values varied from the base case by less than 1%. Based on this, it appears that model uncertainty in the gas conductance model has no significant influence over the outputs of interest generated by FRAPCON-3. Despite the lack of a significant effect, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to decrease with enhanced gas conductivity was observed.

#### 4.4.6 Fission Gas Release

The fission gas release model was biased by multiplying or dividing gas diffusivity, D, by 2. The nominal model is shown in Figure 4.7. The biased models shown in Figures 4.8 and 4.9 bound most of the experimental data.

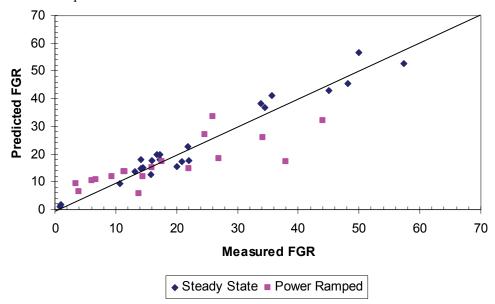
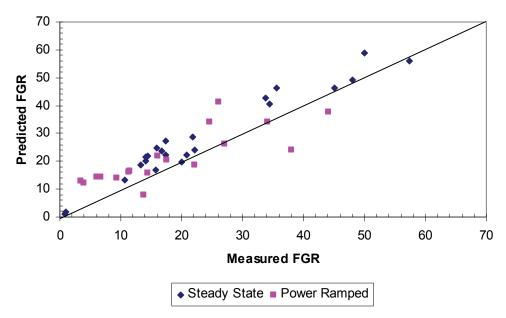
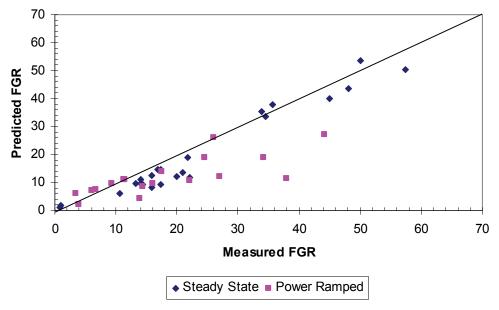


Figure 4.7 Nominal predicted vs. measured fission gas release



**Figure 4.8** Predicted vs. measured fission gas release for upper bound model with D\*2



**Figure 4.9** Predicted vs. measured fission gas release for lower bound model with D/2

# <u>PWR</u>

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the fission gas release model by \*2 or /2 are presented in Table 4.5 for comparison. Rod internal pressures varied by 12.3% from the base case on average and ranged from 9.69% at the negatively biased 40 GWd/MTU condition to 16.57% at the positively biased no AOO condition. Peak fuel centerline and cladding permanent hoop strain values varied from the base case by less than 0.6% and 0.8%, respectively. Based on this, it appears that model uncertainty in the fission gas release model has significant influence over rod internal pressure values and little influence on peak fuel

centerline temperature or cladding permanent hoop strain values generated by FRAPCON-3. The impact on fuel temperature would be more significant if the gap were open, e.g., at lower burnup. As expected, rod internal pressure significantly increased with increased fission gas release.

## **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the fission gas model by \*2 or /2 are presented in Table 4.6 for comparison. Rod internal pressures varied by 23.6% from the base case on average and ranged from 2.04% to 39.93% between the negatively and positively biased 30 GWd/MTU conditions, respectively. Peak fuel centerline and cladding permanent hoop strain values varied from the base case by less than 2.0% and 3.0%, respectively. Based on this, it appears that model uncertainty in the fission gas release model has significant influence over rod internal pressure values and little influence on peak fuel centerline temperature or cladding permanent hoop strain values generated by FRAPCON-3. The impact on fuel temperature would be more significant if the gap were open, e.g., at lower burnup. As expected, rod internal pressure significantly increased with increased fission gas release.

# 4.4.7 Cladding Corrosion

The cladding corrosion model was biased by  $\pm 40\%$ . The nominal model is shown in Figure 4.10. The models biased to bound nearly all experimental data are shown in Figures 4.11 and 4.12.

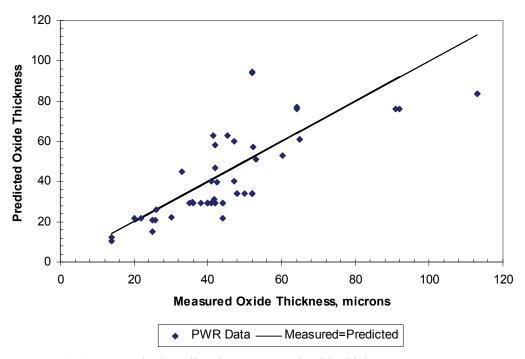


Figure 4.10 Nominal predicted vs. measured oxide thickness

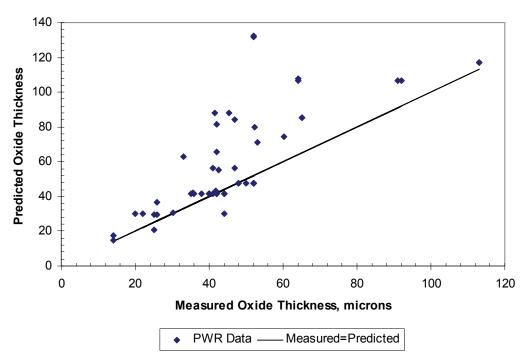


Figure 4.11 Predicted vs. measured oxide thickness for upper bound model with +40%

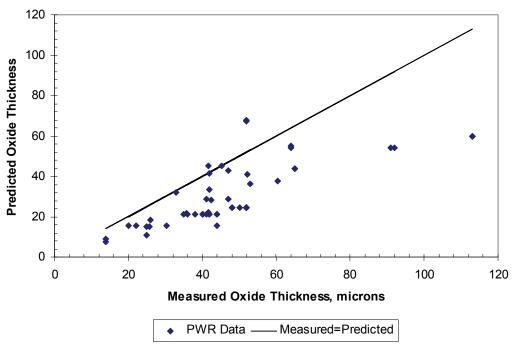


Figure 4.12 Predicted vs. measured oxide thickness for lower bound model with -40%

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the cladding corrosion model by  $\pm 40\%$  are presented in Table 4.5 for comparison. Rod internal pressures

varied by 2.5% from the base case on average and ranged from 0.83% at the positively biased 30 GWd/MTU condition to 4.67% at the positively biased no AOO condition. Peak fuel centerline temperatures varied from the base case by 1.0% on average and ranged from 0.33% at the negatively biased 30 GWd/MTU condition to 3.36% at the positively biased 50 GWd/MTU condition. Cladding permanent hoop strain values varied from the base case by 2.5% on average and ranged from 0.41% in the negatively biased 30 GWd/MTU condition to 9.28% in the positively biased 50 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding corrosion model has low to moderate influence on the outputs of interest generated by FRAPCON-3. It should be noted that cladding corrosion and hydriding can have a significant impact on cladding ductility. A tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with cladding corrosion was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the cladding corrosion model by ±40% are presented in Table 4.6 for comparison. Rod internal pressures varied by 0.4% from the base case on average and ranged from 0.00% at the negatively biased 40 GWd/MTU condition to 2.51% at the positively biased 50 GWd/MTU condition. Peak fuel centerline temperatures varied from the base case by 0.3% on average and ranged from 0.17% at the negatively biased 30 GWd/MTU condition to 0.39% at the positively biased 50 GWd/MTU condition. Cladding permanent hoop strain values varied from the base case by 0.3% on average and ranged from 0.07% in the negatively biased 40 GWd/MTU condition to 0.44% in the positively biased 50 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding corrosion model has no significant influence on the outputs of interest generated by FRAPCON-3. It should be noted that cladding corrosion and hydriding can have a significant impact on cladding ductility. Despite the lack of a significant effect, a tendency for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase with positively biased cladding corrosion was observed.

#### 4.4.8 Fuel Swelling

The fuel swelling model was biased by  $\pm 0.3\% \Delta V/V$  per 10 GWd/MTU, which bounds nearly all the data presented in Figure 4.13 as well as the Halden swelling data shown in Figure 2.69.

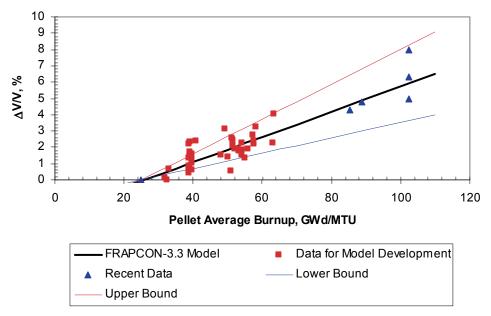


Figure 4.13 Fuel swelling model and available data with  $\pm 0.3\% \Delta V/V$  per 10 GWd/MTU as upper and lower bounds on the swelling rate

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the fuel swelling model by ±0.3 per 10GWd/MTU are presented in Table 4.5 for comparison. Rod internal pressure values varied from the base case by 1.6% on average and ranged from 0.00% at the negatively biased no AOO condition to 4.75% at the negatively biased 40 GWd/MTU condition. Peak fuel centerline temperatures varied from the base case by less than 0.1%. Cladding permanent hoop strain values varied form the based case by 2.1% on average and ranged from 0.03% at the no AOO conditions to 4.90% at the negatively biased 50 GWd/MTU condition. There is a significant impact on rod pressure limits based on no-cladding-liftoff criteria where the cladding creep rate cannot exceed the fuel swelling rate. Overall, it appears that model uncertainty in the fuel swelling model has a small influence over the rod internal pressure and cladding permanent hoop strain and little influence on peak fuel centerline temperature values generated by FRAPCON-3 at bunrups and LHGRs where the gap is closed. A tendency for rod internal pressure and cladding permanent hoop strain to increase and decrease with fuel swelling was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the fuel swelling model by ±0.3 per 10GWd/MTU are presented in Table 4.6 for comparison. Rod internal pressure values varied form the base case by 2.9% on average and ranged from 0.29% at the positively biased 30 GWd/MTU condition to 8.47% in the negatively biased no AOO condition. Peak fuel centerline temperatures varied from the base case by less than 0.25%. Cladding permanent hoop strain values varied from the base case by 7.8% and ranged from 2.64% to 16.89% at the positively and negatively biased 30 GWd/MTU conditions, respectively. There is a significant impact on rod pressure limits based on no-cladding-liftoff criteria where the

cladding creep rate cannot exceed the fuel swelling rate. Overall, it appears that model uncertainty in the fuel swelling model has a small to moderate influence on rod internal pressure and cladding permanent hoop strain values generated by FRAPCON-3 and little influence on peak fuel centerline temperature. Despite the lack of a significant effect, a tendency for rod internal pressure and cladding permanent hoop strain to increase and decrease with fuel swelling was observed.

## 4.4.9 Creep of Irradiated Cladding

The irradiated cladding creep model was biased by +10%/-40%, which bounds nearly all the data presented in Figure 4.14.

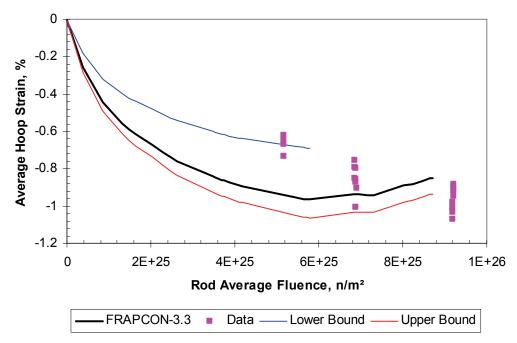


Figure 4.14 Cladding creep model and available data with +10%/-40% upper and lower bound on creep rate.

#### **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the irradiated cladding creep model by +10%/-40% are presented in Table 4.5 for comparison. Rod internal pressure values varied from the base case by 0.6% on average and ranged from 0.05% to 1.21% at the positively and negatively biased no AOO conditions, respectively. Peak fuel centerline temperatures and cladding permanent hoop strain values varied form the base case by less that 0.2%. The impact of cladding creep on fuel temperature will be significant at lower burnups when the gap is open. Also, there is a significant impact on rod pressure limits based on no-cladding-liftoff criteria where the cladding creep rate cannot exceed the fuel swelling rate. Overall, it appears that model uncertainty in the irradiated cladding creep model has no influence over the rod internal pressure, peak fuel centerline temperature and cladding permanent hoop strain values generated by FRAPCON-3.

## **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the irradiated cladding creep model by +10%/-40% are presented in Table 4.6 for comparison. Rod internal pressure and cladding permanent hoop strain values vary form the base case by less than 1.0 and 1.8%, respectively. Peak fuel centerline temperatures varied form the base case by less than 0.1%. The impact of cladding creep on fuel temperature will be significant at lower burnups when the gap is open. Also, there is a significant impact on rod pressure limits based on no-cladding-liftoff criteria where the cladding creep rate cannot exceed the fuel swelling rate. Overall, it appears that model uncertainty in the irradiated cladding creep model has no significant influence on rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values generated by FRAPCON-3.

## 4.4.10 Cladding Yield Strength

The cladding yield model was biased by adjusting the strength coefficient, K, by  $\pm$  30%. The nominal model is shown in Figure 4.15. The biased models bound nearly all experimental data as shown in Figures 4.16 and 4.17.

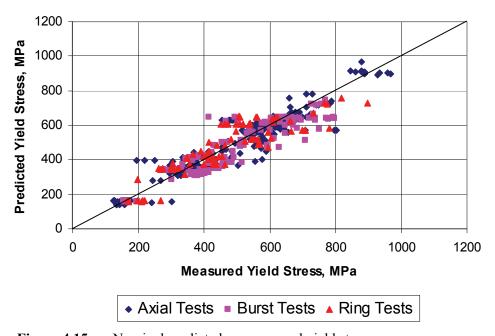
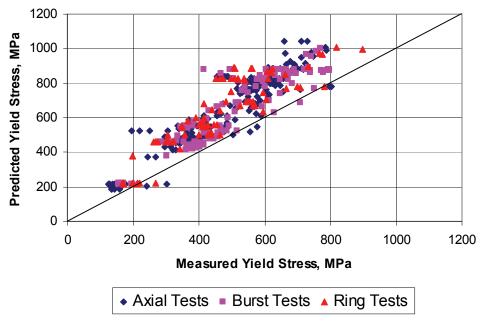


Figure 4.15 Nominal predicted vs. measured yield stress



**Figure 4.16** Predicted vs. measured yield stress for upper bound model with K\*1.3

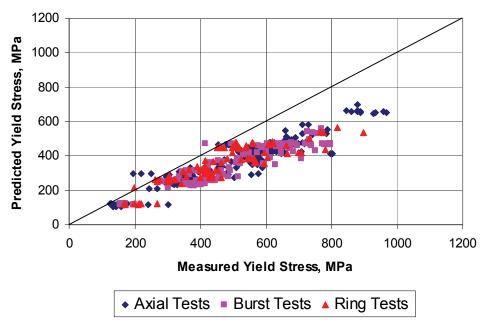


Figure 4.17 Predicted vs. measured yield stress for lower bound model with K/1.3

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the strength coefficient, K, of the cladding yield strength model by  $\pm$  30% are presented in Table 4.5 for comparison. Rod internal pressure, peak fuel centerline, and cladding permanent hoop strain values varied form the base case by less than 1.1%. Based on this, it appears that model

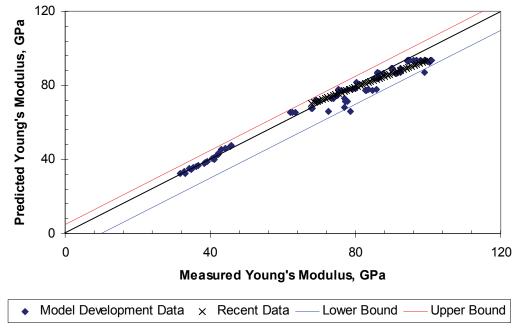
uncertainty in the cladding yield strength model has little influence over the outputs of interest generated by FRAPCON-3.

## **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the strength coefficient, K, of the cladding yield strength model by  $\pm$  30% are presented in Table 4.6 for comparison. Rod internal pressure and peak fuel centerline temperatures varied from the base case by less than 1.6% and 0.6% respectively. Cladding permanent hoop strain values varied from the base case by 1.7% on average and ranged from 0.15% at the positively biased 40 GWd/MTU condition to 6.05% at the positively biased 50 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding yield strength model has little influence on rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values generated by FRAPCON-3.

## 4.4.11 Young's Modulus of Cladding

The cladding Young's modulus model was biased by +5/-10GPa, which bounds nearly all the data presented in Figure 4.18.



**Figure 4.18** Predicted and measured cladding Young's Modulus data with +5/-10 GPa as upper and lower bounds

## **PWR**

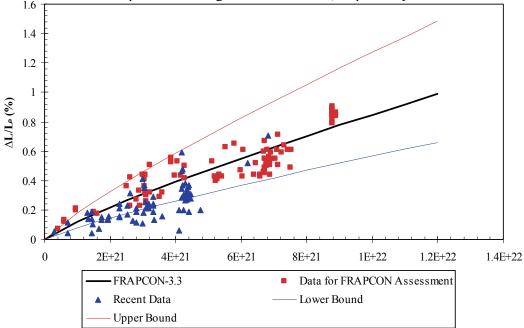
Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the Young's modulus of cladding model by + 5MPa and -10MPa are presented in Table 4.5 for comparison. Based on these results, it appears that model uncertainty in the Young's modulus of cladding model has no influence on rod internal pressure, fuel centerline temperature, or cladding permanent hoop strain values predicted by FRAPCON-3.

# **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the Young's modulus of cladding model by +5 MPa and -10MPa are presented in Table 4.6 for comparison. Based on these results, it appears that uncertainty in the Young's modulus model has no effect on rod internal pressure, fuel centerline temperature, or cladding permanent hoop strain values predicted by FRAPCON-3.

# 4.4.12 Cladding Axial Growth

The cladding axial growth models for PWR and BWR reactors were biased by  $\pm$  50%, which bounds most of the data presented in Figures 4.19 and 4.20, respectively.



**Figure 4.19** Cladding axial growth model for PWR cladding with ±50% as upper and lower bounds

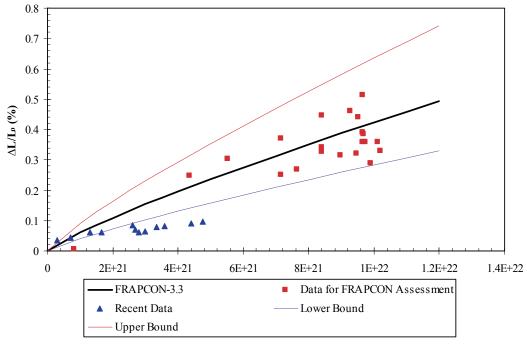


Figure 4.20 Cladding axial growth model for BWR cladding with ±50% as upper and lower bounds

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the cladding axial growth model by  $\pm$  50% are presented in Table 4.5 for comparison. Rod internal pressure values varied from the base case by 4.5% on average and ranged from 3.17% at the negatively biased 40 GWd/MTU condition to 6.23% at the positively biased 30 GWd/MTU condition. Peak fuel centerline temperatures varied from the base case by less than 0.1% and cladding permanent hoop strain values varied by 0.15% or less. Based on this, it appears that model uncertainty in the cladding axial growth model has a small effect on rod internal pressure and no effect on peak fuel centerline temperature or cladding permanent hoop strain values predicted by FRAPCON-3. A tendency for rod internal to increase or decrease with the cladding axial growth model was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the cladding axial growth model by  $\pm$  50% are presented in Table 4.6 for comparison. Rod internal pressure values varied form the base case by 2.9% on average and ranged from 1.34% at the positively biased 50 GWd/MTU condition to 3.64% at the positively biased 30 GWd/MTU condition. Peak fuel centerline temperature and cladding permanent hoop strain values varied by less then 0.05% and 0.3%, respectively. Based on this, it appears that model uncertainty in the cladding axial growth model has no significant effect on rod internal pressure and no effect on peak fuel centerline temperature or cladding permanent hoop strain values predicted by FRAPCON-3. Despite the lack of a significant effect, a tendency for rod internal to increase or decrease with the cladding axial growth model was observed.

# 4.4.13 Cladding Thermal Expansion

The cladding thermal expansion model was biased by  $\pm$  30%. Figures 4.21 and 4.22 present diametral and axial thermal expansion data, respectively, with most of the experimental bounded by the bias.

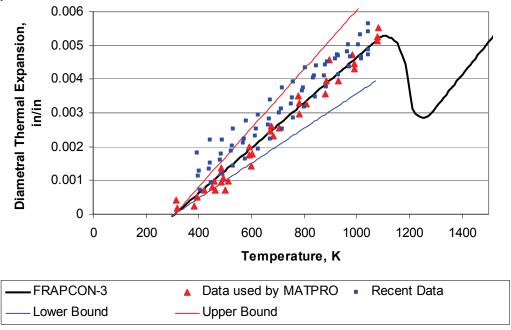


Figure 4.21 Cladding diametral thermal expansion model with  $\pm 30\%$  as upper and lower bounds

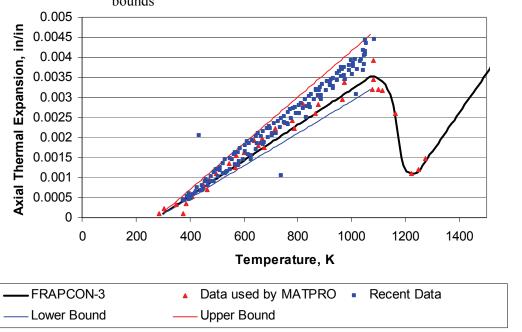


Figure 4.22 Cladding axial thermal expansion model with +30%/-10% as upper and lower bounds

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the cladding thermal expansion model by  $\pm$  30% are presented in Table 4.5 for comparison. Rod internal pressure and peak fuel centerline temperature values varied from the base case by less than 0.5%. Cladding permanent hoop strain values varied from the base case by 1.2% on average and ranged from 0.67% at the negatively biased 30 GWd/MTU condition to 1.95% at the positively biased 50 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding thermal expansion model has no significant effect on outputs of interest generated by FRAPCON-3. Despite the lack of a significant effect, a tendency for cladding permanent hoop strain to vary inversely with cladding thermal expansion was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the cladding thermal expansion model by  $\pm$  30% are presented in Table 4.6 for comparison. Rod internal pressure values varied form the base case by 0.3% on average and ranged from 0.01% at the positively biased 30 GWd/MTU condition to 1.10% at the negatively biased 50 GWd/MTU condition. Peak fuel centerline temperatures varied from the base case by less than 0.05%. Cladding permanent hoop strain values varied from the based case by 1.1% and ranged from 0.58% at the negatively biased 50 GWd/MTU condition to 1.79% at the positively biased 30 GWd/MTU condition. Based on this, it appears that model uncertainty in the cladding thermal expansion model has no significant effect on the outputs of interest generated by FRAPCON-3. Despite the lack of a significant effect, a tendency for cladding permanent hoop strain to increase with decreased cladding thermal expansion was observed.

## 4.5 Effects of Power Uncertainties

Power uncertainties include fluctuations in the steady state power as well as the range of times and power levels that may be experienced during an AOO. In this study, the steady state power was varied by 10% over the entire power history to account for uncertainties in the calculation of steady state power. In addition, an AOO resulting in a 50% increase in power output for a period of 4 hrs was also considered. To study the influence of uncertainty in this AOO, two separate instances were analyzed. In the first case, the power increase was varied from 40% to 60%. The second case consisted of decreasing and increasing the duration of the transient by 1 hour. Results of the power uncertainty study are presented in Tables 4.7 and 4.8 and discussed in the following subsections.

Comparison between unbiased output and output biased by power uncertainties for a 17x17 PWR **Table 4.7** 

			Steady S	tate	Height of A(		Duration	of Pulse
Condition	Responses	Unbiased	+ 10%	- 10%	%09 +		+ 1hr	- 1hr
No AOO	Rod Internal Pressure (MPa)	12.16	14.59	68.6	₹		۷Z	₹
	Peak Fuel Centerline T (°C)	1590	1751	1432	¥		Ν	Š
8	Rod Internal Pressure (MPa)	13.25	Ϋ́	Ϋ́	13.85		13.42	12.88
GWd/MTU	Peak Fuel Centerline T (°C)	2319	Α	Ϋ́	2446		2321	2317
	Cladding Permanent $\Box_{h\infty p}\left(\% ight)$	0.4354	N A	N	0.5430		0.4414	0.4277
4	Rod Internal Pressure (MPa)	14.13	Ϋ́	Ϋ́	14.86		14.48	13.63
GWd/MTU	Peak Fuel Centerline T (°C)	2079	Α V	Ϋ́	2200		2080	2077
	Cladding Permanent $\Box_{h\infty p}$ (%)	0.3575	75 NA	Ν	0.4552	0.4552 0.2584	0.3630 0.3503	0.3503
22	Rod Internal Pressure (MPa)	14.20	Ϋ́	Ϋ́	15.13		14.45	13.25
GWd/MTU	Peak Fuel Centerline T (°C)	1788	Ϋ́	Ϋ́	1899	1676	1789	1786
	Cladding Permanent ⊏ <sub>h∞p</sub> (%)	0.2672	Ϋ́	Ϋ́Z	0.3514	0.1846	02715	0.2611

Comparison between unbiased output and output biased by power uncertainties for a 10x10 BWR Table 4.8

			Steady State	ate	Height of A	OO Pulse	Duration o	of Pulse
Condition	Responses	Unbiased	+ 10%	- 10%	%09 +	+ 40%	+1hr	-1hr
No AOO	Rod Internal Pressure (MPa)	5.37	5.97	4.21	Ϋ́	Ϋ́Z	Ϋ́Z	Ϋ́
	Peak Fuel Centerline T (°C)	1234	1364	1110	NA	∢ Z	٩	Ϋ́
30	Rod Internal Pressure (MPa)	5.30	Ϋ́	Ϋ́	6.22	4.66	5.49 5.04	5.04
GWd/MTU	Peak Fuel Centerline T (°C)	1868	ΑN	Ν	2000	1733	1871	1862
	Cladding Permanent $\epsilon_{\text{hoop}}$ (%)	0.3180	Ą	ΑN	0.4210	0.2163	0.3244	0.3081
!		!	;		İ	!	ļ	
40	Rod Internal Pressure (MPa)	6.56	Ϋ́	ΑN	7.76	5.47	6.72	6.13
GWd/MTU	Peak Fuel Centerline T (°C)	1729	Ϋ́	ΑN	1849	1606	1732	1725
	Cladding Permanent $\epsilon_{ ext{hoop}}$ (%)	0.2683	Ϋ́	Ϋ́	0.3599	0.1775	0.2742	0.2608
20	Rod Internal Pressure (MPa)	6.73	Ϋ́	Ν Α	8.18	5.72	7.26	09.9
GWd/MTU	Peak Fuel Centerline T (°C)	1530	Ϋ́	Ν Α	1636	1426	1531	1524
	Cladding Permanent $\epsilon_{hoop}$ (%)	0.2067	Ϋ́	ΑN	0.2844	0.1326	0.2111	0.1994

## 4.5.1 Steady State

## **PWR**

Rod internal pressure and peak fuel centerline temperature values for an unbiased 17X17 PWR base case and cases biased by adjusting the steady state power by  $\pm 10\%$  are presented in Table 4.7 for comparison. The average variance in rod internal pressure and peak fuel centerline temperature is 20% and 10%, respectively. Based on these results, it is appears that power uncertainty in steady state power has a major effect on rod internal pressure and peak fuel centerline temperature.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting steady state power by  $\pm 10\%$  are presented in Table 4.8 for comparison. The average variance in rod internal pressure and peak fuel centerline temperature is 15% and 10%, respectively. Based on these results it appears that power uncertainty in steady state power has a major effect on rod internal pressure and peak fuel centerline temperature.

# 4.5.2 Height of AOO Pulse

## **PWR**

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the height of AOO pulse by ±10% are presented in Table 4.7 for comparison. The average variance in rod internal pressure is 5.9% and varies from 4.53% at the positively biased 30 GWd/MTU condition to 7.98% at the negatively biased 40 GWd/MTU condition. Peak fuel centerline temperatures varied from the unbiased case by an average of 6.0% and ranged from 5.47% at the positively biased 30 GWd/MTU condition to 6.25% at the positively biased 50 GWd/MTU condition. Cladding permanent hoop strain values varied, on average, by 28.0% from the unbiased case. Cladding variance ranged from 24.71% at the positively biased 30 GWd/MTU condition to 31.51% at the positively biased 50 GWd/MTU condition. Based on these results, it appears that power uncertainty in AOO pulse height has a moderate effect on rod internal pressure and peak fuel centerline temperature, and a major effect on cladding permanent hoop strain values generated by FRAPCON-3. A trend for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with AOO pulse height was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the height of AOO pulse by ±10% are presented in Table 4.8 for comparison. The average variance in rod internal pressure is 16.8% and varies from 12.05% at the negatively biased 30 GWd/MTU condition to 21.61% at the positively biased 50 GWd/MTU condition. Peak fuel centerline temperatures varied, on average, by 7.0% and ranged from 6.80% at the negatively biased 50 GWd/MTU condition to 7.25% at the negatively biased 30 GWd/MTU condition. Cladding permanent hoop strain values varied from the base case by 34.3%, on average and ranged from 31.98% at the negatively biased 30 GWd/MTU condition to 37.59% at the positively biased 50GWd/MTU condition. Based on these results it appears that power uncertainty in the AOO

pulse height has a moderate effect on peak fuel centerline temperature, and a major effect on rod internal pressure and cladding permanent hoop strain values predicted by FRAPCON-3. A trend for rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with AOO pulse height was observed.

#### 4.5.3 **Duration of AOO Pulse**

## <u>PWR</u>

Rod internal pressure, peak fuel centerline temperature, and cladding permanent hoop strain values for an unbiased 17X17 PWR base case and cases biased by adjusting the duration of AOO pulse by ±1hr are presented in Table 4.7 for comparison. The average variance in rod internal pressure is 3.1% and varies from 1.24% at the positively biased 30 GWd/MTU condition to 6.67% at the negatively biased 50 GWd/MTU condition. Peak fuel centerline temperatures, on the other hand, varied by 0.1% or less. Cladding permanent hoop strain values varied by 1.8% on average and ranged from 1.38% at the positively biased 30 GWd/MTU condition to 2.28% at the negatively biased 50 GWd/MTU condition. Based on this, it appears that power uncertainty in the AOO pulse duration has a moderate effect on the outputs of interest generated by FRAPCON-3. A trend for rod internal pressure, fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with the duration of AOO pulse was observed.

#### **BWR**

Outputs of interest for the unbiased 10X10 BWR base case and cases biased by adjusting the duration of AOO pulse by ±1hr are presented in Table 4.8 for comparison. The average variance in rod internal pressure is 4.5% and varies from 1.90% at the negatively biased 50 GWd/MTU condition to 7.89% at the positively biased 50 GWd/MTU condition. Peak fuel centerline temperatures varied by less than 0.5%. Cladding permanent hoop strain values varied from the base case by 2.6% on average and ranged from 2.01% at the positively biased 30 GWd/MTU condition to 3.53% at the negatively biased 50 GWd/MTU condition. Based on this, it appears that power uncertainty in the AOO pulse duration has a moderate effect on the outputs of interest generated by FRAPCON-3. A trend for rod internal pressure, fuel centerline temperature, and cladding permanent hoop strain to increase and decrease with the duration of AOO pulse was observed.

#### 4.6 Conclusions

The influence of manufacturing, model, and power uncertainties on outputs of interest generated by FRAPCON-3 has been evaluated. Overall, it appears that manufacturing uncertainties have a small influence over the outputs of interest. The average variation between unbiased PWR and BWR base cases and cases biased by manufacturing uncertainties is typically less than 7%. Model uncertainties, on the other hand, significantly influence outputs of interest generated by FRAPCON-3 and may result in values that differ from the base cases by as much as 60%. This underscores the importance of exercising care in the selection and derivation of models and fitting parameters. Finally, evaluation of power uncertainties has revealed variation in steady state power has a major impact on centerline temperature and rod internal pressure and that the AOO pulse height has a more significant influence than the pulse duration on FRAPCON-3 outputs. In particular, cladding permanent hoop strain values can vary from the base case by as much as 34% when the AOO pulse height is varied from the base case by  $\pm 10\%$ . The following subsections summarize the individual sources of uncertainty that have a significant impact on outputs of interest generated by FRAPCON-3.

The conclusions of this example sensitivity study could change depending on power histories. For example, if the peak power started higher than assumed here and dropped off at lower burnup, the gap would be open at lower burnup. This could make cladding creep, fuel swelling and fission gas release more important to the peak fuel centerline temperature predictions.

#### 4.6.1 Rod Internal Pressure

Individual manufacturing uncertainties only influenced rod internal pressure values by 5% or less, however, examination of model uncertainties revealed that rod internal pressure values can be significantly influenced by uncertainty in the fuel thermal conductivity and fission gas release models. Rod internal pressure values varied, on average, from the PWR and BWR base cases by approximately 32% and 60%, respectively, when the fuel thermal conductivity model is biased by ±0.5W/m-K. Biasing the diffusivity of the fission gas release model by ±2 resulted variations from the base case by 12% and 24% for PWR and BWR cases, respectively. Power uncertainty also had a significant influence on rod internal pressure. The uncertainty in steady state power has a major impact on the prediction of rod internal pressure. In addition, variation in AOO pulse height results rod internal pressures varying by 17% from the BWR base case. However, this effect was not as significant for the PWR, as the biased AOO pulse height only varied from the base case by 6%.

## 4.6.2 Peak Fuel Centerline Temperature

Peak fuel centerline temperature values were insensitive to individual manufacturing uncertainties. However, biasing the fuel thermal conductivity model by  $\pm 0.5$ W/m-K resulted in variation from the PWR and BWR base cases by 20 and 22%, respectively. Power uncertainties have a major impact on peak fuel centerline temperature.

## 4.6.3 Cladding Permanent Hoop Strain

Cladding permanent hoop strain values were insensitive to individual manufacturing uncertainties. However, model uncertainty in the fuel thermal conductivity and fuel thermal expansion models resulted in significant variation from the PWR and BWR base cases. Biasing the fuel thermal conductivity model by  $\pm 0.5$ W/m-K resulted in variations of 36 and 52% from the PWR and BWR base cases, respectively. Biasing the fuel thermal expansion model by  $\pm 15\%$  resulted in variations of 19 and 21% from the PWR and BWR base cases, respectively. Power uncertainties also influence cladding permanent hoop strains. In particular, biasing the AOO pulse height by  $\pm 10\%$  resulted in values that varied by 28 and 34% from the PWR and BWR base cases, respectively.

## 5.0 CONCLUSIONS

The conclusion of this assessment is that both FRAPCON-3.3 and FRAPTRAN-1.3 provide best-estimate predictions of fuel and cladding temperatures and cladding stress and strain. The assessments of each model and the assessments of the combined model predictions are shown in Section 2. Several areas have been identified as areas that should be re-examined and new models developed to improve the model's predictive capability. These areas are outlined below.

- Cladding corrosion: The model for hydrogen pickup in Zircaloy-2 under BWR conditions was found to over-predict hydrogen data. A new model was developed and is described in Section 3.1.1. The model for corrosion of ZIRLO<sup>TM</sup> was found to under-predict cladding corrosion at high burnup (>60 GWd/MTU). New model parameters were developed and are described in Section 3.1.2. The model for corrosion of M5<sup>TM</sup> was found to over-predict cladding corrosion at high burnup (>60 GWd/MTU). New model parameters were developed and are described in Section 3.1.3. After making this adjustment, it was also necessary to change the hydrogen pickup for M5<sup>TM</sup> as described in Section 3.1.3.
- Radial power profile: The TUBRNP subroutine that calculates radial power profile was updated as recommended by the authors of the subroutine to model the radial power profile in the HWR neutron spectrum as well as a LWR neutron spectrum. The details of this update are described in Section 3.2. A lookup and interpolation routine was developed and implemented in FRAPCON-3.4 to model the radial power profile for UO<sub>2</sub>-Gd<sub>2</sub>O<sub>3</sub> fuel in both HWR and LWR neutron spectrums. The details of this update are described in Section 3.3
- UO<sub>2</sub> thermal expansion: The model for UO<sub>2</sub> fuel thermal expansion was found to slightly under-predict expansion strain at high temperature between 2500K and 3000K. Although this under prediction was within the scatter of the data, new model parameters were developed to predict the mean of the expansion strain data at high temperature and are described in Section 3.4.
- Gas conductivity: The gas conductivity models do not model the conductivity well for most gasses beyond 1100K. This will not affect most of the temperature predictions since the gas does not typically exceed 1000K. New data model parameters were developed to better predict gas conductivity at high temperature and are described in Section 3.5.
- Steam conductivity: The steam conductivity models in FRAPCON-3.3 and FRAPTRAN 1.3 were not the same. In addition, neither model predicted the data well. The models in both codes were changed to match the ASME model as described in Section 3.6. This is most important in FRAPTRAN-1.3 where the gap may be filled with steam after cladding rupture.
- Cladding irradiation creep: That the cladding irradiation creep model in FRAPCON-3.3 predicts creepdown to occur too rapidly. A new model has been selected and compared to creepdown data from fuel rods and from in-reactor pressurized cladding tube creep tests. This model is described in Section 3.7.

The influence of manufacturing, model, and power uncertainties on outputs of interest generated by FRAPCON-3.3 has been evaluated. Overall, it appears that manufacturing uncertainties on an individual basis have a small to moderate or little influence over the outputs of interest. The average variation between unbiased PWR and BWR base cases and cases biased by individual manufacturing uncertainties is typically less than 5%. Individual model uncertainties, on the other hand, significantly influence outputs of interest generated by FRAPCON-3.3 and may result in values that differ from the base cases by as much as 60%. This underscores the importance of exercising care in the selection and derivation of models and fitting parameters. Finally, evaluation of power uncertainties has revealed that the uncertainty on steady state power has a

major impact on the prediction of fuel centerline temperature and rod internal gas pressure. In addition, for a 50% overpower even with a 4 hour hold time, the pulse height has a more significant influence than the pulse duration on FRAPCON-3.3 outputs. In particular, cladding permanent hoop strain values can vary from the base case by as much as 34% when the AOO pulse height is varied from the base case by  $\pm 10\%$ . The individual sources of uncertainty that have a significant impact on outputs of interest generated by FRAPCON-3.3 are summarized below.

- Rod Internal Pressure: Although manufacturing uncertainty only influenced rod internal pressure values by 5% or less, examination of model uncertainties revealed that rod internal pressure values can be significantly influenced by uncertainty in the fuel thermal conductivity and fission gas release models. Rod internal pressure values varied, on average, from the PWR and BWR base cases by approximately 32% and 60%, respectively, when the fuel thermal conductivity model is biased by ±0.5W/m-K. Biasing the diffusivity of the fission gas release model by ±2 resulted variations from the base case by 12% and 24% for PWR and BWR cases, respectively. Power uncertainty also had a significant influence on rod internal pressure. The uncertainty in steady state power has a major impact on the prediction of rod internal pressure. In addition, variation in AOO pulse height results rod internal pressures varying by 17% from the BWR base case. However, this effect was not as significant for the PWR, as the biased AOO pulse height only varied from the base case by 6%.
- Peak Fuel Centerline Temperature: Peak fuel centerline temperature values were insensitive to manufacturing uncertainty. However, biasing the fuel thermal conductivity model by ±0.5W/m-K resulted in variation from the PWR and BWR base cases by 20 and 22%, respectively. Power uncertainties have a major impact on peak fuel centerline temperature.
- Cladding Permanent Hoop Strain: Cladding permanent hoop strain values were insensitive to manufacturing uncertainty. However, model uncertainty in the fuel thermal conductivity and fuel thermal expansion models resulted in significant variation from the PWR and BWR base cases. Biasing the fuel thermal conductivity model by ±0.5W/m-K resulted in variations of 36 and 52% from the PWR and BWR base cases, respectively. Biasing the fuel thermal expansion model by ±15% resulted in variations of 19 and 21% from the PWR and BWR base cases, respectively. Power uncertainties also influence cladding permanent hoop strains. In particular, biasing the AOO pulse height by ±10% resulted in values that varied by 28 and 34% from the PWR and BWR base cases, respectively.

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10. SUPPLEMENTARY NOTES

J.C. Voglewede, NRC Project Manager

11. ABSTRACT (200 words or less)

The latest versions of the fuel performance codes, FRAPCON-3 and FRAPTRAN, were examined to ensure best estimate behavior of the codes and to ensure (to the extent possible) that unintentional bias has been eliminated. Each individual model and type of code prediction was examined and compared to the data that was used to develop the model. In addition, a brief literature search was performed to determine if more recent data have become available since the original model development for model comparison. If new data were discovered, these data were compared to the models and code predictions in FRAPCON-3.3 and FRAPTRAN-1.3 in order to determine if the model is biased. Models or integral effect prediction found to be biased relative to the data were updated and corrected in the upcoming versions of the codes, FRAPCON-3.4 and FRAPTRAN 1.4. Areas where modeling may be lacking were noted for further model development. The details of the updated models are provided in this report.

Subsequently, a sensitivity study was performed on the steady-state code, FRAPCON-3.3 to determine the effects of uncertainty in model predictions, manufacturing parameters and power history on the code outputs of regulatory interest.

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